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1. Given that

$$\frac{2x^4 - 3x^2 + x + 1}{(x^2 - 1)} \equiv (ax^2 + bx + c) + \frac{dx + e}{(x^2 - 1)},$$

find the values of the constants  $a, b, c, d$  and  $e$ .

(4)

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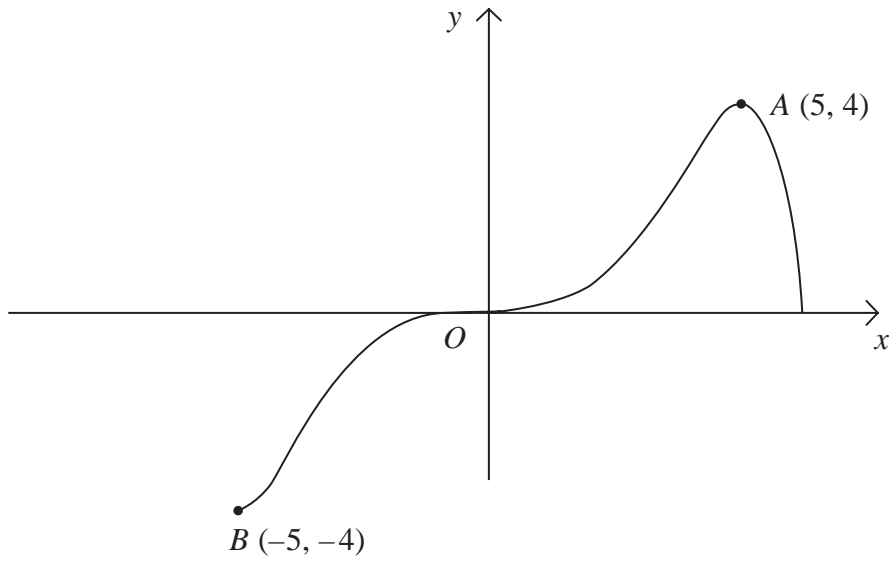






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4.



**Figure 1**

Figure 1 shows a sketch of the curve with equation  $y = f(x)$ .  
The curve passes through the origin  $O$  and the points  $A(5, 4)$  and  $B(-5, -4)$ .

In separate diagrams, sketch the graph with equation

(a)  $y = |f(x)|$ , (3)

(b)  $y = f(|x|)$ , (3)

(c)  $y = 2f(x+1)$ . (4)

On each sketch, show the coordinates of the points corresponding to  $A$  and  $B$ .



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**Question 4 continued**



H 2 6 3 1 5 R B 0 9 2 4

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5. The radioactive decay of a substance is given by

$$R = 1000e^{-ct}, \quad t \geq 0.$$

where  $R$  is the number of atoms at time  $t$  years and  $c$  is a positive constant.

- (a) Find the number of atoms when the substance started to decay. (1)

It takes 5730 years for half of the substance to decay.

- (b) Find the value of  $c$  to 3 significant figures. (4)
- (c) Calculate the number of atoms that will be left when  $t = 22\,920$  . (2)
- (d) In the space provided on page 13, sketch the graph of  $R$  against  $t$  . (2)

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6. (a) Use the double angle formulae and the identity

$$\cos(A + B) \equiv \cos A \cos B - \sin A \sin B$$

to obtain an expression for  $\cos 3x$  in terms of powers of  $\cos x$  only.

(4)

(b) (i) Prove that

$$\frac{\cos x}{1 + \sin x} + \frac{1 + \sin x}{\cos x} \equiv 2 \sec x, \quad x \neq (2n + 1) \frac{\pi}{2}.$$

(4)

(ii) Hence find, for  $0 < x < 2\pi$ , all the solutions of

$$\frac{\cos x}{1 + \sin x} + \frac{1 + \sin x}{\cos x} = 4.$$

(3)

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7. A curve  $C$  has equation

$$y = 3 \sin 2x + 4 \cos 2x, \quad -\pi \leq x \leq \pi.$$

The point  $A(0, 4)$  lies on  $C$ .

(a) Find an equation of the normal to the curve  $C$  at  $A$ . (5)

(b) Express  $y$  in the form  $R \sin(2x + \alpha)$ , where  $R > 0$  and  $0 < \alpha < \frac{\pi}{2}$ .  
Give the value of  $\alpha$  to 3 significant figures. (4)

(c) Find the coordinates of the points of intersection of the curve  $C$  with the  $x$ -axis.  
Give your answers to 2 decimal places. (4)

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8. The functions  $f$  and  $g$  are defined by

$$f : x \mapsto 1 - 2x^3, \quad x \in \mathbb{R}$$

$$g : x \mapsto \frac{3}{x} - 4, \quad x > 0, \quad x \in \mathbb{R}$$

(a) Find the inverse function  $f^{-1}$ . (2)

(b) Show that the composite function  $gf$  is

$$gf : x \mapsto \frac{8x^3 - 1}{1 - 2x^3}.$$

(4)

(c) Solve  $gf(x) = 0$ . (2)

(d) Use calculus to find the coordinates of the stationary point on the graph of  $y = gf(x)$ . (5)

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**Question 8 continued**

(Area for handwritten answers to Question 8)

**Q8**

**(Total 13 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**

