

2.

$$y = \frac{x}{\sqrt{1+x}}$$

(a) Complete the table below with the value of y corresponding to $x = 1.3$, giving your answer to 4 decimal places.

(1)

x	1	1.1	1.2	1.3	1.4	1.5
y	0.7071	0.7591	0.8090		0.9037	0.9487

(b) Use the trapezium rule, with all the values of y in the completed table, to obtain an approximate value for

$$\int_1^{1.5} \frac{x}{\sqrt{1+x}} dx$$

giving your answer to 3 decimal places.

You must show clearly each stage of your working.

(4)



4. $f(x) = ax^3 - 11x^2 + bx + 4$, where a and b are constants.

When $f(x)$ is divided by $(x - 3)$ the remainder is 55

When $f(x)$ is divided by $(x + 1)$ the remainder is -9

(a) Find the value of a and the value of b .

(5)

Given that $(3x + 2)$ is a factor of $f(x)$,

(b) factorise $f(x)$ completely.

(4)



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5. The first three terms of a geometric series are $4p$, $(3p + 15)$ and $(5p + 20)$ respectively, where p is a **positive** constant.

(a) Show that $11p^2 - 10p - 225 = 0$ (4)

(b) Hence show that $p = 5$ (2)

(c) Find the common ratio of this series. (2)

(d) Find the sum of the first ten terms of the series, giving your answer to the nearest integer. (3)



6. Given that $\log_3 x = a$, find in terms of a ,

(a) $\log_3 (9x)$ **(2)**

(b) $\log_3 \left(\frac{x^5}{81} \right)$ **(3)**

giving each answer in its simplest form.

(c) Solve, for x ,

$$\log_3 (9x) + \log_3 \left(\frac{x^5}{81} \right) = 3$$

giving your answer to 4 significant figures. **(4)**



7.

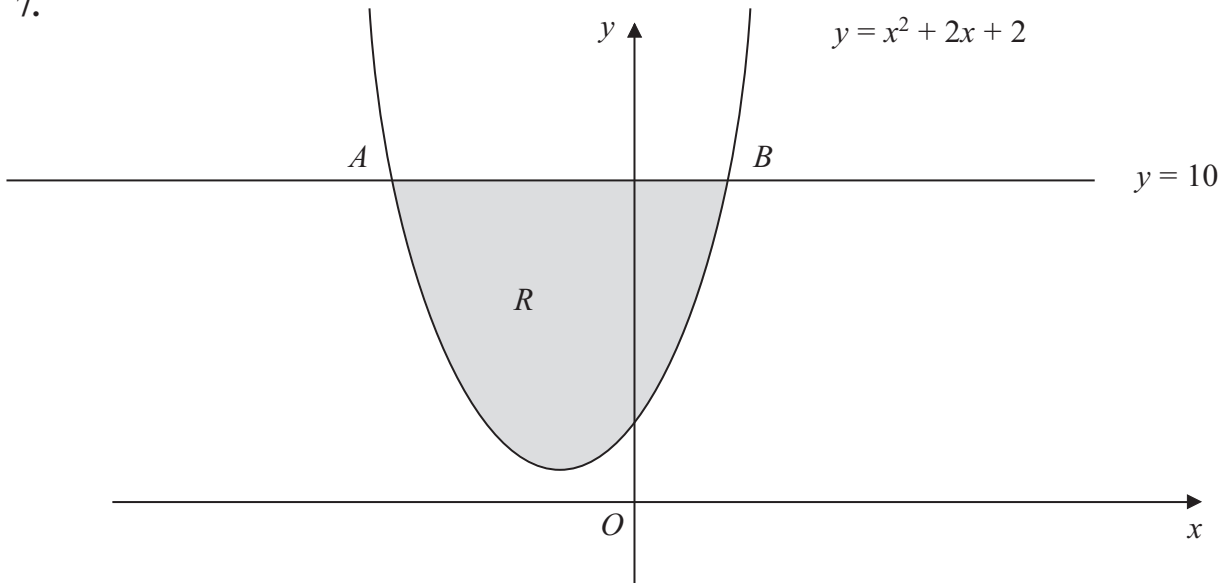


Figure 1

The line with equation $y = 10$ cuts the curve with equation $y = x^2 + 2x + 2$ at the points A and B as shown in Figure 1. The figure is not drawn to scale.

- (a) Find by calculation the x -coordinate of A and the x -coordinate of B . **(2)**

The shaded region R is bounded by the line with equation $y = 10$ and the curve as shown in Figure 1.

- (b) Use calculus to find the exact area of R . **(7)**



8.

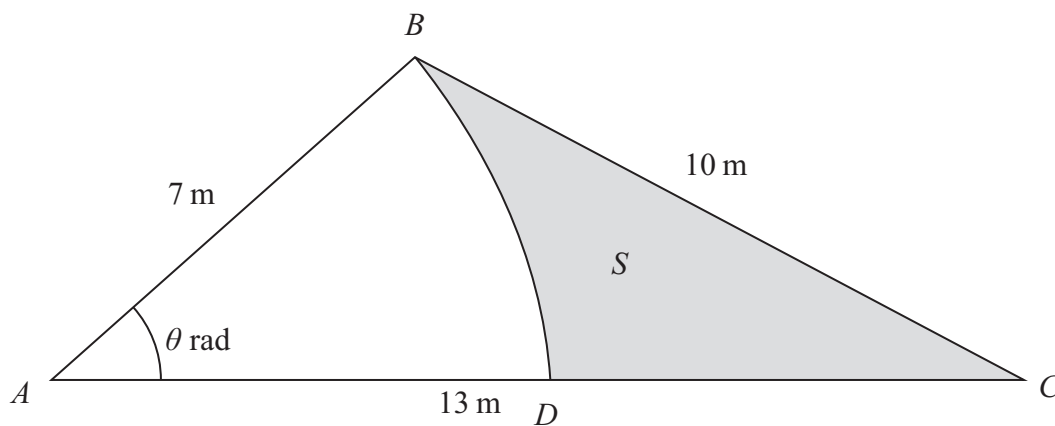


Figure 2

Figure 2 shows the design for a triangular garden ABC where $AB = 7$ m, $AC = 13$ m and $BC = 10$ m.

Given that angle $BAC = \theta$ radians,

(a) show that, to 3 decimal places, $\theta = 0.865$ **(3)**

The point D lies on AC such that BD is an arc of the circle centre A , radius 7 m.

The shaded region S is bounded by the arc BD and the lines BC and DC . The shaded region S will be sown with grass seed, to make a lawned area.

Given that 50 g of grass seed are needed for each square metre of lawn,

(b) find the amount of grass seed needed, giving your answer to the nearest 10 g. **(7)**



