

1	$c = 6$ $k = -7$	1 2	M1 for $f(2) = 0$ used or for long division as far as $x^3 - 2x^2$ in working	3
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2	(i) $(x + 1)(2x - 3) = 9$ o.e. $2x^2 - x - 3 = 18$ or $x^2 - \frac{1}{2}x - \frac{3}{2} = 9$ (ii) $(x - 7)(x + 3)$ -3 and $\frac{7}{2}$ o.e. or ft their factors base 4, height 4.5 o.e. cao	M1 A1 B1 B1 B1	for clear algebraic use of $\frac{1}{2}bh$; condone $(x + 1)(2x - 3) = 18$ allow x terms uncollected. NB ans $2x^2 - x - 21 = 0$ given NB B0 for formula or comp. sq. if factors seen, allow omission of -3 B0 if also give $b = -9, h = -2$	5
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3	$f(2) = 3$ seen or used $2^3 + 2k + 5 = 3$ o.e. $k = -5$	M1 M1 B1	allow M1 for divn by $(x - 2)$ with $x^2 + 2x + (k + 4)$ or $x^2 + 2x - 1$ obtained <u>alt</u> : M1 for $(x - 2)(x^2 + 2x - 1) + 3$ (may be seen in division) then M1dep (and B1) for $x^3 - 5x + 5$ <u>alt</u> divn of $x^3 + kx + 2$ by $x - 2$ with no rem.	3
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4	$f(1)$ used $1^3 + 3 \times 1 + k = 6$ $k = 2$	M1 A1 A1	or division by $x - 1$ as far as $x^2 + x$ or remainder = $4 + k$ B3 for $k = 2$ www	3
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<p>5</p>	<p>$5 + 2k$ soi</p> <p>$k = 12$</p> <p>attempt at $f(3)$</p> <p>$27 + 36 + m = 59$ o.e.</p> <p>$m = -4$ cao</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>allow M1 for expansion with $5x^3 + 2kx^3$ and no other x^3 terms or M1 for $(29 - 5) / 2$ soi</p> <p>must substitute 3 for x in cubic not product or long division as far as obtaining $x^2 + x$ in quotient or from division $m - (-63) = 59$ o.e. or for $27 + 3k + m = 59$ or ft their k</p>
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<p>6 (i)</p>	<p>trials of at calculating $f(x)$ for at least one factor of 30</p> <p>details of calculation for $f(2)$ or $f(-3)$ or $f(-5)$</p> <p>attempt at division by $(x - 2)$ as far as $x^3 - 2x^2$ in working</p> <p>correctly obtaining $x^2 + 8x + 15$</p> <p>factorising a correct quadratic factor</p> <p>$(x - 2)(x + 3)(x + 5)$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>M0 for division or inspection used</p> <p>or equiv for $(x + 3)$ or $(x + 5)$; or inspection with at least two terms of quadratic factor correct</p> <p>or B2 for another factor found by factor theorem</p> <p>for factors giving two terms of quadratic correct; M0 for formula without factors found</p> <p>condone omission of first factor found; ignore '= 0' seen</p> <p>allow last four marks for $(x - 2)(x + 3)(x + 5)$ obtained; for all 6 marks must see factor theorem use first</p>
<p>6 (ii)</p>	<p>sketch of cubic right way up, with two turning points</p> <p>values of intns on x axis shown, correct $(-5, -3, \text{ and } 2)$ or ft from their factors/ roots in (i)</p> <p>y-axis intersection at -30</p>	<p>B1</p> <p>B1</p> <p>B1</p>	<p>0 if stops at x-axis</p> <p>on graph or nearby in this part</p> <p>mark intent for intersections with both axes</p> <p>or $x = 0, y = -30$ seen in this part if consistent with graph drawn</p>

<p>6 (iii)</p>	<p>$(x - 1)$ substituted for x in either form of eqn for $y = f(x)$</p> <p>$(x - 1)^3$ expanded correctly (need not be simplified) or two of their factors multiplied correctly</p> <p>correct completion to given answer [condone omission of 'y =']</p>	<p>M1</p> <p>M1 dep</p> <p>M1</p>	<p>correct or ft their (i) or (ii) for factorised form; condone one error; allow for new roots stated as $-4, -2$ and 3 or ft</p> <p>or M1 for correct or correct ft multiplying out of all 3 brackets at once, condoning one error [$x^3 - 3x^2 + x^2 + 2x^2 + 8x - 6x - 12x - 24$]</p> <p>unless all 3 brackets already expanded, must show at least one further interim step allow SC1 for $(x + 1)$ subst <u>and</u> correct exp of $(x + 1)^3$ or two of their factors ft</p> <p><u>or</u>, for those using given answer: M1 for roots stated or used as $-4, -2$ and 3 or ft A1 for showing all 3 roots satisfy given eqn B1 for comment re coefft of x^3 or product of roots to show that eqn of translated graph is not a multiple of RHS of given eqn</p>
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7		f(-2) used $-8 + 36 - 40 + 12 = 0$	M1 A1	or M1 for division by $(x + 2)$ attempted as far as $x^3 + 2x^2$ then A1 for $x^2 + 7x + 6$ with no remainder	2
	ii	divn attempted as far as $x^2 + 3x$ $x^2 + 3x + 2$ or $(x + 2)(x + 1)$	M1 A1	or inspection with $b = 3$ or $c = 2$ found; B2 for correct answer	2
	iii	$(x + 2)(x + 6)(x + 1)$	2	allow seen earlier; M1 for $(x + 2)(x + 1)$	2
	iv	sketch of cubic the right way up <u>through</u> 12 marked on y axis intercepts $-6, -2, -1$ on x axis	G1 G1 G1	with 2 turning pts; no 3rd tp curve must extend to $x > 0$ condone no graph for $x < -6$	3
	v	$[x](x^2 + 9x + 20)$ $[x](x + 4)(x + 5)$ $x = 0, -4, -5$	M1 M1 A1	or other partial factorisation or B1 for each root found e.g. using factor theorem	3