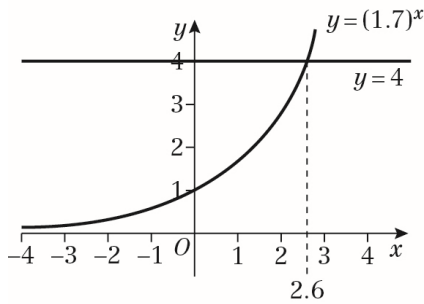
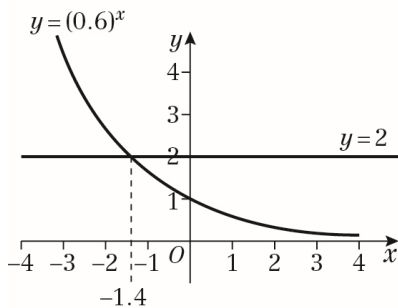


## Exercise 5A

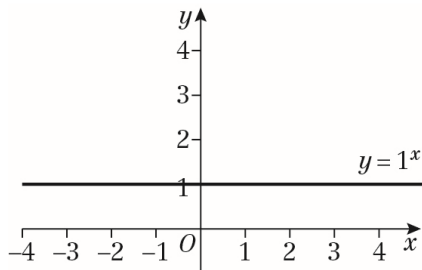
1 a

b Where  $y = 4$ ,  $x \approx 2.6$ 

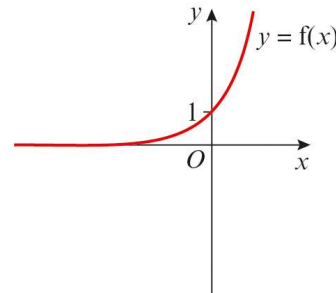
2 a

b Where  $y = 2$ ,  $x \approx -1.4$ 

3

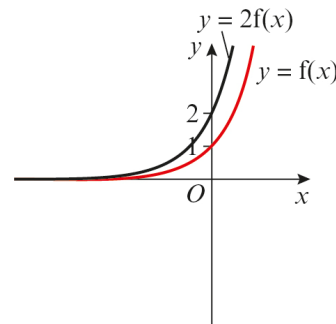
4 a True because, when  $x = 0$ ,  $a^0 = 1$  when  $a$  is positiveb False. For example, when  $a = \frac{1}{2}$ , the function  $f(x) = a^x$  is not an increasing function.c True because, when  $a$  is positive,  $a^x > 0$  for all values of  $x$ .

5 a The graph crosses the  $y$ -axis when  $x = 0$ .  
 $y = 3^0$   
 So  $y = 1$   
 The graph crosses the  $y$ -axis at  $(0, 1)$ .  
 Asymptote is at  $y = 0$ .



b The graph is a vertical stretch by scale factor 2.

The graph crosses the  $y$ -axis when  $x = 0$ .  
 $y = 2 \times 3^0$   
 So  $y = 2$   
 The graph crosses the  $y$ -axis at  $(0, 2)$ .  
 Asymptote is at  $y = 0$ .



- 5 c The graph is a translation by the vector  $\begin{pmatrix} 0 \\ -4 \end{pmatrix}$ .

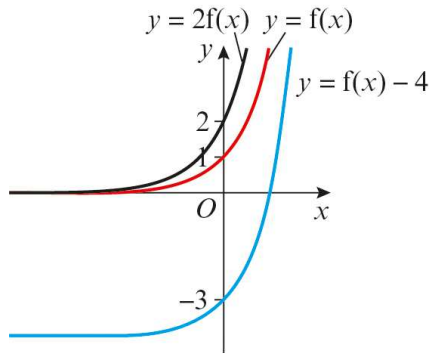
The graph crosses the  $y$ -axis when  $x = 0$ .

$$y = 3^0 - 4$$

$$\text{So } y = -3$$

The graph crosses the  $y$ -axis at  $(0, -3)$ .

Asymptote is at  $y = -4$ .



- d The graph is a horizontal stretch by scale factor 2.

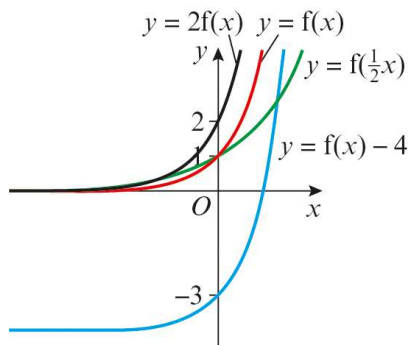
The graph crosses the  $y$ -axis when  $x = 0$ .

$$y = 3^{\frac{1}{2} \times 0}$$

$$\text{So } y = 1$$

The graph crosses the  $y$ -axis at  $(0, 1)$ .

Asymptote is at  $y = 0$ .



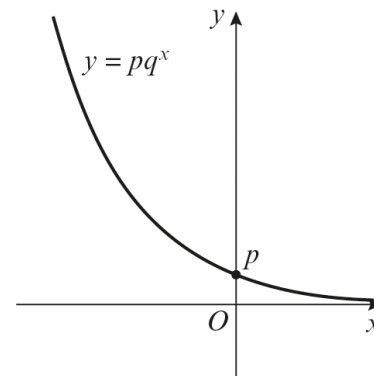
- 6 Substitute the coordinates into  $y = ka^x$ .  
 $6 = ka^1$  (equation 1)  
 $48 = ka^4$  (equation 2)  
 Solve simultaneously: divide equation 2 by equation 1,

$$48 \div 6 = \frac{ka^4}{ka}$$

$$a^3 = 8$$

$$a = 2, k = 3$$

- 7 a As  $x$  increases,  $y$  decreases



- b Substitute the coordinates into  $y = pq^x$ .  
 $150 = pq^{-3}$  (equation 1)  
 $0.048 = pq^2$  (equation 2)  
 Solve simultaneously, divide equation 2 by equation 1.

$$0.048 \div 150 = \frac{pq^2}{pq^{-3}}$$

$$q^5 = 0.00032$$

$$q = 0.2$$

$$p = 0.048 \div 0.2^2 = 1.2$$

$$p = 1.2, q = 0.2$$

**Challenge**

To draw the graph, note that it is a translation of the graph  $y = 2^x$  by the vector  $\begin{pmatrix} 2 \\ 5 \end{pmatrix}$ .

The graph crosses the  $y$ -axis when  $x = 0$ ,  
so  $y = 2^{0-2} + 5$   
 $y = 5.25$

The graph crosses the  $y$ -axis at  $(0, 5.25)$ .  
Asymptote is at  $y = 5$ .

