

**Mathematics**

Advanced Subsidiary GCE

Unit **4722**: Core Mathematics 2

**Mark Scheme for January 2012**

---

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, OCR Nationals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

© OCR 2012

Any enquiries about publications should be addressed to:

OCR Publications  
PO Box 5050  
Annesley  
NOTTINGHAM  
NG15 0DL

Telephone: 0870 770 6622  
Facsimile: 01223 552610  
E-mail: [publications@ocr.org.uk](mailto:publications@ocr.org.uk)

## Annotations

Annotation in scoris	Meaning
✓ and ✖	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	

Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

## Subject-specific Marking Instructions

- a Annotations should be used whenever appropriate during your marking.

**The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.** It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c The following types of marks are available.

### **M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

### **A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

### **B**

Mark for a correct result or statement independent of Method marks.

## E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep \*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

- g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

- h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

Question		Answer	Marks	Guidance
1	(i)	$\text{perimeter} = (4.2 \times 12) + (2 \times 12)$ $= 74.4 \text{ cm}$	<p><b>M1*</b></p> <p>Use <math>s = 12\theta</math></p> <p><b>M1d*</b></p> <p>Attempt perimeter of sector</p> <p><b>A1</b></p> <p>Obtain 74.4</p> <p>[3]</p>	<p>Allow equiv method using fractions of a circle</p> <p>If working in degrees, must use 180 and <math>\pi</math> (or 360 and <math>2\pi</math>) to find angle</p> <p>M0 if <math>12\theta</math> used with <math>\theta</math> in degrees</p> <p>M0 if <math>4.2\pi</math> used instead of 4.2</p> <p>M1 if attempting arc of minor sector (<math>12 \times 2.1</math> (or better))</p> <p>Add 24 to their attempt at <math>12\theta</math></p> <p>M0 if using minor sector</p> <p>Units not required</p> <p>Allow a more accurate answer that rounds to 74.4, with no errors seen (poss resulting from working in degrees)</p>
1	(ii)	$\text{area} = \frac{1}{2} \times 12^2 \times 4.2$ $= 302.45 \text{ cm}^2$	<p><b>M1</b></p> <p>Use <math>A = (\frac{1}{2})12^2 \theta</math></p> <p><b>A1</b></p> <p>Obtain 302, or better</p> <p>[2]</p>	<p>Condone omission of <math>\frac{1}{2}</math>, but no other error</p> <p>Allow equiv method using fractions of a circle</p> <p>M0 if <math>(\frac{1}{2})12^2 \theta</math> used with <math>\theta</math> in degrees</p> <p>M0 if <math>4.2\pi</math> used instead of 4.2</p> <p>M1 if attempting area of minor sector</p> <p>Units not required</p> <p>Allow 302 or a more accurate answer that rounds to 302.4, with no errors seen (could be slight inaccuracy if using fractions of a circle)</p>

Question		Answer	Marks	Guidance
2	(i)	$0.5 \times 1.5 \times \{\lg 9 + 2(\lg 12 + \lg 15 + \lg 18) + \lg 21\}$ $= 6.97$	<p><b>B1</b> State, or use, y-values of lg9, lg12, lg15, lg18 and lg21</p> <p><b>M1</b> Attempt correct trapezium rule, any <math>h</math>, to find area between <math>x = 4</math> and <math>x = 10</math></p> <p><b>M1</b> Use correct <math>h</math> in recognisable attempt at trap rule</p> <p><b>A1</b> Obtain 6.97, or better</p> <p><b>[4]</b></p>	<p>B0 if other y-values also found (unless not used in trap rule) Allow decimal equivs (0.95, 1.08, 1.18, 1.26, 1.32 or better)</p> <p>Correct structure required, including correct placing of y-values The ‘big brackets’ must be seen, or implied by later working Could be implied by stating general rule in terms of <math>y_0</math> etc, as long as these have been attempted elsewhere and clearly labelled Could use other than 4 strips as long as of equal width Using <math>x</math>-values is M0 Can give M1, even if error in <math>y</math>-values eg using 9, 12, 15, 18, 21 or using now incorrect function eg <math>\log(2x) + 1</math> Allow BoD if first or last <math>y</math>-value incorrect, unless clearly from an incorrect <math>x</math>-value (eg <math>y_0 = \lg 7</math>, but <math>x = 4</math> not seen)</p> <p>Must be in attempt at trap rule, not Simpson’s rule Allow if muddle over placing <math>y</math>-values (but M0 for <math>x</math>-values) Allow if <math>\frac{1}{2}</math> missing Allow other than 4 strips, as long as <math>h</math> is consistent Allow slips which result in <math>x</math>-values not equally spaced</p> <p>Allow answers in the range [6.970, 6.975] if &gt;3sf</p> <p>Answer only is 0/4 Using the trap rule on result of an integration attempt is 0/4 Using 4 separate trapezia can get full marks – if other than 4 trapezia then mark as above However, using only one trapezium is 0/4</p>



Question		Answer	Marks	Guidance
2	(ii)	tops of trapezia are below curve	<b>B1</b>  <b>[1]</b>	<p>Convincing reason referring to the top of a trapezium being below the curve, or the gap between a trapezium and the curve – explanation must be sufficient and fully correct</p> <p>B0 for ‘the trapezium is below the curve’ (ie ‘top’ not used)  Sketch with explanation is fine, even if just arrow and ‘gap’  Sketching rectangles / triangles is B0, as is a trapezium that doesn’t have both top vertices intended to be on curve  Concave / convex is B0, as is comparing to exact area  B1 for reference to decreasing gradient</p>
3	(i)	$20 \times 4^3 \times a^3 = 160$ $1280a^3 = 160$ $a^3 = \frac{1}{8}$ $a = \frac{1}{2}$	<p><b>M1</b>  <b>A1</b>  <b>M1</b>  <b>A1</b>  <b>[4]</b></p>	<p>Attempt relevant term</p> <p>Obtain correct <math>1280a^3</math>, or unsimplified equiv</p> <p>Equate to 160 and attempt to solve for <math>a</math></p> <p>Obtain <math>a = \frac{1}{2}</math></p> <p>Must be an attempt at a product involving a binomial coeff of 20 (not just <math>{}^6C_3</math> unless later seen as 20), <math>4^3</math> and an intention to cube <math>ax</math> (but allow for <math>ax^3</math>)  Could come from <math>4^6(1 + \frac{ax}{4})^6</math> as long as done correctly  Ignore any other terms if fuller expansion attempted</p> <p>Allow <math>1280a^3x^3</math>, or <math>1280(ax)^3</math>, but not <math>1280ax^3</math> unless <math>a^3</math> subsequently seen, or implied by working</p> <p>Must be equating coeffs – allow if <math>x^3</math> present on both sides (but not just one) as long as they both go at same point  Allow for their coeff of <math>x^3</math>, as long as two, or more, parts of product are attempted eg <math>20ax^3 / 64ax^3</math>  Allow M1 for <math>1280a = 160</math> (giving <math>a = 0.125</math>)  M0 for incorrect division (eg giving <math>a^3 = 8</math>)</p> <p>Allow 0.5, but not an unsimplified fraction  Answer only gets full credit, as does T&amp;I  <b>SR: max of 3 marks</b> for <math>a = 0.5</math> from incorrect algebra, eg <math>1280ax^3 = 160</math>, so <math>a = 0.5</math> would get M1A1(implied)B1</p>

Question		Answer	Marks	Guidance	
3	(ii)	$4^6 + 6 \times 4^5 \times \frac{1}{2} = 4096 + 3072x$	<b>B1</b>	State 4096	Allow $4^6$ if given as final answer Mark final answer – so do not isw if a constant term is subsequently added to 4096 from an incorrect attempt at second term eg using sum rather than product
			<b>B1FT</b>	State $3072x$ , or $(6144 \times \text{their } a)x$	Must follow a numerical value of $a$ , from attempt in part (i) Must be of form $kx$ so just stating coeff of $x$ is B0 Mark final answer  B2 can still be awarded if two terms are not linked by a '+' sign – could be a comma, 'and', or just two separate terms  <b>SR: B1</b> can be awarded if both terms seen as correct, but then 'cancelled' by a common factor
4	(i)	$b^2 = 2.4^2 + 2^2 - 2 \times 2.4 \times 2 \times \cos 40^\circ$ $b = 1.55 \text{ km}$	<b>M1</b>	Attempt use of correct cosine rule	Must be correct formula seen or implied, but allow slip when evaluating eg omission of 2, incorrect extra 'big bracket' Allow M1 even if subsequently evaluated in rad mode (4.02) Allow M1 if expression is not square rooted, as long as LHS was intended to be correct ie $b^2 = \dots$ or $AC^2 = \dots$
			<b>A1</b>	Obtain 1.55, or better	Actual answer is 1.55112003... so allow more accurate answer as long as it rounds to 1.551 Units not required

Question		Answer	Marks	Guidance	
4	(ii)	$\frac{\sin A}{2} = \frac{\sin 40}{1.55} \quad \frac{\sin C}{2.4} = \frac{\sin 40}{1.55}$ $A = 56^\circ \quad C = 84^\circ$ <p>hence bearing is <math>124^\circ</math></p>	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>A1ft</b></p> <p><b>[3]</b></p>	<p>Attempt to find one of the other two angles in triangle</p> <p>Obtain <math>A = 56^\circ</math>, or <math>C = 84^\circ</math></p> <p>Obtain <math>124^\circ</math>, following their angle <math>A</math> or <math>C</math></p>	<p>Could use sine rule or cosine rule, but must be correct rule attempted Need to substitute in and rearrange as far as <math>\sin A = \dots / \cos A = \dots</math> etc, but may not actually attempt angle</p> <p>Any angle rounding to <math>56^\circ</math> or <math>84^\circ</math>, and no errors seen</p> <p>Allow any answer rounding to 124 Finding bearing of <math>A</math> from <math>C</math> is A0 – ie not a MR</p>
4	(iii)	$d = 2 \times \sin 40^\circ$ $= 1.29 \text{ km}$	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>[2]</b></p>	<p>Attempt perpendicular distance</p> <p>Obtain 1.29, or better</p>	<p>Any valid method, but must attempt required distance Can still get M1 if using incorrect or inaccurate sides / angles found earlier in question Allow M1 if evaluated in rad mode (1.49)</p> <p>Allow more accurate final answers in range [1.285, 1.286] A0 for inaccurate answers due to PA elsewhere in question (typically <math>C = 84.4</math>, so <math>A = 55.6</math>, so <math>d = 1.28</math>) Units not required</p>
5	(i)	$f(3) = 54 + 27 - 51 + 6$ $= 36$	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>[2]</b></p>	<p>Attempt <math>f(3)</math></p> <p>Obtain 36</p>	<p>Allow equiv methods as long as remainder is attempted A0 if answer subsequently stated as <math>-36</math> ie do not isw</p>

Question		Answer	Marks	Guidance
5	(ii)	$f(x) = (x - 2)(2x^2 + 7x - 3)$	<p><b>B1</b></p> <p>State or imply that <math>(x - 2)</math> is a factor</p> <p><b>M1</b></p> <p>Attempt full division, or equiv, by <math>(x \pm 2)</math></p> <p><b>A1</b></p> <p>Obtain <math>2x^2</math> and at least one other correct term</p> <p><b>A1</b></p> <p>Obtain <math>(x - 2)(2x^2 + 7x - 3)</math></p> <p><b>[4]</b></p>	<p>Just stating this is enough for B1, even if not used Could be implied by attempting division, or equiv, by <math>(x - 2)</math></p> <p>Must be complete method – ie all three terms attempted If long division then must subtract lower line (allow one slip); if inspection then expansion must give correct first and last terms and also one of the two middle terms of the cubic; if coefficient matching then must be valid attempt at all 3 quadratic coeffs, considering all relevant terms each time Allow M1 for valid division attempt by <math>(x + 2)</math></p> <p>If coeff matching then allow for stating values eg <math>A = 2</math> etc</p> <p>Must be stated as a product</p>
5	(iii)	$b^2 - 4ac = 73$ > 0 hence 3 roots	<p><b>M1</b></p> <p>Attempt explicit numerical calculation to find number of roots of quadratic</p> <p><b>A1ft</b></p> <p>State 3 roots (<math>\sqrt{\text{their quotient}}</math>) Condone no explicit check for repeated roots</p> <p><b>[2]</b></p>	<p>Could attempt discriminant (allow <math>b^2 \pm 4ac</math>), or could use full quadratic formula to attempt to find the roots themselves (implied by stating decimal roots); M0 for factorising unless their incorrect quotient could be factorised M0 for ‘3 roots as positive discriminant’ but no evidence</p> <p>Sufficient working must be shown, and all values shown must be correct Discriminant needs to be 73 (allow <math>7^2 - 4(2)(-3)</math>) Quadratic formula must be correct, though may not necessarily be simplified as far as <math>\frac{1}{4}(-7 \pm \sqrt{73})</math></p> <p>Need to state no. of roots – just listing them is not enough <b>SR:</b> if a conclusion is given in part (iii) then allow evidence from part (ii) eg finding actual roots</p>

Question		Answer	Marks	Guidance	
6	(i)	$u_1 = 80$ $u_2 = 75, u_3 = 70$	B1	State 80	Just a list of numbers is fine, no need for labels
			B1 [2]	State 75 and 70	Ignore extra terms beyond $u_3$
6	(ii)	$S_{20} = \frac{20}{2}(2 \times 80 + 19 \times -5)$ $= 650$	M1	Show intention to sum 1 <sup>st</sup> 20 terms of an arithmetic sequence	Any recognisable attempt at the sum of an AP, including manual addition of terms – no need to list all of the terms, but intention (inc no of terms) must be clear
			M1	Attempt use of correct sum formula for an AP, with $n = 20, a = 80, d = \pm 5$	Must use correct formula – only exception is $10(2a + 9d)$ If using $\frac{1}{2}n(a + l)$ , must be a valid attempt at $l$ , either from $a + 19d$ or from $u_{20}$
			A1 [3]	Obtain 650	Answer only gets full marks, as does manual addition

Question		Answer	Marks	Guidance
6	(iii)	$r = \frac{60}{80} = 0.75$ $u_p = 80 \times 0.75^2 = 45$ $85 - 5p = 45$ $p = 8$	<p><b>M1*</b> Attempt to find <math>u_p</math></p> <p><b>A1</b> Obtain 45</p> <p><b>M1d*</b> Attempt to solve <math>85 - 5p = k</math></p> <p><b>A1</b> Obtain <math>p = 8</math></p> <p><b>[4]</b></p>	<p>Allow any valid method, inc informal Allow if first and/or second terms of their GP are incorrect Allow ratio of <math>\frac{4}{3}</math> if used correctly to find 3<sup>rd</sup> term (<math>60 \div \frac{4}{3}</math>)</p> <p>Seen or implied <b>SR: M1* A0</b> if 45 results from using <math>u_n = ar^n</math>. The following M1A1 are still available.</p> <p><math>k</math> must be from attempt at third term of GP LHS could be <math>80 + (p - 1)(-5)</math>, from <math>p^{\text{th}}</math> term of the AP, but M0 if incorrect eg <math>80 + (p - 1)(5)</math></p> <p>Allow full credit for answer only Any variable, including <math>n</math></p>
6	(iv)	$S_\infty = \frac{80}{1 - 0.75}$ $= 320$	<p><b>M1</b> Use correct formula for sum to infinity</p> <p><b>A1</b> Obtain 320</p> <p><b>[2]</b></p>	<p>Must be from attempt at <math>r</math> for their GP</p> <p>A0 for 'tends to 320', 'approximately 320' etc</p>

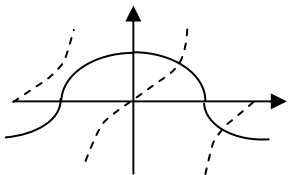
Question		Answer	Marks	Guidance	
7	(a)	$\int (x^3 - 6x^2 + 4x - 24) dx$ $= \frac{1}{4}x^4 - 2x^3 + 2x^2 - 24x + c$	<b>M1</b>  <b>A1ft</b>  <b>A1</b>  <b>[3]</b>	Expand and attempt in  Obtain at least two correct (algebraic) terms  Obtain fully correct expression, inc + c	Must attempt to expand brackets first Increase in power by 1 for the majority of their terms Allow if the constant term disappears  At least two correct from their expansion Allow for unsimplified coefficients  All coefficients now simplified A0 if integral sign or dx still present in their answer (but allow $\int = \dots$ )
7	(b)	$\int 6x^{\frac{3}{2}} dx = \frac{12}{5}x^{\frac{5}{2}}$ $\int (8x^{-2} - 2) dx = -8x^{-1} - 2x$ $\left[ \frac{12}{5}x^{\frac{5}{2}} \right]_0^1 = \frac{12}{5}$ $\left[ -8x^{-1} - 2x \right]_0^2 = (-8) - (-10) = 2$ <p>hence total area = <math>\frac{22}{5}</math></p>	<b>M1</b>  <b>A1</b>  <b>M1</b>  <b>A1</b>  <b>B1</b>  <b>M1</b>	Obtain $kx^{\frac{5}{2}}$  Obtain $\frac{12}{5}x^{\frac{5}{2}}$ , or any exact equiv  Obtain at least one of $-8x^{-1}$ and $-2x$  Obtain $-8x^{-1} - 2x$	Any exact equiv for the index  Including unsimplified coefficient  Allow M1 even if $-2$ disappears Could be part of a sum or difference; with consistent signs  Allow unsimplified expressions If subtraction from other curve attempted before integration then allow for $8x^{-1} + 2x$  Could imply by using it as a limit  Must be using correct $x$ limits, and subtracting, with the appropriate function (allow implicit use of $x = 0$ ); the only error allowed is an incorrect $(2, 0)$ Allow use in any function other than the original, inc from differentiation

7	(b) con	<p><b>Alternative scheme</b> for those who integrate between the curves and the y-axis</p> <p>Some solutions may involve both integration onto x-axis and y-axis, so you may need to combine aspects of both schemes</p>	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>[8]</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A2</b></p>	<p>Attempt fully correct process to find required area</p> <p>Obtain <math>\frac{22}{5}</math>, or any exact equiv</p> <p>Obtain <math>ky^{\frac{5}{3}}</math></p> <p>Obtain <math>6^{\frac{-2}{3}} \times \frac{3}{5} \times y^{\frac{5}{3}}</math></p> <p>Obtain <math>k\sqrt{2+y}</math></p> <p>Obtain <math>2\sqrt{8}\sqrt{2+y}</math></p> <p>Use limits of 6 (and 0) correctly at least once</p> <p>Attempt correct method to find required area – correct use of limits required</p> <p>Obtain 4.4</p>	<p>Use both pairs of limits correctly (allow an incorrect (2, 0)), in appropriate functions and sum the two areas</p> <p>Answer only is 0/8, as no evidence is provided of integration</p>
---	------------	--	--	--	--



Question		Answer	Marks	Guidance	
8	(a)	$\log 7^{w-3} = \log 184$ $(w-3) \log 7 = \log 184$ $w-3 = 2.68$ $w = 5.68$	<b>M1*</b>	Rearrange, introduce logs and use $\log a^b = b \log a$	Must first rearrange to $7^{w-3} = k$ , with $k$ from attempt at $180 \pm 4$ , before introducing logs Can use logs to any base, as long as consistent on both sides If taking $\log_7$ then base must be explicit  Condone lack of brackets ie $w-3 \log 7 = \log 184$ , as long clearly implied by later working  Attempt at correct process ie $w = \frac{\log k}{\log 7} \pm 3$ , or equiv following expanding bracket first  More accurate final answer must round to 5.680  Answer only, or T&I, is 0/4
			<b>A1</b>	Obtain $(w-3) \log 7 = \log 184$ , or equiv eg $w-3 = \log_7 184$	
			<b>M1d*</b>	Attempt to solve linear equation	
			<b>A1</b>	Obtain 5.68, or better	
			<b>[4]</b>		

Question		Answer	Marks	Guidance	
8	(b)	$\log xy = \log 3$ hence $xy = 3$ $3x + y = 10$  $x(10 - 3x) = 3$ $3x^2 - 10x + 3 = 0$ $(3x - 1)(x - 3) = 0$ <b>or</b> $\frac{1}{3}(10 - y)y = 3$ $y^2 - 10y + 9 = 0$ $(y - 1)(y - 9) = 0$  $x = \frac{1}{3}, y = 9$ $x = 3, y = 1$	<b>M1</b>	Attempt correct use of log law to combine 2 (or more) logs	Must be used on at least two of $\log x / \log y / \log 3$ Allow $\log (x^y/3)$ (condone no = 0)
			<b>A1</b>	Obtain $xy = 3$	aef as long as no logs present, or equiv in one variable
			<b>B1</b>	Obtain $3x + y = 10$	aef as long as no logs present, or equiv in one variable
			<b>M1</b>	Attempt to eliminate one variable, and solve the resulting three term quadratic	<b>SR:</b> if A0 B0 given above, then allow <b>B1</b> for a correct combination of the 2 eqns eg $9x + 3y = 10xy$ (others poss)
			<b>A1</b>	Obtain two correct values	Elimination of one variable could happen prior to removal of logs from one equation – as long as logs are then removed completely to obtain three term quadratic
<b>A1</b>	Obtain $x = \frac{1}{3}, y = 9$ and $x = 3, y = 1$	Could be for two values for one variable, or for one pair of correct (x, y) values			
			<b>[6]</b>	Pairings must be clear, but not necessarily as coordinates <b>SR: B1</b> for each pair of correct (x, y) values but no method <b>M1A1B1B1</b> - 1 pair of (x, y) values, from 2 correct eqns but no other method shown (but 6/6 if both pairs found)	

Question		Answer	Marks	Guidance	
9	(i)		<b>B1</b>	Correct shape for $y = k \cos\left(\frac{1}{2}x\right)$	Must show intention to pass through $(-\pi, 0)$ and $(\pi, 0)$ Should be roughly symmetrical in the $y$ -axis, but condone slightly different $y$ -values at $-2\pi$ and $2\pi$ Ignore graph outside of given range
			<b>B1</b>	Correct shape for $y = \tan\left(\frac{1}{2}x\right)$	Must show intention to pass through $(-2\pi, 0)$ , $(0, 0)$ , $(2\pi, 0)$ Asymptotes need not be marked, but there should be no clear overlap of the limbs, nor significant gaps between them Ignore graph outside of given range
			<b>B1</b>	$(0, 3)$ stated or clearly indicated	Can still be given if $y = 3\cos\left(\frac{1}{2}x\right)$ graph is incorrect or not attempted If more than one point marked on the $y$ -axis then mark the label on the graph intercept
			<b>[3]</b>		

Question		Answer	Marks	Guidance	
9	(ii)	$\frac{\sin(\frac{1}{2}x)}{\cos(\frac{1}{2}x)} = 3\cos(\frac{1}{2}x)$ $\sin(\frac{1}{2}x) = 3\cos^2(\frac{1}{2}x)$ $\sin(\frac{1}{2}x) = 3(1 - \sin^2(\frac{1}{2}x))$ $3\sin^2(\frac{1}{2}x) + \sin(\frac{1}{2}x) - 3 = 0 \quad \mathbf{AG}$ $\sin(\frac{1}{2}x) = 0.847, -1.18$ $\frac{1}{2}x = 1.01, 2.13$ $x = 2.02, 4.26$	<b>M1</b>	Attempt use of relevant identities to show given equation	Must attempt use of both identities; these must be correct but allow poor notation eg using $\frac{\sin}{\cos}(\frac{1}{2}x)$ and/or $3(1 - \sin^2)(\frac{1}{2}x)$ could get M1A0
			<b>A1</b>	Obtain given equation, with no errors seen	Use both identities correctly, to obtain given equation Brackets around the $\frac{1}{2}x$ not required
			<b>M1</b>	Attempt to solve given quadratic to find solution(s) for $\sin(\frac{1}{2}x)$	Must use quadratic formula (or completing the square) – M0 if attempting to factorise Allow variables other than $\sin(\frac{1}{2}x)$ , eg $y =$ , or even $x =$ Allow $-1.18$ to be discarded at any stage
			<b>M1</b>	Attempt to solve $\sin(\frac{1}{2}x) = k$	Attempt $\sin^{-1}$ (their root) and then double the answer
			<b>A1</b>	Obtain one correct angle	Allow in degrees ( $116^\circ$ and $244^\circ$ )
			<b>A1</b>	Obtain both correct angles, and no others in given range	Must both be in radians (allow equivs as multiples of $\pi$ ) A0 if extra, incorrect, angles in given range of $[-2\pi, 2\pi]$ but ignore any outside of given range <b>SR:</b> if no working shown then allow B1 for each correct solution (max of B1 if in degrees, or extra solns in range)
		<b>[6]</b>			

**Guidance for marking C2****Accuracy**

Allow answers to 3sf or better, unless an integer is specified or clearly required.

Answers to 2 sf are penalised, unless stated otherwise in the mark scheme.

3sf is sometimes explicitly specified in a question - this is telling candidates that a decimal is required rather than an exact answer eg in logs, and more than 3sf should not be penalised unless stated in mark scheme.

If more than 3sf is given, allow the marks for an answer that falls within the guidance given in the mark scheme, with no obvious errors.

**Extra solutions**

Candidates will usually be penalised if an extra, incorrect, solution is given. However, in trigonometry questions only look at solutions in the given range and ignore any others, correct or incorrect.

**Solving equations**

With simultaneous equations, the method mark is given for eliminating one variable allowing sign errors, addition / subtraction confusion or incorrect order of operations. Any valid method is allowed ie balancing or substitution for two linear equations, substitution only if at least one is non-linear.

**Solving quadratic equations**

Factorising - candidates must get as far as factorising into two brackets which, on expansion, would give the correct coefficient of  $x^2$  and at least one of the other two coefficients. This method is only credited if it is possible to factorise the quadratic – if the roots are surds then candidates are expected to use either the quadratic formula or complete the square.

Completing the square - candidates must get as far as  $(x + p) = \pm \sqrt{q}$ , with reasonable attempts at  $p$  and  $q$ .

Using the formula - candidates need to substitute values into the formula and do at least one further step. Sign slips are allowed on  $b$  and  $4ac$ , but all other aspects of the formula must be seen correct, either algebraic or numerical. The division line must extend under the entire numerator (seen or implied by later working). If the algebraic formula is quoted then candidates are allowed to make one slip when substituting their values. Condone not dividing by  $2a$  as long as it has been seen earlier.

**OCR (Oxford Cambridge and RSA Examinations)**  
1 Hills Road  
Cambridge  
CB1 2EU

**OCR Customer Contact Centre**

**Education and Learning**

Telephone: 01223 553998

Facsimile: 01223 552627

Email: [general.qualifications@ocr.org.uk](mailto:general.qualifications@ocr.org.uk)

**[www.ocr.org.uk](http://www.ocr.org.uk)**

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

**Oxford Cambridge and RSA Examinations**  
is a Company Limited by Guarantee  
Registered in England  
Registered Office; 1 Hills Road, Cambridge, CB1 2EU  
Registered Company Number: 3484466  
OCR is an exempt Charity

**OCR (Oxford Cambridge and RSA Examinations)**  
Head office  
Telephone: 01223 552552  
Facsimile: 01223 552553

