

1		$a + (10 - 1)d = 11.1$ and $a + (50 - 1)d = 7.1$ $d = -0.1$ $a = 12$ $\frac{1}{2} \times 50(\text{their } a + 7.1)$ with $a > 11.1$ 477.5 or $477\frac{1}{2}$ or $\frac{955}{2}$ cao	M1 A1 A1 M1 A1 [5]	may be implied by $40d = \pm 4$ or embedded in attempt to solve if unsupported, B2 for one of these and B3 for both or $\frac{50}{2}(2a + (50 - 1)d)$ with $a > 11.1$ and $d < 0$	condone one slip in coefficient of d if M0, B2 for any form of correct answer www
2	(i)	3×3^7 oe 6561	M1 A1 [2]	condone 1×3^7 or B2 if unsupported	do not award if only seen in sum of terms of GP if 0, SC1 for 2187 unsupported
2	(ii)	valid attempt to sum a GP with $r = 3$ and $n = 15$ $\frac{3(3^{15} - 1)}{3 - 1}$ oe 21 523 359	M1 M1 A1 [3]	eg $3 + 3^2 + \dots + 3^{15}$ or B2 if M1M0 or B3 if unsupported	must see at least first two terms and last term NB 7 174 453 implies M1 from $1 + 3 + \dots + 3^{14}$

2	(iii)	$\frac{3(3^n - 1)}{3 - 1} > 1000000$ <p>oe</p> $\text{eg } 3^{n+1} > 2000003 \text{ or } 3^n > \frac{2000000}{3} + 1$ <p>www</p> <p>correctly taking logs of both sides</p> $\text{eg } (n + 1) \log 3 > \log 2000003 \text{ or } n \log 3 > \log 2000003 - \log 3$ $\text{eg } n + 1 > \frac{\log 2000003}{\log 3} \text{ and completion to } n > \frac{\log 2000003}{\log 3} - 1$ <p>$n = 13$ seen</p>	<p>M1*</p> <p>M1dep*</p> <p>A1</p> <p>B1</p> <p>[4]</p>	<p>eg $\log 3^{n+1} > \log 2000003$ www or $\log 3^n + \log 3 > \log 2000003$ www; may be implied by next stage of working</p> <p>without any wrong working</p> <p>B0 for $n \geq 13$ or $n > 13$</p>	<p>M0 for working backwards</p> <p>M0 if = or < used</p> <p>at least one previous progressive interim step needed with no wrong working; M0dep* for $\log(3^n - 1) > \dots$</p> <p>do not allow recovery from bracket errors at any stage</p>
2	(iv)	<p>valid attempt to sum a GP with $r = 2$ and $n = 15$</p> <p>their 21 523 359 – their 65 534 21 457 825 isw</p>	<p>M1*</p> <p>M1dep*</p> <p>A1</p> <p>[3]</p>	<p>if correct eg $2 + 2^2 + \dots + 2^{15} = 65\,534$</p> <p>with their $65\,534 <$ their $21\,523\,359$</p> <p>allow B3 for 21 457 825 unsupported</p>	<p>NB 32767 implies M1 from $1 + 2 + \dots + 2^{14}$</p>

3	(i)	$21 \left(\frac{1}{1+2} + \frac{1}{2+2} + \frac{1}{3+2} + \frac{1}{4+2} + \frac{1}{5+2} \right)$ oe soi 22.95 or $\frac{459}{20}$ or $22\frac{19}{20}$	M1 A1 [2]	may be implied by correct answer	NB $7 + 5.25 + 4.2 + 3.5 + 3$ M0 if extra terms or terms missing
3	(ii)	$a + 45$ cao $\frac{10}{2} a + a + their45$ $5(2a + 45)$ or $10a + 225$ cao isw	B1 M1 A1 [3]	mark the final answer must be explicitly stated or $\frac{10}{2} 2a + (10 - 1) \times 5$ ignore further work attempting to find a	condone wrongly attributed answers B2 if correct answer derived from adding terms separately

4		$ar = 24$ (i) $\frac{a}{1-r} = 150$ (ii) correct substitution to eliminate one unknown $r = 0.8$ or 0.2 $a = 30$ or $a = 120$	B1* B1* M1dep* A1 A1 [5]	eg subst. of $a = 150(1 - r)$ or $r = \frac{150 - a}{150}$ in (i) alternatively, subst. of $a = \frac{24}{r}$ or $r = \frac{24}{a}$ in (ii) or A1 for each correct pair of values ignore incorrect pairing if correct values already correctly attributed	allow $ar^{2-1} = 24$ if M0, B1 for both values of r and B1 for both values of a , or B1 for each pair of correct values NB $150r^2 - 150r + 24 [= 0]$ $a^2 - 150a + 3600 [= 0]$ A0 if wrongly attributed A0 if wrongly attributed
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Question		Answer	Marks	Guidance	
5	(i)	$2S$ cao	B1 [1]		
5	(ii)	$\frac{a}{1-r^2}$ $\frac{S}{1+r}$ or $\frac{1}{1+r}S$	M1 A1 [2]	if M0, SC1 for $\frac{1-r}{1-r^2} \times S$ oe	

6		(5), 8, 11, (14),...isw $a = 5$ and $d = 3$ soi $S_{50} = \frac{50}{2}(2 \times 5 + (50 - 1) \times 3)$ oe 3925	B1 B1 M1 A1 [4]	if M0, SC1 for use of $a = 8$ and obtaining 4075	if M0, award B2 if 3925 is obtained from summing individual terms or if unsupported
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Question		Answer	Marks	Guidance	
7	(i)	$ar = 6$ oe $\frac{a}{1-r} = 25$ oe $25 = \frac{a}{1-\frac{6}{a}}$ $a^2 - 25a + 150 [= 0]$ $a = 10$ obtained from formula, factorising, Factor theorem or completing the square $a = 15$ $r = 0.4$ and 0.6	B1 B1 M1 A1 A1 A1 A1 [7]	must be in a and r must be in a and r or $\frac{6}{r} = 25(1-r)$ or $25r^2 - 25r + 6 [= 0]$ $r = 0.4$ and $r = 0.6$ $a = 15$ $a = \frac{6}{0.6} = 10$ oe	NB assuming $a = 10$ earns M0 All signs may be reversed if M0, B1 for $r = 0.4$ and 0.6 and B1 for $a = 15$ by trial and improvement mark to benefit of candidate
7	(ii)	$10 \times (3/5)^{n-1}$ and $15 \times (2/5)^{n-1}$ seen $15 \times 2^{n-1} : 10 \times 3^{n-1}$ or $3 \times \frac{2^{n-1}}{5^{n-1}} : 2 \times \frac{3^{n-1}}{5^{n-1}}$ $3 \times 2^{n-1} : 2 \times 3^{n-1}$	M1 M1 A1 [3]	 may be implied by $3 \times 2^{n-1} : 2 \times 3^{n-1}$ and completion to given answer www	condone ratio reversed condone ratio reversed