

7.

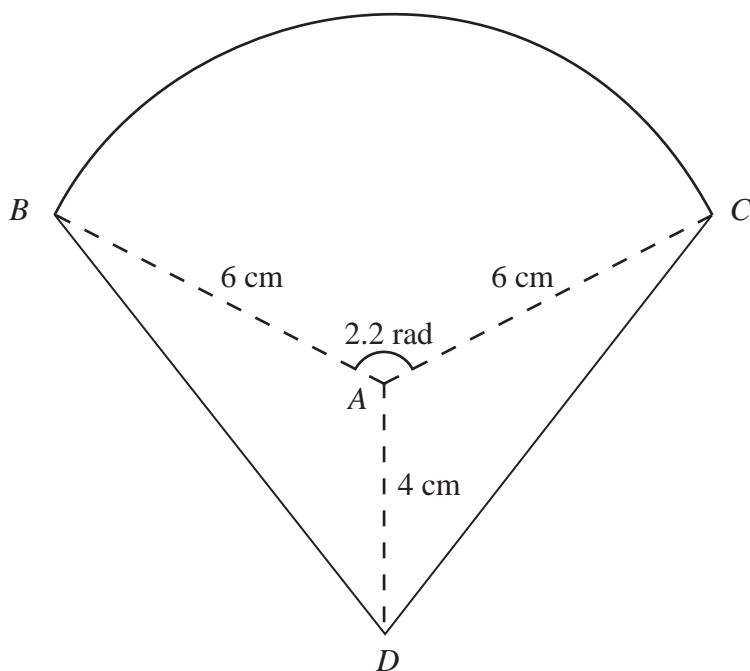


Figure 3

The shape BCD shown in Figure 3 is a design for a logo.

The straight lines DB and DC are equal in length. The curve BC is an arc of a circle with centre A and radius 6 cm. The size of $\angle BAC$ is 2.2 radians and $AD = 4$ cm.

Find

- (a) the area of the sector BAC , in cm^2 , (2)
- (b) the size of $\angle DAC$, in radians to 3 significant figures, (2)
- (c) the complete area of the logo design, to the nearest cm^2 . (4)



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8. (a) Show that the equation

$$4 \sin^2 x + 9 \cos x - 6 = 0$$

can be written as

$$4 \cos^2 x - 9 \cos x + 2 = 0.$$

(2)

(b) Hence solve, for $0 \leq x < 720^\circ$,

$$4 \sin^2 x + 9 \cos x - 6 = 0,$$

giving your answers to 1 decimal place.

(6)



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Question 8 continued

Lined writing area for Question 8 continued.

Q8

(Total 8 marks)



9. The first three terms of a geometric series are $(k + 4)$, k and $(2k - 15)$ respectively, where k is a positive constant.

(a) Show that $k^2 - 7k - 60 = 0$. (4)

(b) Hence show that $k = 12$. (2)

(c) Find the common ratio of this series. (2)

(d) Find the sum to infinity of this series. (2)

Lined area for student work, consisting of 20 horizontal lines.



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Question 9 continued

Lined writing area for the answer to Question 9.



H 3 0 9 5 7 A 0 2 3 2 8

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10. A solid right circular cylinder has radius r cm and height h cm.

The total surface area of the cylinder is 800 cm^2 .

(a) Show that the volume, $V \text{ cm}^3$, of the cylinder is given by

$$V = 400r - \pi r^3. \tag{4}$$

Given that r varies,

(b) use calculus to find the maximum value of V , to the nearest cm^3 . (6)

(c) Justify that the value of V you have found is a maximum. (2)



