

OCR

Oxford Cambridge and RSA

Tuesday 21 June 2016 – Morning**A2 GCE MATHEMATICS****4723/01** Core Mathematics 3**QUESTION PAPER**

Candidates answer on the Printed Answer Book.

OCR supplied materials:

- Printed Answer Book 4723/01
- List of Formulae (MF1)

Other materials required:

- Scientific or graphical calculator

Duration: 1 hour 30 minutes**INSTRUCTIONS TO CANDIDATES**

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found inside the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- **Write your answer to each question in the space provided in the Printed Answer Book.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer **all** the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.

INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [] at the end of each question or part question on the Question Paper.
- **You are reminded of the need for clear presentation in your answers.**
- The total number of marks for this paper is **72**.
- The Printed Answer Book consists of **12** pages. The Question Paper consists of **4** pages. Any blank pages are indicated.

INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

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Answer **all** the questions

- 1 Find the equation of the tangent to the curve

$$y = 3x^2(x+2)^6$$

at the point $(-1, 3)$, giving your answer in the form $y = mx + c$. [5]

- 2 Find

(i) $\int \left(2 - \frac{1}{x}\right)^2 dx$,

(ii) $\int (4x+1)^{\frac{1}{3}} dx$.

[5]

- 3 The mass of a substance is decreasing exponentially. Its mass is m grams at time t years. The following table shows certain values of t and m .

t	0	5	10	25
m	200	160		

- (i) Find the values missing from the table. [2]

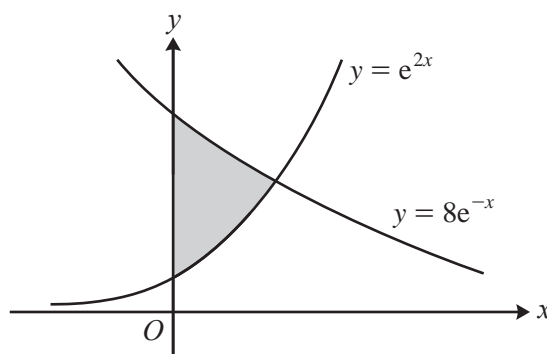
- (ii) Determine the value of t , correct to the nearest integer, for which the mass is 50 grams. [4]

- 4 It is given that A and B are angles such that

$$\sec^2 A - \tan A = 13 \quad \text{and} \quad \sin B \sec^2 B = 27 \cos B \operatorname{cosec}^2 B.$$

Find the possible exact values of $\tan(A - B)$. [8]

- 5



The diagram shows the curves $y = e^{2x}$ and $y = 8e^{-x}$. The shaded region is bounded by the curves and the y -axis. Without using a calculator,

- (i) solve an appropriate equation to show that the curves intersect at a point for which $x = \ln 2$, [2]

- (ii) find the area of the shaded region, giving your answer in simplified form. [5]

- 6 The curves C_1 and C_2 have equations

$$y = \ln(4x - 7) + 18 \quad \text{and} \quad y = a(x^2 + b)^{\frac{1}{2}}$$

respectively, where a and b are positive constants. The point P lies on both curves and has x -coordinate 2. It is given that the gradient of C_1 at P is equal to the gradient of C_2 at P . Find the values of a and b . [8]

- 7 (i) By sketching the curves $y = x(2x + 5)$ and $y = \cos^{-1}x$ (where y is in radians) in a single diagram, show that the equation $x(2x + 5) = \cos^{-1}x$ has exactly one real root. [3]

- (ii) Use the iterative formula

$$x_{n+1} = \frac{\cos^{-1}x_n}{2x_n + 5} \quad \text{with} \quad x_1 = 0.25$$

to find the root correct to 3 significant figures. Show the result of each iteration correct to at least 4 significant figures. [4]

- (iii) Two new curves are obtained by transforming each of the curves $y = x(2x + 5)$ and $y = \cos^{-1}x$ by the pair of transformations:

reflection in the x -axis followed by reflection in the y -axis.

State an equation of each of the new curves and determine the coordinates of their point of intersection, giving each coordinate correct to 3 significant figures. [4]

- 8 The functions f and g are defined for all real values of x by

$$f(x) = |2x + a| + 3a \quad \text{and} \quad g(x) = 5x - 4a,$$

where a is a positive constant.

- (i) State the range of f and the range of g . [2]

- (ii) State why f has no inverse, and find an expression for $g^{-1}(x)$. [3]

- (iii) Solve for x the equation $gf(x) = 31a$. [5]

- 9 (i) Show that $\sin 2\theta(\tan \theta + \cot \theta) \equiv 2$. [4]

- (ii) Hence

(a) find the exact value of $\tan \frac{1}{12}\pi + \tan \frac{1}{8}\pi + \cot \frac{1}{12}\pi + \cot \frac{1}{8}\pi$, [3]

(b) solve the equation $\sin 4\theta(\tan \theta + \cot \theta) = 1$ for $0 < \theta < \frac{1}{2}\pi$, [3]

(c) express $(1 - \cos 2\theta)^2 \left(\tan \frac{1}{2}\theta + \cot \frac{1}{2}\theta\right)^3$ in terms of $\sin \theta$. [2]

END OF QUESTION PAPER

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