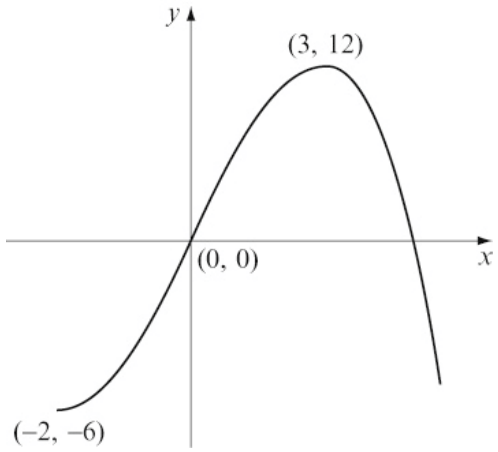
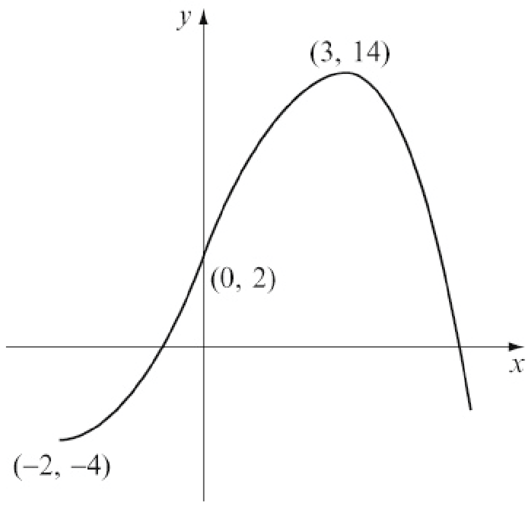
Exercise 2F

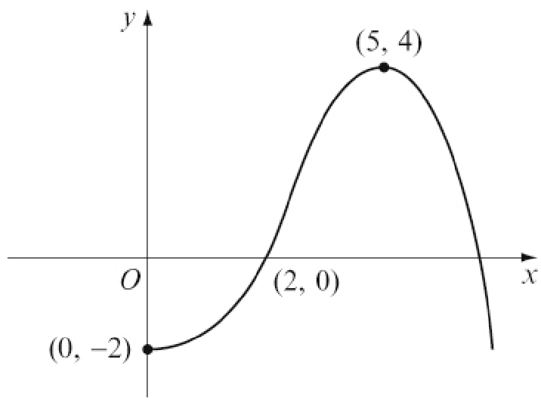
1 a $y = 3\mathrm{f}(x)$
Vertical stretch, scale factor 3.



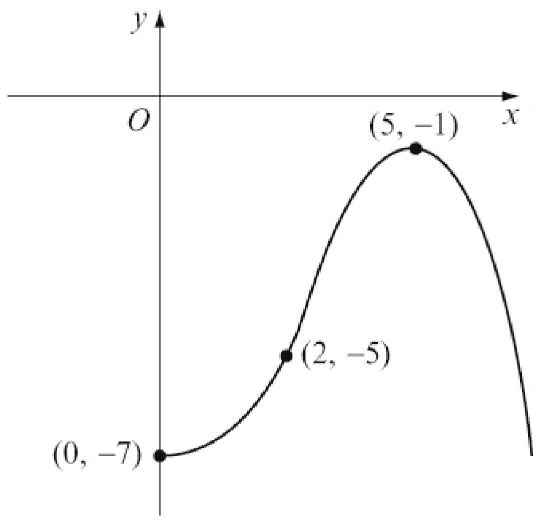
$y = 3\mathrm{f}(x) + 2$. Vertical translation of +2.



b $y = \mathrm{f}(x-2)$.
Horizontal translation of $+2$.



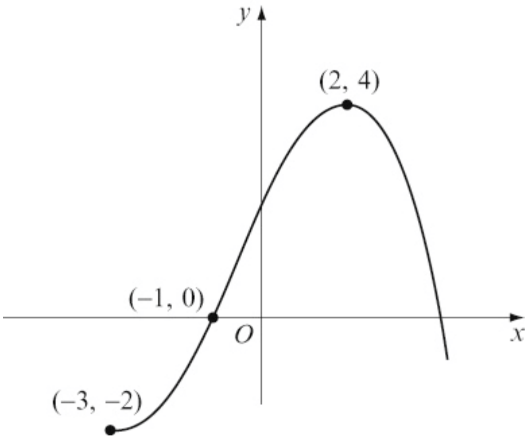
$y = \mathrm{f}(x-2) - 5$.
Vertical translation of -5.



© Pearson Education Ltd 2019. Copying permitted for purchasing institution only. This material is not copyright free.

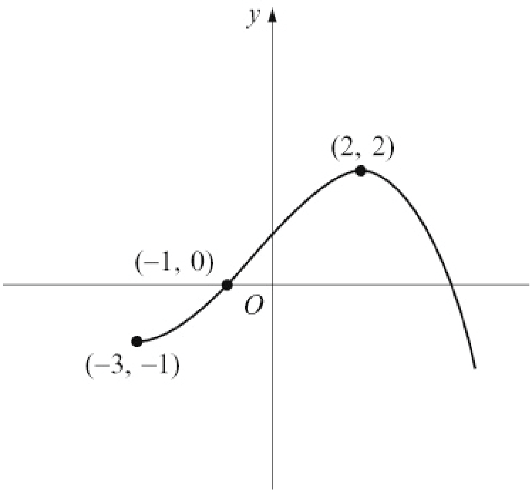
1 c $y = \mathrm{f}(x+1)$

Horizontal translation of -1.



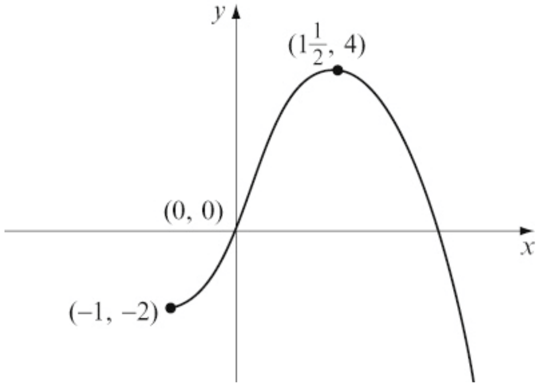
$y = \frac{1}{2}\mathrm{f}(x+1)$

Vertical stretch, scale factor $\frac{1}{2}$



d $y = \mathrm{f}(2x)$

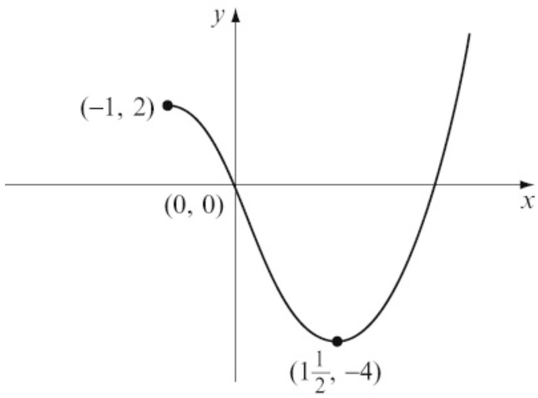
Horizontal stretch, scale factor $\frac{1}{2}$



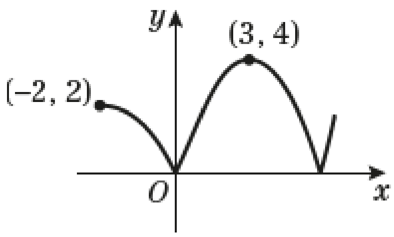
$y = -\mathrm{f}(2x)$

Reflection in the x-axis.

(or Vertical stretch, scale factor -1).



e $y = |\mathrm{f}(x)|$. Reflect, in the x-axis, the parts of the graph that lie below the x-axis.

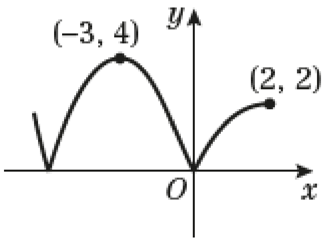


© Pearson Education Ltd 2019. Copying permitted for purchasing institution only. This material is not copyright free.

1 f $y = \mathrm{f}(-x)$. Reflection in the y-axis.

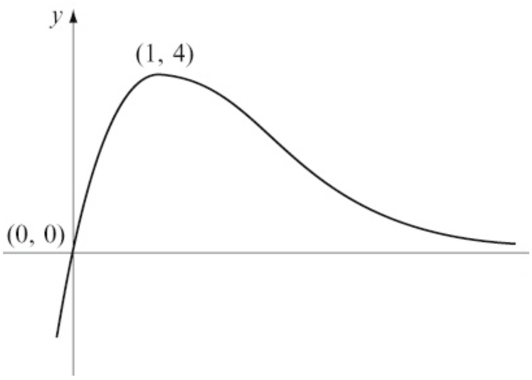
$y = |\mathrm{f}(-x)|$.

Reflect, in the x-axis, the parts of the graph that lie below the x-axis.



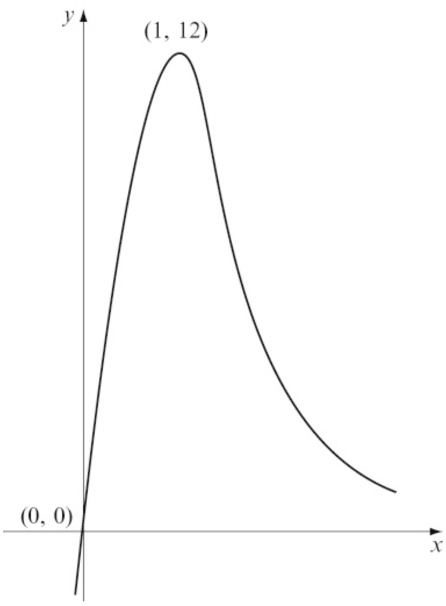
2 a $y = \mathrm{f}(x-2)$

Horizontal translation of $+2$



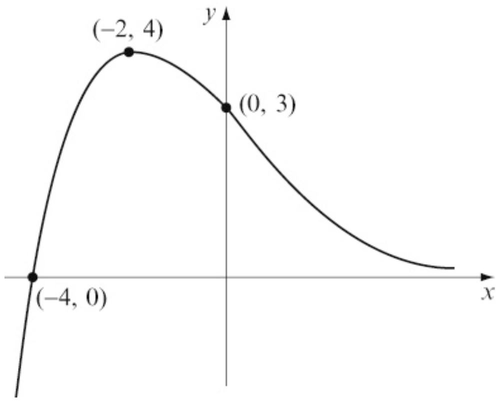
$y = 3\mathrm{f}(x-2)$

Vertical stretch, scale factor 3.



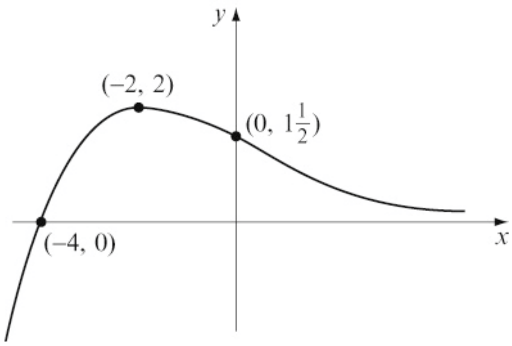
2 b $y = \mathrm{f}\left(\frac{1}{2}x\right)$

Horizontal stretch, scale factor 2.



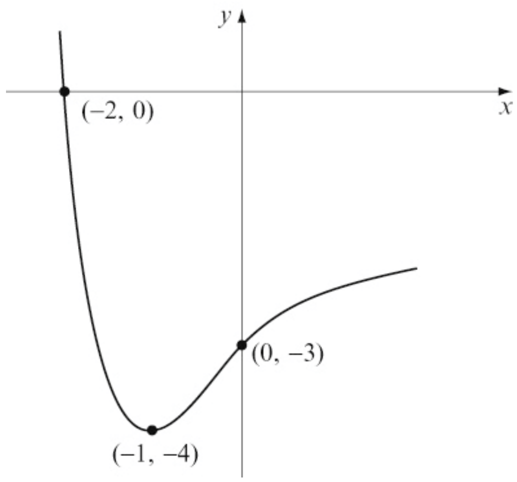
$y = \frac{1}{2}\mathrm{f}\left(\frac{1}{2}x\right)$

Vertical stretch, scale factor $\frac{1}{2}$

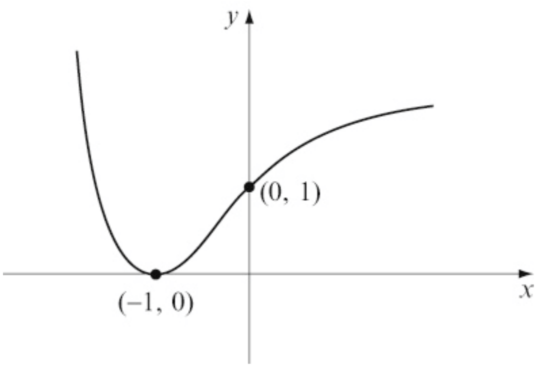


2 c $y = -f(x)$

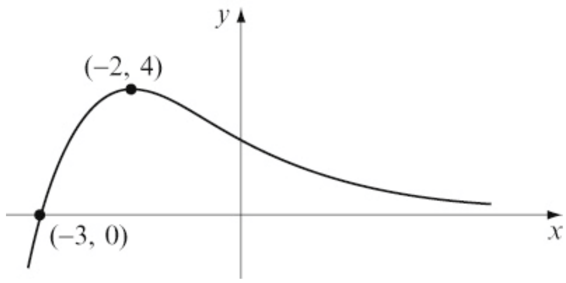
Reflection in the x-axis.
(Or vertical stretch, scale factor -1).



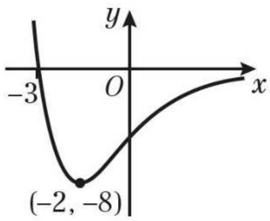
$y = -f(x) + 4$
Vertical translation of $+4$.



2 d $y = f(x+1)$
Horizontal translation of -1.



$y = -2f(x+1)$
Reflection in the x-axis,
and vertical stretch, scale factor 2.

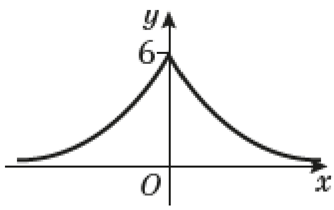


2 e $y = f(|x|)$ can be written

$$y = \begin{cases} f(x), & x \geq 0 \\ f(-x), & x < 0 \end{cases}$$

$y = f(-x)$ is a reflection of
$y = f(x)$ in the y-axis.
Hence, $y = f(|x|)$ is the following:

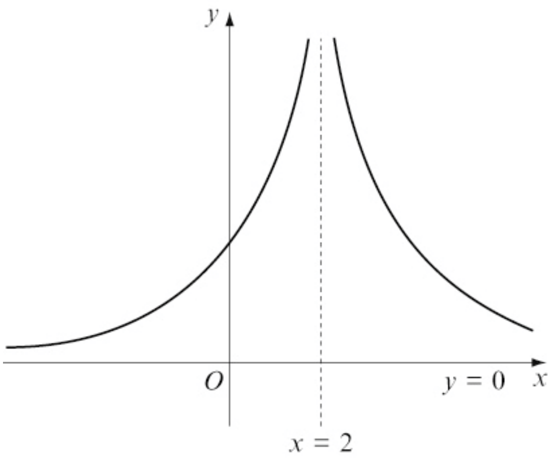
$y = 2f(|x|)$
Vertical stretch, scale factor 2.



© Pearson Education Ltd 2019. Copying permitted for purchasing institution only. This material is not copyright free.

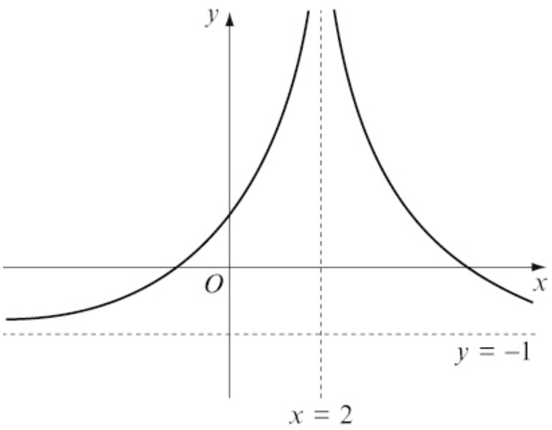
3 a $y = 3\mathrm{f}(x)$

Vertical stretch, scale factor 3.



$y = 3\mathrm{f}(x) - 1$

Vertical translation of -1.

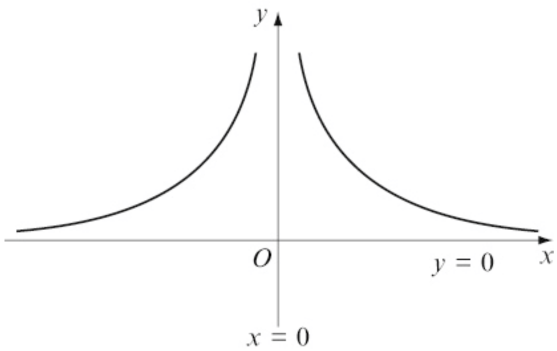


Asymptotes: $x = 2$, $y = -1$

A: (0, 2)

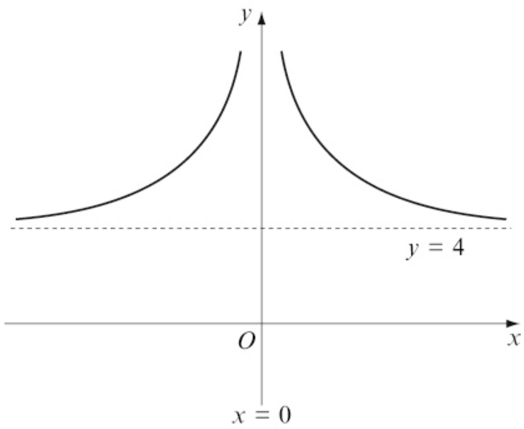
3 b $y = \mathrm{f}(x+2)$

Horizontal translation of -2.



$y = \mathrm{f}(x+2) + 4$

Vertical translation of $+4$.

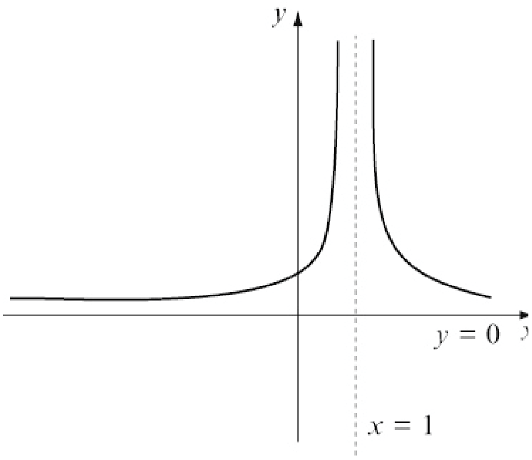


Asymptotes: $x = 0$, $y = 4$

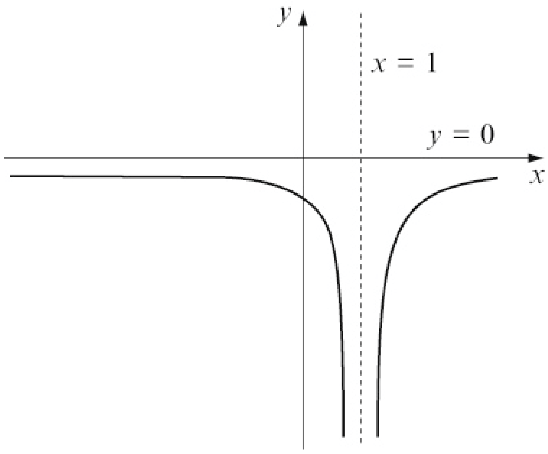
A: (–2, 5)

3 c $y = f(2x)$

Horizontal stretch, scale factor $\frac{1}{2}$



$y = -f(2x)$. Reflection in the x-axis.



Asymptotes: $x = 1$, $y = 0$

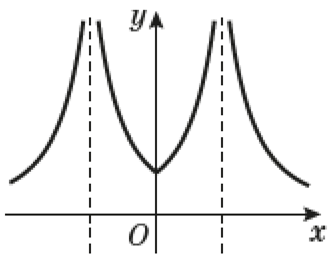
A: (0, –1)

3 d $y = f(|x|)$ can be written

$$y = \begin{cases} f(x), & x \geq 0 \\ f(-x), & x < 0 \end{cases}$$

$y = f(-x)$ is a reflection of $y = f(x)$ in the y-axis.

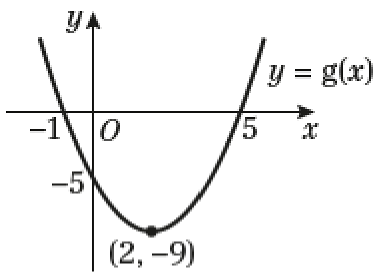
Hence, $y = f(|x|)$ is the following:



Asymptotes are $x = -2$, $x = 2$ and $y = 0$.

A: (0, 1)

4 a



b i $(2 + 4, -9 \times 2) = (6, -18)$

ii $(2 \times \frac{1}{2}, -9) = (1, -9)$

iii $(2, -9 \times -1) = (2, 9)$

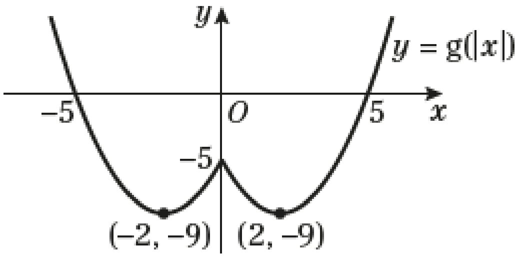
© Pearson Education Ltd 2019. Copying permitted for purchasing institution only. This material is not copyright free.

4 c $y = g(|x|)$ can be written

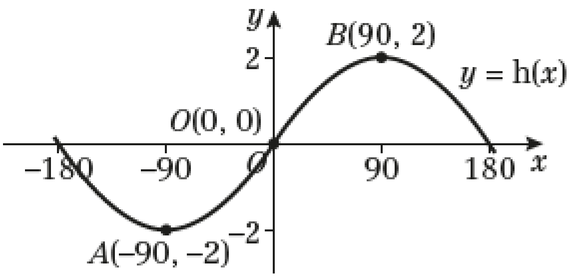
$$y = \begin{cases} g(x) = (x-2)^2 - 9, & x \geq 0 \\ g(-x) = (x+2)^2 - 9, & x < 0 \end{cases}$$

$y = g(-x)$ is a reflection of $y = g(x)$ in the y-axis.

Hence, $y = g(|x|)$ is the following:



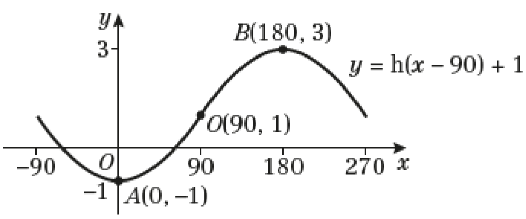
5 a $y = 2\sin x$ is a vertical stretch of $y = \sin x$ by a scale factor 2.



b minimum $A(-90°, -2)$ and maximum $B(90°, 2)$

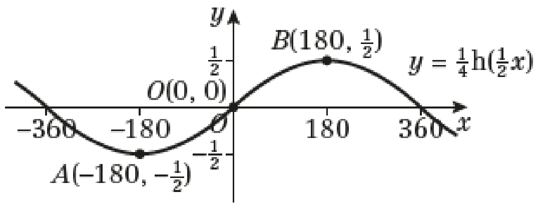
c i $h(x-90)$ is a horizontal translation of $+90°$

$h(x-90)+1$ is a vertical translation of $+1$.



5 c ii $h\left(\frac{1}{2}x\right)$ is a horizontal stretch scale factor 2

$\frac{1}{4}h\left(\frac{1}{2}x\right)$ is a vertical stretch scale factor $\frac{1}{4}$



iii $h(-x)$ is a reflection in the y-axis

$|h(-x)|$ causes the part of the graph below the x-axis to be reflected in the x-axis.

$\frac{1}{2}|h(-x)|$ is a vertical stretch scale factor $\frac{1}{2}$