

Question		Answer	Marks	Guidance
1		<p>use of $f(2)$</p> $4 \times 2^3 + 2k + 6 = 42$ $k = 2$ <p>$[x =] -1$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[4]</p>	<p>2 substituted in $f(x)$ or $f(2) = 42$ seen or correct division of $4x^3 + kx + 6$ by $x - 2$ as far as obtaining $4x^2 + 8x + (k + 16)$ oe [may have $4x^2 + 8x + 18$]</p> <p>or $6 + 2(k + 16) = 42$ oe or finding (usually after division) that the constant term is 36 and then working with the x term to find k eg $kx + 16x = 18x$</p> <p>as their answer, not just a trial;</p> <p>A0 for just $f(-1) = 0$ with no further statement</p> <p>A0 if confusion between roots and factors in final statement eg '$x + 1$ is a root', even if they also state $x = -1$</p>
				accept with no working since it can be found by inspection

2		$f(2) = 18$ seen or used	M1	or long division oe as far as obtaining a remainder (ie not involving x) and equating that remainder to 18 (there may be errors along the way)	A0 for just 2^5 instead of 32 unless 32 implied by further work
		$32 + 2k - 20 = 18$ oe	A1	after long division: $2(k + 16) - 20 = 18$ oe	
		$[k =] 3$	A1 [3]		

3	(i)	$3n$ isw	1 [1]	accept equivalent general explanation	
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3	(ii)	at least one of $(n - 1)^2$ and $(n + 1)^2$ correctly expanded	M1	must be seen	M0 for just $n^2 + 1 + n^2 + n^2 + 1$
		$3n^2 + 2$	B1		accept even if no expansions / wrong expansions seen
		comment eg $3n^2$ is always a multiple of 3 so remainder after dividing by 3 is always 2	B1	dep on previous B1 B0 for just saying that 2 is not divisible by 3 – ust comment on $3n^2$ term as well allow B1 for $\frac{3n^2 + 2}{3} = n^2 + \frac{2}{3}$	SC: $n, n + 1, n + 2$ used similarly can obtain first M1, and allow final B1 for similar comment on $3n^2 + 6n + 5$
			[3]		

4	(i)	<p>$f(1) = 1 - 1 + 1 + 9 - 10 [= 0]$</p> <p>attempt at division by $(x - 1)$ as far as $x^4 - x^3$ in working</p> <p>correctly obtaining $x^3 + x + 10$</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>allow for correct division of $f(x)$ by $(x - 1)$ showing there is no remainder,</p> <p>or for $(x - 1)(x^3 + x + 10)$ found, showing it 'works' by multiplying it out</p> <p>allow equiv for $(x + 2)$ as far as $x^4 + 2x^3$ in working</p> <p>or for inspection with at least two terms of cubic factor correct</p> <p>or $x^3 - 3x^2 + 7x - 5$</p>	<p>condone $1^4 - 1^3 + 1^2 + 9 - 10$</p> <p>eg for inspection, M1 for two terms right and two wrong</p> <p>if M0 and this division / factorising is done in part (ii) or (iii), allow SC1 if correct cubic obtained there; attach the relevant part to (i) with a formal chain link if not already seen in the image zone for (i)</p>
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4	(iii)	<p>attempted division of $x^3 + x + 10$ by $(x + 2)$ as far as $x^3 + 2x^2$ in working</p> <p>correctly obtaining $x^2 - 2x + 5$</p> <p>use of $b^2 - 4ac$ with $x^2 - 2x + 5$</p> <p>$b^2 - 4ac = 4 - 20 [= -16]$</p> <p>so only two real roots[of $f(x)$] [and hence no more linear factors]</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[5]</p>	<p>or $x^3 - 3x^2 + 7x - 5$ by $(x - 1)$ as far as $x^3 - x^2$ in working</p> <p>or inspection with at least two terms of quadratic factor correct</p> <p>allow these first 2 marks if this has been done in (ii), even if not used here</p> <p>may be in attempt at formula (ignore rest of formula)</p> <p>may be in formula;</p> <p>or no real roots of $x^2 - 2x + 5 = 0$; allow this last mark if clear use of $x^2 - 2x + 5 = 0$, even if error in $b^2 - 4ac$, provided result negative, but no ft from wrong factor</p> <p>if last M1 not earned, allow SC1 for stating that the only factors of 5 are 1 and 5 and reasoning eg that $(x - 1)(x - 5)$ and $(x + 1)(x + 5)$ do not give $x^2 - 2x + 5$ [hence $x^2 - 2x + 5$ does not factorise]</p> <p>alt method: allow M1 for attempted division of quartic by $x^2 + x - 2$ as far as $x^4 + x^3 - 2x^2$ in working, or inspection etc</p> <p>or completing square form attempted</p> <p>or attempt at calculus or symmetry to find min pt</p> <p>NB M0 for use of $b^2 - 4ac$ with cubic factor etc</p> <p>or $(x - 1)^2 + 4$</p> <p>or $\min = (1, 4)$</p> <p>or $(x - 1)^2 + 4$ is always positive so no real roots [of $(x - 1)^2 + 4 = 0$] [and hence no linear factors]</p> <p>or similar conclusion from min pt</p>

5		$16 + 2b + c = 0$ oe $81 - 3b + c = 85$ oe $20 + 5b = 0$ oe $b = -4$ and $c = -8$	M1 B2 M1 A1 [5]	need not be simplified; condone 8 or 32 as first term if 2^4 not seen M1 for $f(-3)$ seen or used, condoning one error except $+3b$ – need not be simplified or for long division as far as obtaining $x^3 - 3x^2$ in quotient for elimination of one variable, ft their equations in b and c , condoning one error in rearrangement of their original equations or in one term in the elimination allow correct answers to imply last M1 after correct earlier equations	in this question use annotation to indicate where part marks are earned eg M1 for $81 - 3b + c = 0$ ‘long division’ may be seen in grid or a mixture of methods may be used eg B2 for $c - 3(b - 27) = 85$ correct operation must be used in elimination for misread of x^4 as x^3 or x^2 or higher powers, allow all 3 Ms equivalently
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Question		er	Marks	Guidance	
6		$6n + 9$ isw or $3(2n + 3)$	B1		
		$6n$ is even [but 9 is odd], even + odd = odd or $2n + 3$ is odd since even + odd = odd and odd \times odd = odd ‘ n is a multiple of 3’ or ‘ n is divisible by 3’ without additional incorrect statement(s)	B1 dep	this mark is dependent on the previous B1 accept equiv. general statements using either $6n + 9$ or $3(2n + 3)$	
			B2	B2 for ‘it is divisible by 9, so n is divisible by 3’ M1 for ‘ $6n$ is divisible by 9’ or ‘ $2n + 3$ is divisible by 3’ or for ‘ n is a multiple of 3’ oe with additional incorrect statement(s)	B2 for just ‘it is divisible by 3’ but M1 for ‘it is divisible by 9, so it is divisible by 3’ eg M1 for ‘ n is divisible by 9, so n is divisible by 3’ N.B. 0 for ‘ n is a factor of 3’ (but M1 may be earned earlier)
			[4]		

8	$\frac{9y^{10}}{2x^2}$ oe as final answer	3	1 for each 'term'; 27/6 gets 0 for first term if 0, allow B1 for $(3xy^4)^3 = 27x^3y^{12}$	allow eg $4.5x^{-2}y^{10}$
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9	attempt at $f(-3)$ $-27 + 18 - 15 + k = 6$ $k = 30$	M1 A1 A1	or M1 for long division by $(x + 3)$ as far as obtaining $x^2 - x$ and A1 for obtaining remainder as $k - 24$ (but see below) equating coefficients method: M2 for $(x + 3)(x^2 - x + 8)$ [+6] o.e. (from inspection or division) eg M2 for obtaining $x^2 - x + 8$ as quotient in division
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10	10 www	3	M1 for $f(3) = 1$ soi and A1 for $31 - 3k = 1$ or $27 - 3k = -3$ o.e. [a correct 3-term or 2-term equation] long division used: M1 for reaching $(9 - k)x + 4$ in working and A1 for $4 + 3(9 - k) = 1$ o.e. equating coeffs method: M2 for $(x - 3)(x^2 + 3x - 1)$ [+ 1] o.e. (from inspection or division)	3
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11	$a = -5$ www	3	M1 for $f(2) = 0$ used and M1 for $10 + 2a = 0$ or better long division used: M1 for reaching $(8 + a)x - 6$ in working and M1 for $8 + a = 3$ equating coeffs method: M2 for obtaining $x^3 + 2x^2 + 4x + 3$ as other factor	3
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12	$f(2)$ used $2^3 + 2k + 7 = 3$ $k = -6$	M1 M1 A1	or division by $x - 2$ as far as $x^2 + 2x$ obtained correctly or remainder $3 = 2(4 + k) + 7$ o.e. 2nd M1 dep on first	3
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