

1) Area sector = $\frac{1}{2}r^2\theta = \frac{1}{2} \times 11^2 \times 0.7$
 $= 42.35$ (2)

Area $\Delta = \frac{1}{2}ab\sin C = \frac{1}{2} \times 11 \times 5 \sin 0.7$
 $= 38.98$ (1)

Area segment = $42.35 - 38.98$
 $= 3.37$ (1)

2) width strip = $\frac{2-1}{3} = 2$ (1)

$L = \frac{2}{2}(2 + 2(\sqrt{12} + \sqrt{28}) + \sqrt{52})$ (2)

$= 26.7$ (1)
 ie $\frac{2}{2}(2 + 2(3.46 + 5.29) + 7.21)$

3) $\log_2 2 + \log_2 3 = \log_2 6$ (1)

ii) $2\log_0 x - 3\log_0 y = \log_0 x^2 - \log_0 y^3$ (1)
 $= \log_0 \left(\frac{x^2}{y^3}\right)$ (2)

4) $\frac{BD}{\sin 62} = \frac{16}{\sin 50}$ (1) $BD = \frac{16 \sin 62}{\sin 50}$
 $= 18.4 \text{ cm}$ (1)

ii) $\cos \theta = \frac{10^2 + 20^2 - 18.4^2}{2 \times 10 \times 20} = 0.3998$ (1)

$\theta = 66.4^\circ$ (1)

5) $y = \int 12x^{\frac{1}{2}} dx = 8x^{\frac{3}{2}} + C$ (3)

subst $x=4, y=50$

$50 = 8 \times 8 + C \quad C = -14$ (2)

$y = 8x^{\frac{3}{2}} - 14$ (1)

6) $n=1 \quad u_1 = 7$ (3)

$n=2 \quad u_2 = 9$

$n=3 \quad u_3 = 11$ (2)

ii) AP $a=7 \quad d=2$ (1)

iii) $S_n = 2200 = \frac{n}{2}(2 \times 7 + (n-1) \times 2)$ (2)

$4400 = 12n + 2n^2$

$n^2 + 6n - 2200 = 0$ (1)

6) $(N-44)(N+50) = 0$
 $N = 44$ (1)

7) Area below is -ve
 Area above is +ve (1)

ii) $A = \int_0^3 x^2 - 3x dx + \int_3^5 \frac{x^2 - 3x}{2} dx$ (2)

$A_1 = \left[\frac{x^3}{3} - \frac{3x^2}{2} \right] = \left(9 - \frac{27}{2} \right) - 0 = -4\frac{1}{2}$ (2)

$A_2 = \left[\frac{x^3}{3} - \frac{3x^2}{2} \right] = \left(\frac{125}{3} - \frac{75}{2} \right) - \left(9 - \frac{27}{2} \right)$
 $= 8\frac{2}{3}$ (2)

Total = $8\frac{2}{3} + 4\frac{1}{2}$
 $= 13\frac{1}{6}$ (1)

8) i) $a=10 \quad r=0.8$ (2)

$U_n = ar^{n-1} = 10 \times 0.8^3 = 5.12$

ii) $S_{20} = a \frac{(1-r^{20})}{1-r} = 10 \frac{(1-0.8^{20})}{1-0.8}$
 $= 49.4$ (2)

iii) $S_{\infty} = \frac{a}{1-r} = \frac{10}{1-0.8} = 50$ (1)

$S_{20} - S_n = 50 - \frac{10(1-0.8^{20})}{0.2}$

$= 50 - 50(1-0.8^{20})$ (1)

but $S_{20} - S_n < 0.01$

so $50 - 50(1-0.8^{20}) < 0.01$ (1)
 $\div 50 \quad 1 - (1-0.8^{20}) < 0.0002$

$0.8^{20} < 0.0002$ (1)

$\log_0 8^{20} < \log_0 0.0002$ (1)

$N \log_0 8 < \log_0 0.0002$ (1)
 $N > 38.169$

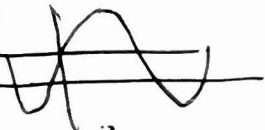
ie $N = 39$ (1)

9. i) $\max(90, 2) \uparrow$ stretch $\times 2$
 $\min(-90, -2)$ (2)

ii) a) 2nd soln $x = 180 - \alpha$ (1)



b) soln $x = -\alpha$ (1)
 or $x = -180 + \alpha$



c) $2\sin x = 2 - 3\cos^2 x$
 $2\sin x = 2 - 3(1 - \sin^2 x)$ (1)

$3\sin^2 x - 2\sin x - 1 = 0$ (1)

$(3\sin x + 1)(\sin x - 1) = 0$ (1)

$\sin x = -\frac{1}{3}$ or $+1$ (1)

10 \uparrow

$x = -19.5$ or $-180 + 19.5$

$= -19.5$ and -160.5 (2)

or $x = 90$ from 2nd bracket

10) i) $(2x+5)^4 = (2x)^4 + 40(2x)^3(5) + 402(2x)^2(5)^2 + 403(2x)5^3 + 5^4$ (2)
 $= 16x^4 + 160x^3 + 600x^2 + 1000x + 625$ (2)

ii) $(2x-5)^4 = 16x^4 - 160x^3 + 600x^2 - 1000x + 625$

ie replace 5 by -5 (2)

$(2x+5)^4 - (2x-5)^4 = 320x^3 + 2000x$ as x^4, x^2 terms disappear
 $k = 2000$

iii) LHS $x=2$ $(2x+5)^4 - (2x-5)^4 = 9^4 - (-1)^4 = 6560$

RHS $3680x - 800 = 7360 - 800 = 6560$

so $x=2$ is a root (1)

but LHS $= 320x^3 + 2000x = 3680x - 800$

12 so $320x^3 - 1680x + 800 = 0$ (1)

$4x^3 - 21x + 10 = 0$ (1)

$x=2$ is a factor do long div to get

$(x-2)(4x^2 + 8x - 5) = 0$ (1)

$(x-2)(2x-1)(2x+5) = 0$ (1)

$x = 2, \frac{1}{2}, -2\frac{1}{2}$ (1)