

## 4722 Core Mathematics 2

1 (i)	$\int (x^3 + 8x - 5) dx = \frac{1}{4}x^4 + 4x^2 - 5x + c$	M1	Attempt integration – increase in power for at least 2 terms
		A1	Obtain at least 2 correct terms
		A1	3 Obtain $\frac{1}{4}x^4 + 4x^2 - 5x + c$ (and no integral sign or dx)
(ii)	$\int 12x^{\frac{1}{2}} dx = 8x^{\frac{3}{2}} + c$	B1	State or imply $\sqrt{x} = x^{\frac{1}{2}}$
		M1	Obtain $kx^{\frac{3}{2}}$
		A1	3 Obtain $8x^{\frac{3}{2}} + c$ (and no integral sign or dx) (only penalise lack of + c, or integral sign or dx once)

**6**

2 (i)	$140^\circ = 140 \times \frac{\pi}{180}$ $= \frac{7}{9}\pi$	M1	Attempt to convert $140^\circ$ to radians
		A1	2 Obtain $\frac{7}{9}\pi$ , or exact equiv
(ii)	arc $AB = 7 \times \frac{7}{9}\pi$ $= 17.1$ chord $AB = 2 \times 7 \sin \frac{7}{18}\pi = 13.2$ hence perimeter = 30.3 cm	M1	Attempt arc length using $r\theta$ or equiv method
		A1√	Obtain 17.1, $\frac{49}{9}\pi$ or unsimplified equiv
		M1	Attempt chord using trig. or cosine or sine rules
		A1	4 Obtain 30.3, or answer that rounds to this

**6**

3 (i)	$u_1 = 23^{1/3}$ $u_2 = 22^{2/3}, u_3 = 22$	B1	State $u_1 = 23^{1/3}$
		B1	2 State $u_2 = 22^{2/3}$ and $u_3 = 22$
(ii)	$24 - \frac{2k}{3} = 0$ $k = 36$	M1	Equate $u_k$ to 0
		A1	2 Obtain 36

(iii)	$S_{20} = \frac{20}{2} \left( 2 \times 23 \frac{1}{3} + 19 \times \frac{-2}{3} \right)$ $= 340$	M1	Attempt sum of AP with $n = 20$
		A1	Correct unsimplified $S_{20}$
		A1	3 Obtain 340

**7**

4	$\int_{-2}^2 (x^4 + 3) dx = \left[ \frac{1}{5}x^5 + 3x \right]_{-2}^2$	M1	Attempt integration – increase of power for at least 1 term
		A1	Obtain correct $\frac{1}{5}x^5 + 3x$
	$= \left( \frac{32}{5} + 6 \right) - \left( \frac{-32}{5} - 6 \right)$	M1	Use limits (any two of -2, 0, 2), correct order/subtraction
	$= 24 \frac{4}{5}$	A1	Obtain $24 \frac{4}{5}$
	area of rectangle = $19 \times 4$	B1	State or imply correct area of rectangle
	hence shaded area = $76 - 24 \frac{4}{5}$	M1	Attempt correct method for shaded area
	$= 51 \frac{1}{5}$	A1	7 Obtain $51 \frac{1}{5}$ aef such as 51.2, $\frac{256}{5}$

**OR**

Area = $19 - (x^4 + 3)$	M1	Attempt subtraction, either order
$= 16 - x^4$	A1	Obtain $16 - x^4$ (not from $x^4 + 3 = 19$ )
$\int_{-2}^2 (16 - x^4) dx = \left[ 16x - \frac{1}{5}x^5 \right]_{-2}^2$	M1	Attempt integration
	A1	Obtain $\pm \left( 16x - \frac{1}{5}x^5 \right)$

$$= (32 - \frac{32}{5}) - (-32 - \frac{-32}{5})$$

$$= 51\frac{1}{5}$$

- M1 Use limits – correct order / subtraction  
 A1 Obtain  $\pm 51\frac{1}{5}$   
 A1 Obtain  $51\frac{1}{5}$  only, no wrong working

**7**

**5 (i)**  $\frac{TA}{\sin 107} = \frac{50}{\sin 3}$   
 $TA = 914 \text{ m}$

- M1 Attempt use of correct sine rule to find  $TA$ , or equiv  
 A1 **2** Obtain 914, or better

**(ii)**  $TC = \sqrt{914^2 + 150^2 - 2 \times 914 \times 150 \times \cos 70}$   
 $= 874 \text{ m}$

- M1 Attempt use of correct cosine rule, or equiv, to find  $TC$   
 A1√ Correct unsimplified expression for  $TC$ , following their (i)  
 A1 **3** Obtain 874, or better

**(iii)** dist from  $A = 914 \times \cos 70 = 313 \text{ m}$   
 beyond  $C$ , hence 874 m is shortest dist  
**OR**  
 perp dist =  $914 \times \sin 70 = 859 \text{ m}$

- M1 Attempt to locate point of closest approach  
 A1 **2** Convincing argument that the point is beyond  $C$ ,  
 or obtain 859, or better  
**SR** B1 for 874 stated with no method shown

**7**

**6 (i)**  $S_\infty = \frac{20}{1-0.9}$   
 $= 200$

- M1 Attempt use of  $S_\infty = \frac{a}{1-r}$   
 A1 **2** Obtain 200

**(ii)**  $S_{30} = \frac{20(1-0.9^{30})}{1-0.9}$   
 $= 192$

- M1 Attempt use of correct sum formula for a GP, with  $n = 30$   
 A1 **2** Obtain 192, or better

**(iii)**  $20 \times 0.9^{p-1} < 0.4$   
 $0.9^{p-1} < 0.02$   
 $(p-1)\log 0.9 < \log 0.02$   
 $p-1 > \frac{\log 0.02}{\log 0.9}$   
 $p > 38.1$   
 hence  $p = 39$

- B1 Correct  $20 \times 0.9^{p-1}$  seen or implied  
 M1 Link to 0.4, rearrange to  $0.9^k = c$  (or  $>$ ,  $<$ ), introduce  
 logarithms, and drop power, or equiv correct method  
 M1 Correct method for solving their (in)equation  
 A1 **4** State 39 (not inequality), no wrong working seen

**8**

**7 (i)**  $6k^2a^2 = 24$   
 $k^2a^2 = 4$   
 $ak = 2$  **A.G.**

- M1\* Obtain at least two of  $6, k^2, a^2$   
 M1dep\* Equate  $6k^m a^n$  to 24  
 A1 **3** Show  $ak = 2$  convincingly – no errors allowed

**(ii)**  $4k^3a = 128$   
 $4k^3(\frac{2}{k}) = 128$   
 $k^2 = 16$   
 $k = 4, a = \frac{1}{2}$

- B1 State or imply coeff of  $x$  is  $4k^3a$   
 M1 Equate to 128 and attempt to eliminate  $a$  or  $k$   
 A1 Obtain  $k = 4$   
 A1 **4** Obtain  $a = \frac{1}{2}$   
**SR** B1 for  $k = \pm 4, a = \pm \frac{1}{2}$

**(iii)**  $4 \times 4 \times (\frac{1}{2})^3 = 2$

- M1 Attempt  $4 \times k \times a^3$ , following their  $a$  and  $k$  (allow if still in  
 terms of  $a, k$ )  
 A1 **2** Obtain 2 (allow  $2x^3$ )

**9**

**8 (a)(i)**  $\log_a xy = p + q$

B1 1 State  $p + q$  cwo

**(ii)**  $\log_a \left(\frac{a^2 x^3}{y}\right) = 2 + 3p - q$

M1 Use  $\log a^b = b \log a$  correctly at least once

M1 Use  $\log \frac{a}{b} = \log a - \log b$  correctly

A1 3 Obtain  $2 + 3p - q$

**(b)(i)**  $\log_{10} \frac{x^2 - 10}{x}$

B1 1 State  $\log_{10} \frac{x^2 - 10}{x}$  (with or without base 10)

**(ii)**  $\log_{10} \frac{x^2 - 10}{x} = \log_{10} 9$

B1 State or imply that  $2 \log_{10} 3 = \log_{10} 3^2$

$\frac{x^2 - 10}{x} = 9$

M1 Attempt correct method to remove logs

$x^2 - 9x - 10 = 0$

A1 Obtain correct  $x^2 - 9x - 10 = 0$  aef, no fractions

$(x - 10)(x + 1) = 0$

M1 Attempt to solve three term quadratic

$x = 10$

A1 5 Obtain  $x = 10$  only

**10**

**9 (i)**  $f(1) = 1 - 1 - 3 + 3 = 0$  **A.G.**

B1 Confirm  $f(1) = 0$ , or division with no remainder shown, or matching coeffs with  $R = 0$

$f(x) = (x - 1)(x^2 - 3)$

M1 Attempt complete division by  $(x - 1)$ , or equiv

A1 Obtain  $x^2 + k$

A1 Obtain completely correct quotient (allow  $x^2 + 0x - 3$ )

$x^2 = 3$

M1 Attempt to solve  $x^2 = 3$

$x = \pm \sqrt{3}$

A1 6 Obtain  $x = \pm \sqrt{3}$  only

**(ii)**  $\tan x = 1, \sqrt{3}, -\sqrt{3}$

B1√ State or imply  $\tan x = 1$  or  $\tan x =$  at least one of their roots from (i)

$\tan x = \sqrt{3} \Rightarrow x = \frac{\pi}{3}, \frac{4\pi}{3}$

M1 Attempt to solve  $\tan x = k$  at least once

$\tan x = -\sqrt{3} \Rightarrow x = \frac{2\pi}{3}, \frac{5\pi}{3}$

A1 Obtain at least 2 of  $\frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$  (allow degs/decimals)

$\tan x = 1 \Rightarrow x = \frac{\pi}{4}, \frac{5\pi}{4}$

A1 Obtain all 4 of  $\frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$  (exact radians only)

B1 Obtain  $\frac{\pi}{4}$  (allow degs / decimals)

B1 6 Obtain  $\frac{5\pi}{4}$  (exact radians only)

**SR** answer only is B1 per root, max of B4 if degs / decimals

**12**