

CORE MATHEMATICS 2 (C) TEST PAPER 10 Page 2

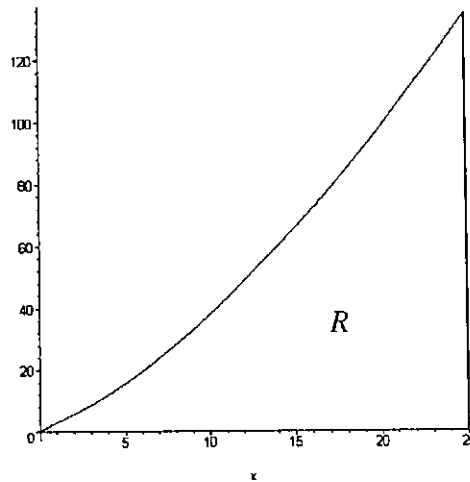
8. S_1 is the sum of the positive integers from 1 to n inclusive.

S_2 is the sum of the *odd* positive integers from 1 to $2n + 1$ inclusive.

Given that $S_2 - S_1 = 66$, find the value of n .

[10]

9. The diagram shows the region R bounded by the curve $y = (x + 2)\sqrt{x}$, the line $x = 25$ and the x -axis.



(i) Use the trapezium rule, with five intervals of equal length, to estimate the area of R to the nearest integer.

[6]

(ii) Calculate the true value of this area.

[5]

CORE MATHS 2 (C) TEST PAPER 10 : ANSWERS AND MARK SCHEME

1. (i) (a) $4 \log_3 x = 4y$ (b) $\log_3 81 - \log_3 x = 4 - y$ B1 M1 A1
 (ii) $\log_{10} 8 / \log_{10} 9 = 0.946$ M1 A1 5
2. $\sin^2 x = 2 \cos x$ $\cos^2 x + 2 \cos x - 1 = 0$ $(\cos x + 1)^2 = 2$ B1 M1 A1
 $\cos x = \sqrt{2} - 1 = 0.414$ $x = 66, x = 294$ M1 A1 A1 6
3. (i) $x^2 = 3(48) = 144$ $x = -12$ or $x = 12$ M1 A1 A1
 (ii) $r = \frac{1}{4}$ or $-\frac{1}{4}$ $S_{\infty} = 48/(5/4) = 38.4$ or $48/(3/4) = 64$ B1 M1 A1 A1 7
4. (i) $\sin C / 4 = \sin 1 / 3.5$ $\sin C = 0.962$ $\angle ACB = 1.29$ M1 A1 A1
 (ii) $\angle ACB = 1.293$; $\angle BAC = 0.849$ Area = $7 \sin 0.849 = 5.3 \text{ cm}^2$ M1 A1 M1 A1 7
5. (i) $\frac{1}{2} r^2 \theta = 100$ $\theta = 200/r^2$ Perimeter = $2r + r\theta = 2r + 200/r$ M1 A1 M1 A1
 (ii) $dp/dr = 2 - 200/r^2 = 0$ when $r = 10$ M1 A1 M1 A1 8
6. (i) $y = \int 2x + 2 \, dx = x^2 + 2x + c$ $y(1) = 5$ so $c = 2$ $y = x^2 + 2x + 2$ M1 A1 M1 A1
 (ii) $y = x + k$ has gradient 1, so at P, $2(x + 1) = 1$ $x = -1/2$ M1 A1
 Then $y = 5/4$, so $k = 7/4$ M1 A1 8
7. (i) $(2 - x)^6 = 2^6 + 6(2^5)(-x) + 15(2^4)(-x)^2 + 20(2^3)(-x)^3 + 15(2^2)(-x)^4$ M1 A1
 $+ 6(2)(-x)^5 + (-x)^6 = 64 - 192x + 240x^2 - 160x^3 + 60x^4 - 12x^5 + x^6$ M1 A1
 (ii) $(2 + x)^6 = 64 + 192x + 240x^2 + 160x^3 + 60x^4 + 12x^5 + x^6$ M1 A1
 (iii) $(2 + x)^6 - (2 - x)^6 = 384x + 320x^3 + 24x^5 = 8x(3x^4 + 40x^2 + 48)$ M1 A1
 $= 8x(3x^2 + 4)(x^2 + 12)$ M1 A1 10
8. $S_1 = \frac{1}{2} n(n + 1)$ $S_2 = \frac{1}{2} (n + 1)(2 + 2n) = (n + 1)^2$ M1 A1 M1 A1 A1
 When $(n + 1)^2 - \frac{1}{2} n(n + 1) = 66$, $(n + 1)(2n + 2 - n) = 132$ M1 A1 A1
 $n^2 + 3n - 130 = 0$ $(n - 10)(n + 13) = 0$ $n = 10$ M1 A1 10
9. (i) (0, 0), (5, 15.652), (10, 37.947), (15, 65.841), (20, 98.387), (25, 135) B3
 $\frac{1}{2} (5)(135 + 2(217.827)) = 1427$ M1 A1 A1
 (ii) $\int_0^{25} x^{3/2} + 2x^{1/2} \, dx = \left[\frac{2}{5} x^{5/2} + \frac{4}{3} x^{3/2} \right]_0^{25} = 1250 + 500/3 = 1416 \frac{2}{3}$ B2 M1 A1 A1 11