PMT

Given that $f(x) = x(x+2)^3$, find f'(x)1

a by first expanding f(x),

b using the product rule.

Differentiate each of the following with respect to x and simplify your answers. 2

- $\mathbf{a} x \mathbf{e}^x$
- **b** $x(x+1)^5$
- $\mathbf{c} \quad x \ln x$
- **d** $x^2(x-1)^3$

- **e** $x^3 \ln 2x$ **f** $x^2 e^{-x}$
- **g** $2x^4(5+x)^3$ **h** $x^2(x-3)^4$

Find $\frac{dy}{dx}$, simplifying your answer in each case. 3

- **a** $y = x(2x-1)^3$ **b** $y = 3x^4e^{2x+3}$
- $\mathbf{c} \quad y = x\sqrt{x-1}$

- $\mathbf{d} \quad y = x^2 \ln (x + 6)$
- **e** $y = x(1-5x)^4$ **f** $y = (x+2)(x-3)^3$
- $\mathbf{g} \quad \mathbf{v} = x^{\frac{4}{3}} \mathbf{e}^{3x}$
- **h** $y = (x+1) \ln (x^2 1)$ **i** $y = x^2 \sqrt{3x+1}$

Find the value of f'(x) at the value of x indicated in each case. 4

- **a** $f(x) = 4xe^{3x}$,
- x = 0 \mathbf{b} $f(x) = 2x(x^2 + 2)^3$, x = -1
- **c** $f(x) = (5x 4) \ln 3x$, $x = \frac{1}{3}$ **d** $f(x) = x^{\frac{1}{2}} (1 2x)^3$, $x = \frac{1}{4}$

5 Find the coordinates of any stationary points on each curve.

 $\mathbf{a} \quad \mathbf{v} = x\mathbf{e}^{2x}$

- **b** $y = x(x-4)^3$
- **c** $y = x^2(2x 3)^4$

- **d** $y = x\sqrt{x+12}$
- **e** $y = 2 + x^2 e^{-4x}$ **f** $y = (1 3x)(3 x)^3$

6 Find an equation for the tangent to each curve at the point on the curve with the given *x*-coordinate.

- **a** $y = x(x-2)^4$,
- x = 1 **b** $y = 3x^2 e^x$,
- x = 1

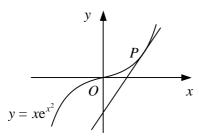
- **c** $y = (4x 1) \ln 2x$, $x = \frac{1}{2}$ **d** $y = x^2 \sqrt{x + 6}$, x = -2

7 Find an equation for the normal to each curve at the point on the curve with the given *x*-coordinate. Give your answers in the form ax + by + c = 0, where a, b and c are integers.

- **a** $y = x^2(2-x)^3$,
- x = 1 **b** $y = x \ln (3x 5)$,

- $\mathbf{c} \quad \mathbf{v} = (x^2 1)e^{3x}$
- x = 0 **d** $y = x\sqrt{x-4}$. x = 8

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The diagram shows part of the curve with equation $y = xe^{x^2}$ and the tangent to the curve at the point *P* with *x*-coordinate 1.

a Find an equation for the tangent to the curve at *P*.

b Show that the area of the triangle bounded by this tangent and the coordinate axes is $\frac{2}{3}$ e.