

1. Given that $p = \log_q 16$, express in terms of p ,

(a) $\log_q 2$,

(2)

(b) $\log_q (8q)$.

(4)

2. The expansion of $(2 - px)^6$ in ascending powers of x , as far as the term in x^2 , is

$$64 + Ax + 135x^2.$$

Given that $p > 0$, find the value of p and the value of A .

(7)

3. A circle C has equation

$$x^2 + y^2 - 6x + 8y - 75 = 0.$$

(a) Write down the coordinates of the centre of C , and calculate the radius of C .

(3)

A second circle has centre at the point $(15, 12)$ and radius 10.

(b) Sketch both circles on a single diagram and find the coordinates of the point where they touch.

(4)

4. (a) Sketch, for $0 \leq x \leq 360^\circ$, the graph of $y = \sin(x + 30^\circ)$.

(2)

(b) Write down the coordinates of the points at which the graph meets the axes.

(3)

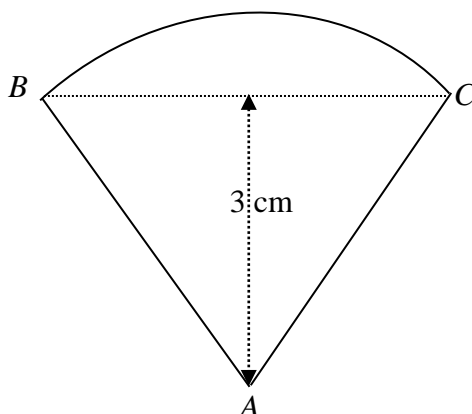
(c) Solve, for $0 \leq x < 360^\circ$, the equation

$$\sin(x + 30^\circ) = -\frac{1}{2}.$$

(3)

5.

Figure 1



The shape of a badge is a sector ABC of a circle with centre A and radius AB , as shown in Fig 1. The triangle ABC is equilateral and has a perpendicular height 3 cm.

- (a) Find, in surd form, the length AB . (2)
- (b) Find, in terms of π , the area of the badge. (2)
- (c) Prove that the perimeter of the badge is $\frac{2\sqrt{3}}{3}(\pi + 6)$ cm. (2)

6.

$$f(x) = 6x^3 + px^2 + qx + 8, \text{ where } p \text{ and } q \text{ are constants.}$$

Given that $f(x)$ is exactly divisible by $(2x - 1)$, and also that when $f(x)$ is divided by $(x - 1)$ the remainder is -7 ,

- (a) find the value of p and the value of q . (6)
- (b) Hence factorise $f(x)$ completely. (3)

7. A geometric series has first term 1200. Its sum to infinity is 960.

(a) Show that the common ratio of the series is $-\frac{1}{4}$. (3)

(a) Find, to 3 decimal places, the difference between the ninth and tenth terms of the series. (3)

(c) Write down an expression for the sum of the first n terms of the series. (2)

Given that n is odd,

(d) prove that the sum of the first n terms of the series is $960(1 + 0.25^n)$. (2)

8. A circle C has centre $(3, 4)$ and radius $3\sqrt{2}$. A straight line l has equation $y = x + 3$.

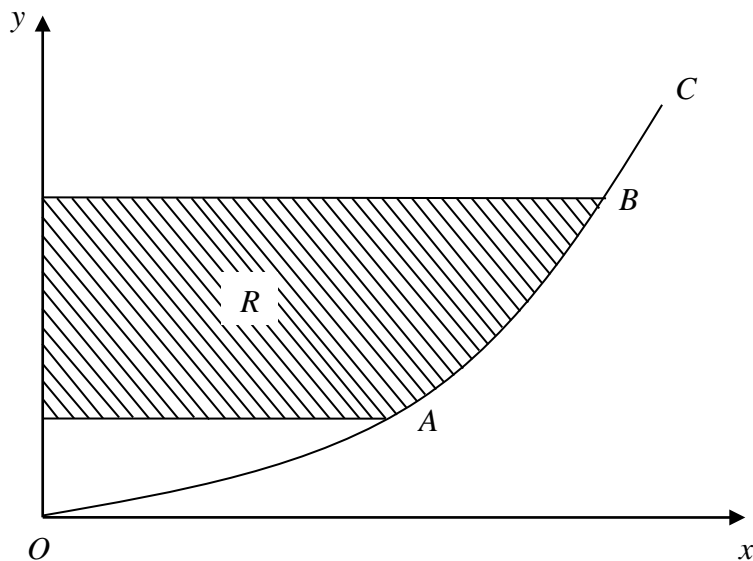
(a) Write down an equation of the circle C . (2)

(b) Calculate the exact coordinates of the two points where the line l intersects C , giving your answers in surds. (5)

(c) Find the distance between these two points. (2)

9.

Figure 2



The curve C , shown in Fig. 2, represents the graph of

$$y = \frac{x^2}{25}, \quad x \geq 0.$$

The points A and B on the curve C have x -coordinates 5 and 10 respectively.

(a) Write down the y -coordinates of A and B . (1)

(b) Find an equation of the tangent to C at A . (4)

The finite region R is enclosed by C , the y -axis and the lines through A and B parallel to the x -axis.

(c) For points (x, y) on C , express x in terms of y . (2)

(d) Use integration to find the area of R . (5)

END