

1 Find $\int (3x^5 + 2x^{-\frac{1}{2}}) dx$. [4]

2

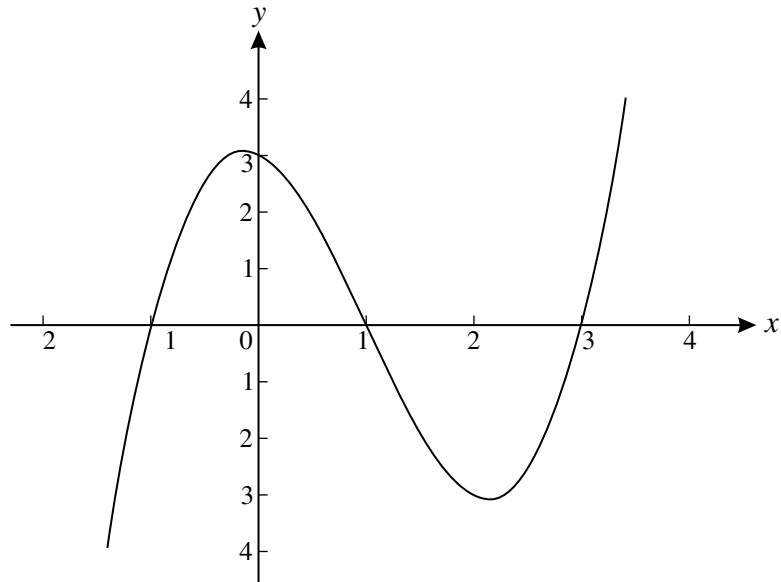


Fig. 11

Fig. 11 shows the curve $y = x^3 - 3x^2 - x + 3$.

(i) Use calculus to find $\int_1^3 (x^3 - 3x^2 - x + 3) dx$ and state what this represents. [6]

(ii) Find the x -coordinates of the turning points of the curve $y = x^3 - 3x^2 - x + 3$, giving your answers in surd form. Hence state the set of values of x for which $y = x^3 - 3x^2 - x + 3$ is a decreasing function. [5]

3 Find $\int \left(x - \frac{3}{x^2}\right) dx$. [3]

4 Find $\int (20x^4 + 6x^{-\frac{3}{2}}) dx$. [4]

5 Find $\int (12x^5 + \sqrt[3]{x} + 7) dx$. [5]

6 Find $\int \left(x^{\frac{1}{2}} + \frac{6}{x^3} \right) dx$. [5]

7 Find $\int \left(x^3 + \frac{1}{x^3} \right) dx$. [4]

8 (i) Differentiate $12 \sqrt[3]{x}$. [2]

(ii) Integrate $\frac{6}{x^3}$. [3]