



1. A circle  $C$  has equation

$$x^2 + y^2 - 10x + 6y - 15 = 0.$$

(a) Find the coordinates of the centre of  $C$ . **(2 marks)**

(b) Find the radius of  $C$ . **(2 marks)**

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2. Express  $\frac{y+3}{(y+1)(y+2)} - \frac{y+1}{(y+2)(y+3)}$  as a single fraction in its simplest form.

**(5 marks)**

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3. Given that  $2 \sin 2\theta = \cos 2\theta$ ,

(a) show that  $\tan 2\theta = 0.5$ . **(1 marks)**

(b) Hence find the values of  $\theta$ , to one decimal place, in the interval  $0 \leq \theta < 360$  for which  $2 \sin 2\theta^\circ = \cos 2\theta^\circ$ . **(5 marks)**

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4.  $f(x) = x^3 - x^2 - 7x + c$ , where  $c$  is a constant.

Given that  $f(4) = 0$ ,

(a) find the value of  $c$ , **(2 marks)**

(b) factorise  $f(x)$  as the product of a linear factor and a quadratic factor. **(3 marks)**

(c) Hence show that, apart from  $x = 4$ , there are no real values of  $x$  for which  $f(x) = 0$ . **(2 marks)**

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5.

Figure 1

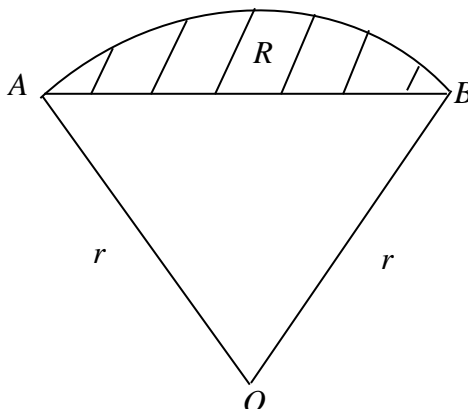


Figure 1 shows the sector  $OAB$  of a circle of radius  $r$  cm. The area of the sector is  $15 \text{ cm}^2$  and  $\angle AOB = 1.5$  radians.

- (a) Prove that  $r = 2\sqrt{5}$ . (3 marks)
- (b) Find, in cm, the perimeter of the sector  $OAB$ . (2 marks)

The segment  $R$ , shaded in Fig 1, is enclosed by the arc  $AB$  and the straight line  $AB$ .

- (c) Calculate, to 3 decimal places, the area of  $R$ . (3 marks)

6. The third and fourth terms of a geometric series are 6.4 and 5.12 respectively.

Find

- (a) the common ratio of the series, (2 marks)
- (b) the first term of the series, (2 marks)
- (c) the sum to infinity of the series. (2 marks)
- (d) Calculate the difference between the sum to infinity of the series and the sum of the first 25 terms of the series. (4 marks)

7.  $f(x) = 5\sin 3x^\circ$ ,  $0 \leq x \leq 180$ .

- (a) Sketch the graph of  $f(x)$ , indicating the value of  $x$  at each point where the graph intersects the  $x$ -axis **(3 marks)**
- (b) Write down the coordinates of all the maximum and minimum points of  $f(x)$ . **(3 marks)**
- (c) Calculate the values of  $x$  for which  $f(x) = 2.5$  **(4 marks)**
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8. (i) Solve, for  $0^\circ < x < 180^\circ$ , the equation

$$\sin(2x + 50^\circ) = 0.6,$$

giving your answers to 1 decimal place. **(7 marks)**

- (ii) In the triangle  $ABC$ ,  $AC = 18$  cm,  $\angle ABC = 60^\circ$  and  $\sin A = \frac{1}{3}$ .

- (a) Use the sine rule to show that  $BC = 4\sqrt{3}$ . **(4 marks)**
- (b) Find the exact value of  $\cos A$ . **(2 marks)**
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9.

Figure 2

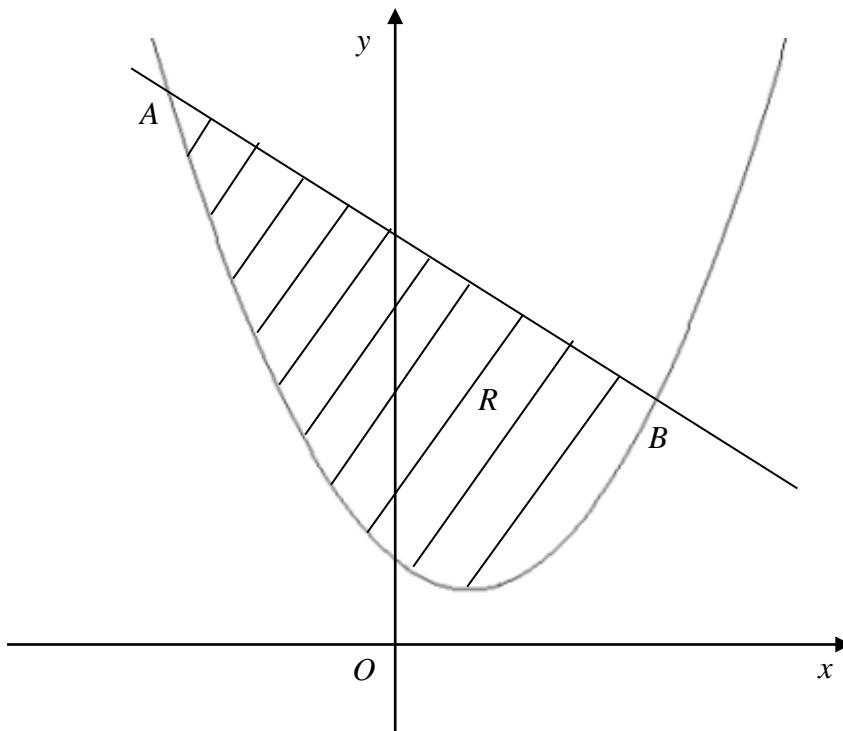


Figure 2 shows the line with equation  $y = 9 - x$  and the curve with equation  $y = x^2 - 2x + 3$ . The line and the curve intersect at the points  $A$  and  $B$ , and  $O$  is the origin.

(a) Calculate the coordinates of  $A$  and the coordinates of  $B$ . **(5 marks)**

The shaded region  $R$  is bounded by the line and the curve.

(b) Calculate the area of  $R$ . **(7 marks)**

**END**