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2. (a) Differentiate with respect to  $x$

(i)  $3 \sin^2x + \sec 2x,$

(3)

(ii)  $\{x + \ln(2x)\}^3.$

(3)

Given that  $y = \frac{5x^2 - 10x + 9}{(x - 1)^2}, \quad x \neq 1,$

(b) show that  $\frac{dy}{dx} = -\frac{8}{(x - 1)^3}.$

(6)

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3. The function  $f$  is defined by

$$f: x \rightarrow \frac{5x+1}{x^2+x-2} - \frac{3}{x+2}, \quad x > 1.$$

(a) Show that  $f(x) = \frac{2}{x-1}$ ,  $x > 1$ . (4)

(b) Find  $f^{-1}(x)$ . (3)

The function  $g$  is defined by

$$g: x \rightarrow x^2 + 5, \quad x \in \mathbb{R}.$$

(c) Solve  $fg(x) = \frac{1}{4}$ . (3)

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4. 
$$f(x) = 3e^x - \frac{1}{2} \ln x - 2, \quad x > 0.$$

- (a) Differentiate to find  $f'(x)$ . (3)

The curve with equation  $y = f(x)$  has a turning point at  $P$ . The  $x$ -coordinate of  $P$  is  $\alpha$ .

- (b) Show that  $\alpha = \frac{1}{6} e^{-\alpha}$ . (2)

The iterative formula

$$x_{n+1} = \frac{1}{6} e^{-x_n}, \quad x_0 = 1,$$

is used to find an approximate value for  $\alpha$ .

- (c) Calculate the values of  $x_1, x_2, x_3$  and  $x_4$ , giving your answers to 4 decimal places. (2)

- (d) By considering the change of sign of  $f'(x)$  in a suitable interval, prove that  $\alpha = 0.1443$  correct to 4 decimal places. (2)

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Figure 1

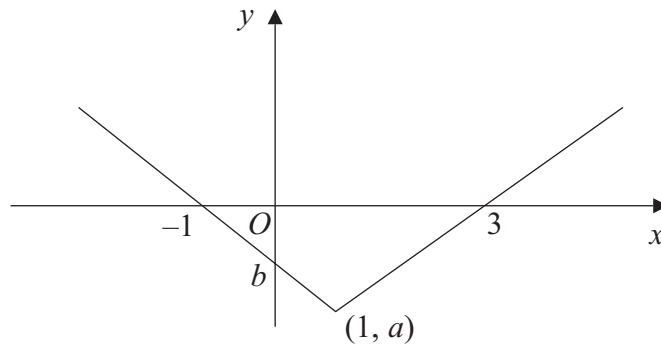


Figure 1 shows part of the graph of  $y = f(x)$ ,  $x \in \mathbb{R}$ . The graph consists of two line segments that meet at the point  $(1, a)$ ,  $a < 0$ . One line meets the  $x$ -axis at  $(3, 0)$ . The other line meets the  $x$ -axis at  $(-1, 0)$  and the  $y$ -axis at  $(0, b)$ ,  $b < 0$ .

In separate diagrams, sketch the graph with equation

(a)  $y = f(x + 1)$ , (2)

(b)  $y = f(|x|)$ . (3)

Indicate clearly on each sketch the coordinates of any points of intersection with the axes.

Given that  $f(x) = |x - 1| - 2$ , find

(c) the value of  $a$  and the value of  $b$ , (2)

(d) the value of  $x$  for which  $f(x) = 5x$ . (4)









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**Question 7 continued**

Lined area for writing answers.

Q7

(Total 10 marks)

**TOTAL FOR PAPER: 75 MARKS**

**END**

