

# Core Mathematics C2 Paper C

1. Giving your answers in terms of  $\pi$ , solve the equation

$$3 \tan^2 \theta - 1 = 0,$$

for  $\theta$  in the interval  $-\pi \leq \theta \leq \pi$ . [5]

2. Given that  $p = \log_2 3$  and  $q = \log_2 5$ , find expressions in terms of  $p$  and  $q$  for

(i)  $\log_2 45$ , [3]

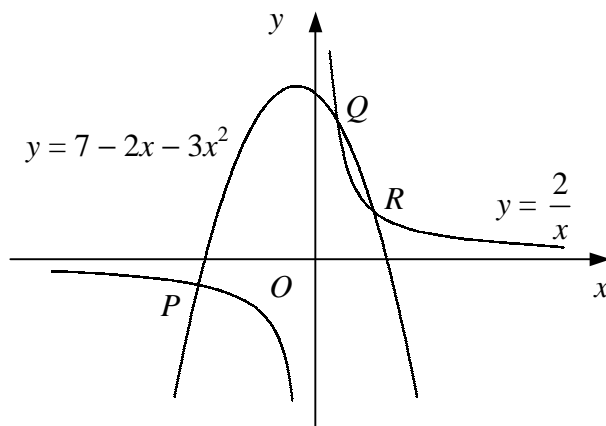
(ii)  $\log_2 0.3$  [3]

3. For the binomial expansion in ascending powers of  $x$  of  $(1 + \frac{1}{4}x)^n$ , where  $n$  is an integer and  $n \geq 2$ ,

(i) find and simplify the first three terms, [3]

(ii) find the value of  $n$  for which the coefficient of  $x$  is equal to the coefficient of  $x^2$ . [3]

- 4.



The diagram shows the curves with equations  $y = 7 - 2x - 3x^2$  and  $y = \frac{2}{x}$ .

The two curves intersect at the points  $P$ ,  $Q$  and  $R$ .

- (i) Show that the  $x$ -coordinates of  $P$ ,  $Q$  and  $R$  satisfy the equation

$$3x^3 + 2x^2 - 7x + 2 = 0. [2]$$

Given that  $P$  has coordinates  $(-2, -1)$ ,

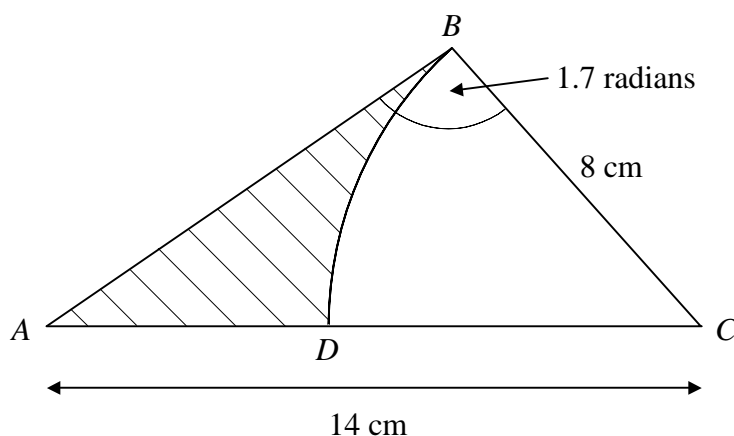
- (ii) find the coordinates of  $Q$  and  $R$ . [6]

5. The curve  $y = f(x)$  passes through the point  $P(-1, 3)$  and is such that

$$\frac{dy}{dx} = -\frac{4}{x^3}, \quad x \neq 0.$$

- (i) Find  $f(x)$ . [4]
- (ii) Show that the area of the finite region bounded by the curve  $y = f(x)$ , the  $x$ -axis and the lines  $x = 1$  and  $x = 4$  is  $4\frac{1}{2}$ . [4]

6.



The diagram shows triangle  $ABC$  in which  $AC = 14$  cm,  $BC = 8$  cm and  $\angle ABC = 1.7$  radians.

- (i) Find the size of  $\angle ACB$  in radians. [4]

The point  $D$  lies on  $AC$  such that  $BD$  is an arc of a circle, centre  $C$ .

- (ii) Find the perimeter of the shaded region bounded by the arc  $BD$  and the straight lines  $AB$  and  $AD$ . [4]

7. (a) Given that  $y = 3^x$ , find expressions in terms of  $y$  for

(i)  $3^{x+1}$ , [2]

(ii)  $3^{2x-1}$ . [2]

- (b) Hence, or otherwise, solve the equation

$$3^{x+1} - 3^{2x-1} = 6. \quad [5]$$

**Turn over**

8. (i) Given that

$$\int_1^3 (x^2 - 2x + k) \, dx = 8\frac{2}{3},$$

find the value of the constant  $k$ . [6]

- (ii) Evaluate

$$\int_2^{\infty} \frac{6}{x^{\frac{5}{2}}} \, dx,$$

giving your answer in its simplest form. [5]

9. The second and fifth terms of a geometric series are  $-48$  and  $6$  respectively.

(i) Find the first term and the common ratio of the series. [4]

(ii) Find the sum to infinity of the series. [2]

(iii) Show that the difference between the sum of the first  $n$  terms of the series and its sum to infinity is given by  $2^{6-n}$ . [5]