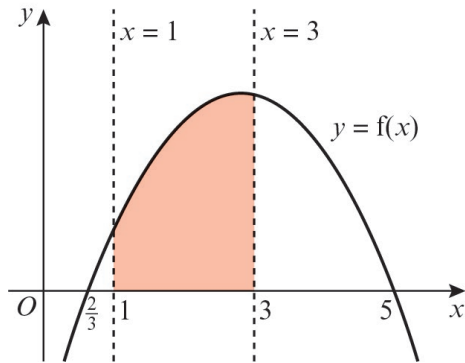


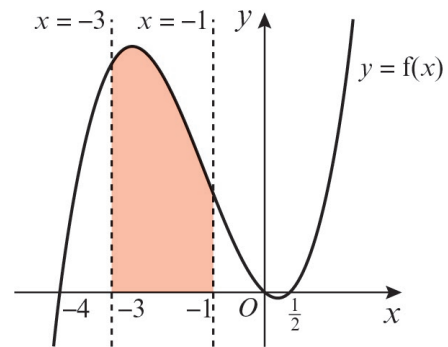
## Exercise 8B

$$\begin{aligned}
 \mathbf{1 \ a} \quad & -3x^2 + 17x - 10 = 0 \\
 & (-3x + 2)(x - 5) = 0 \\
 & x = \frac{2}{3} \text{ or } x = 5
 \end{aligned}$$



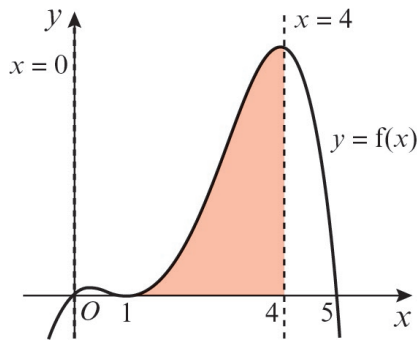
$$\begin{aligned}
 & \int_1^3 (-3x^2 + 17x - 10) \, dx \\
 &= \left[ \frac{-3x^3}{3} + \frac{17x^2}{2} - 10x \right]_1^3 \\
 &= \left[ -x^3 + \frac{17x^2}{2} - 10x \right]_1^3 \\
 &= \left( -3^3 + \frac{17(3)^2}{2} - 10(3) \right) \\
 &\quad - \left( -1^3 + \frac{17(1)^2}{2} - 10(1) \right) \\
 &= \left( -27 + \frac{153}{2} - 30 \right) - \left( -1 + \frac{17}{2} - 10 \right) \\
 &= 22
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{b} \quad & 2x^3 + 7x^2 - 4x = 0 \\
 & x(2x^2 + 7x - 4) = 0 \\
 & x(2x - 1)(x + 4) = 0 \\
 & x = 0, x = \frac{1}{2} \text{ or } x = -4
 \end{aligned}$$



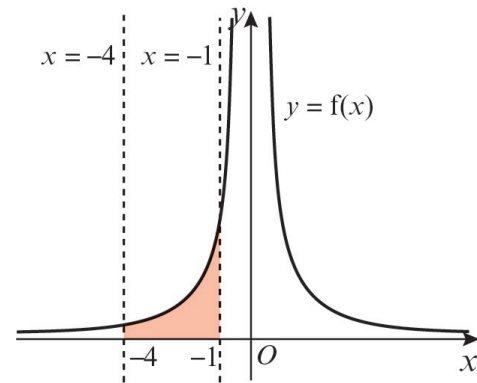
$$\begin{aligned}
 & \int_{-3}^{-1} (2x^3 + 7x^2 - 4x) \, dx \\
 &= \left[ \frac{2x^4}{4} + \frac{7x^3}{3} - \frac{4x^2}{2} \right]_{-3}^{-1} \\
 &= \left( \frac{(-1)^4}{2} + \frac{7(-1)^3}{3} - 2(-1)^2 \right) \\
 &\quad - \left( \frac{(-3)^4}{2} + \frac{7(-3)^3}{3} - 2(-3)^2 \right) \\
 &= \left( \frac{1}{2} - \frac{7}{3} - 2 \right) - \left( \frac{81}{2} - \frac{189}{3} - 18 \right) \\
 &= 36\frac{2}{3}
 \end{aligned}$$

$$\begin{aligned}
 1 \text{ c } \quad & -x^4 + 7x^3 - 11x^2 + 5x = 0 \\
 & -x(x-1)^2(x-5) = 0 \\
 & x = 0, x = 1 \text{ or } x = 5
 \end{aligned}$$



$$\begin{aligned}
 & \int_0^4 (-x^4 + 7x^3 - 11x^2 + 5x) \, dx \\
 &= \left[ -\frac{x^5}{5} + \frac{7x^4}{4} - \frac{11x^3}{3} + \frac{5x^2}{2} \right]_0^4 \\
 &= \left( -\frac{4^5}{5} + \frac{7(4)^4}{4} - \frac{11(4)^3}{3} + \frac{5(4)^2}{2} \right) \\
 &\quad - \left( -\frac{0^5}{5} + \frac{7(0)^4}{4} - \frac{11(0)^3}{3} + \frac{5(0)^2}{2} \right) \\
 &= \left( -\frac{1024}{5} + 448 - \frac{704}{3} + 40 \right) \\
 &= 48\frac{8}{15}
 \end{aligned}$$

1 d

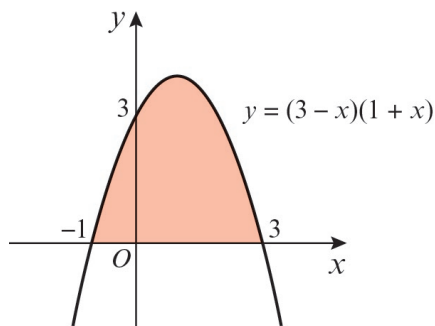


$$\begin{aligned}
 \int_{-4}^{-1} \left( \frac{8}{x^2} \right) \, dx &= \int_{-4}^{-1} (8x^{-2}) \, dx \\
 &= \left[ \frac{8x^{-1}}{-1} \right]_{-4}^{-1} \\
 &= \left[ -\frac{8}{x} \right]_{-4}^{-1} \\
 &= \left( -\frac{8}{(-1)} \right) - \left( -\frac{8}{(-4)} \right) \\
 &= (8) - (2) \\
 &= 6
 \end{aligned}$$

$$\begin{aligned}
 2 \quad A &= \int_{-2}^0 x(x^2 - 4) \, dx = \int_{-2}^0 (x^3 - 4x) \, dx \\
 &= \left( \frac{x^4}{4} - \frac{4x^2}{2} \right)_{-2}^0 \\
 &= \left( \frac{x^4}{4} - 2x^2 \right)_{-2}^0 \\
 &= (0) - \left( \frac{16}{4} - 2 \times 4 \right) \\
 &= -4 + 8 \\
 &= 4
 \end{aligned}$$

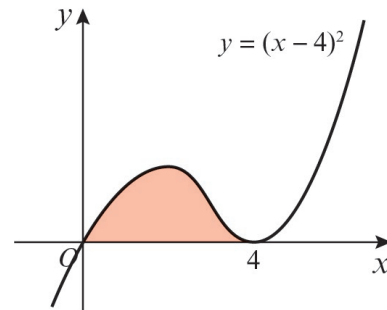
$$\begin{aligned}
 3 \quad A &= \int_1^3 \left( 3x + \frac{6}{x^2} - 5 \right) dx \\
 &= \int_1^3 (3x + 6x^{-2} - 5) dx \\
 &= \left( \frac{3x^2}{2} + \frac{6x^{-1}}{-1} - 5x \right) \Big|_1^3 \\
 &= \left( \frac{3}{2}x^2 - 6x^{-1} - 5x \right) \Big|_1^3 \\
 A &= \left( \frac{3}{2} \times 9 - \frac{6}{3} - 15 \right) - \left( \frac{3}{2} - 6 - 5 \right) \\
 &= \frac{27}{2} - 17 - \frac{3}{2} + 11 \\
 &= \frac{24}{2} - 6 \\
 &= 6
 \end{aligned}$$

$$\begin{aligned}
 4 \quad y &= (3-x)(1+x) \text{ is } \wedge \text{ shaped} \\
 y = 0 &\Rightarrow x = 3, -1 \\
 x = 0 &\Rightarrow y = 3
 \end{aligned}$$



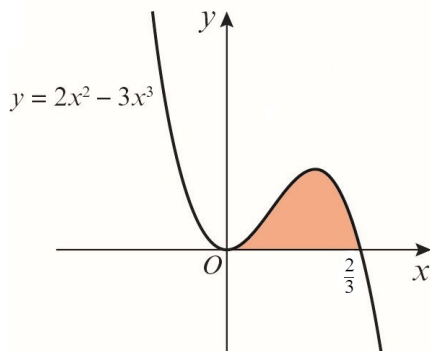
$$\begin{aligned}
 A &= \int_{-1}^3 (3-x)(1+x) dx \\
 &= \int_{-1}^3 (3+2x-x^2) dx \\
 &= \left( 3x + x^2 - \frac{x^3}{3} \right) \Big|_{-1}^3 \\
 &= \left( 9+9-\frac{27}{3} \right) - \left( -3+1+\frac{1}{3} \right) \\
 &= 9+1\frac{2}{3} \\
 &= 10\frac{2}{3}
 \end{aligned}$$

$$\begin{aligned}
 5 \quad y &= x(x-4)^2 \\
 y = 0 &\Rightarrow x = 0, 4 \text{ (twice)} \\
 &\text{There is a turning point at } (4, 0).
 \end{aligned}$$



$$\begin{aligned}
 \text{Area} &= \int_0^4 x(x-4)^2 dx \\
 &= \int_0^4 x(x^2 - 8x + 16) dx \\
 &= \int_0^4 (x^3 - 8x^2 + 16x) dx \\
 &= \left( \frac{x^4}{4} - \frac{8x^3}{3} + 8x^2 \right) \Big|_0^4 \\
 &= \left( 64 - \frac{8}{3} \times 64 + 128 \right) - (0) \\
 &= \frac{64}{3} \text{ or } 21\frac{1}{3}
 \end{aligned}$$

$$\begin{aligned}
 6 \quad & 2x^2 - 3x^3 = 0 \\
 & x^2(2 - 3x) = 0 \\
 & x = 0 \text{ or } x = \frac{2}{3}
 \end{aligned}$$



$$\begin{aligned}
 \int_0^{\frac{2}{3}} (2x^2 - 3x^3) \, dx &= \left[ \frac{2x^3}{3} - \frac{3x^4}{4} \right]_0^{\frac{2}{3}} \\
 &= \left( \frac{2\left(\frac{2}{3}\right)^3}{3} - \frac{3\left(\frac{2}{3}\right)^4}{4} \right) \\
 &\quad - \left( \frac{2(0)^3}{3} - \frac{3 \times 0^4}{4} \right) \\
 &= \frac{16}{81} - \frac{12}{81} \\
 &= \frac{4}{81}
 \end{aligned}$$

$$\begin{aligned}
 7 \quad & \int_0^k (3x^2 - 2x + 2) \, dx = 8 \\
 & \left[ \frac{3x^3}{3} - \frac{2x^2}{2} + 2x \right]_0^k = 8 \\
 & [x^3 - x^2 + 2x]_0^k = 8 \\
 & (k^3 - k^2 + 2k) - (0^3 - 0^2 + 2(0)) = 8 \\
 & k^3 - k^2 + 2k - 8 = 0
 \end{aligned}$$

Using the factor theorem,  $k = 2$  as  
 $2^3 - 2^2 + 2(2) - 8 = 0$

Therefore,  $k = 2$

$$\begin{aligned}
 8 \quad \mathbf{a} \quad & -x^2 + 2x + 3 = 0 \\
 & (-x + 3)(x + 1) = 0 \\
 & x = 3 \text{ or } x = -1 \\
 & A(-1, 0) \text{ and } B(3, 0)
 \end{aligned}$$

$$8 \quad \mathbf{b} \quad \int_{-1}^3 (-x^2 + 2x + 3) \, dx$$

$$\begin{aligned}
 &= \left[ -\frac{x^3}{3} + \frac{2x^2}{2} + 3x \right]_{-1}^3 \\
 &= \left[ -\frac{x^3}{3} + x^2 + 3x \right]_{-1}^3 \\
 &= \left( -\frac{3^3}{3} + 3^2 + 3(3) \right) - \left( -\frac{(-1)^3}{3} + (-1)^2 + 3(-1) \right) \\
 &= (-9 + 9 + 9) - \left( \frac{1}{3} + 1 - 3 \right) \\
 &= 10\frac{2}{3}
 \end{aligned}$$

$$\begin{aligned}
 9 \quad & \int_0^2 x^2(2-x) \, dx = \int_0^2 2x^2 - x^3 \, dx \\
 &= \left[ \frac{2x^3}{3} - \frac{x^4}{4} \right]_0^2 \\
 &= \left( \frac{2(2)^3}{3} - \frac{2^4}{4} \right) - \left( \frac{2(0)^3}{3} - \frac{0^4}{4} \right) \\
 &= \left( \frac{16}{3} - \frac{16}{4} \right) \\
 &= 1\frac{1}{3}
 \end{aligned}$$