

1 (i) A curve has equation $y = x^2 - 4$. Find the x -coordinates of the points on the curve where $y = 21$. [2]

(ii) The curve $y = x^2 - 4$ is translated by $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$.

Write down an equation for the translated curve. You need not simplify your answer. [2]

2

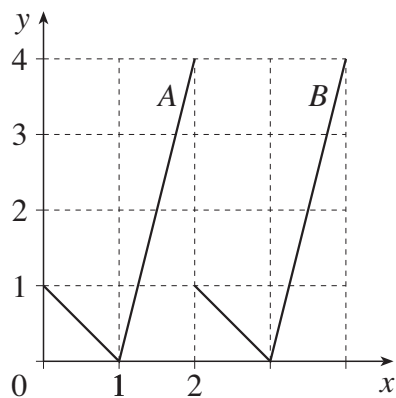


Fig. 2

Fig. 2 shows graphs A and B .

(i) State the transformation which maps graph A onto graph B . [2]

(ii) The equation of graph A is $y = f(x)$.

Which one of the following is the equation of graph B ?

$y = f(x) + 2$

$y = f(x) - 2$

$y = f(x + 2)$

$y = f(x - 2)$

$y = 2f(x)$

$y = f(x + 3)$

$y = f(x - 3)$

$y = 3f(x)$

[2]

- 3** You are given that $f(x) = (x + 3)(x - 2)(x - 5)$.
- (i)** Sketch the curve $y = f(x)$. [3]
 - (ii)** Show that $f(x)$ may be written as $x^3 - 4x^2 - 11x + 30$. [2]
 - (iii)** Describe fully the transformation that maps the graph of $y = f(x)$ onto the graph of $y = g(x)$, where $g(x) = x^3 - 4x^2 - 11x - 6$. [2]
 - (iv)** Show that $g(-1) = 0$. Hence factorise $g(x)$ completely. [5]
- 4** **(i)** You are given that $f(x) = (2x - 5)(x - 1)(x - 4)$.
- (A)** Sketch the graph of $y = f(x)$. [3]
 - (B)** Show that $f(x) = 2x^3 - 15x^2 + 33x - 20$. [2]
- (ii)** You are given that $g(x) = 2x^3 - 15x^2 + 33x - 40$.
- (A)** Show that $g(5) = 0$. [1]
 - (B)** Express $g(x)$ as the product of a linear and quadratic factor. [3]
 - (C)** Hence show that the equation $g(x) = 0$ has only one real root. [2]
- (iii)** Describe fully the transformation that maps $y = f(x)$ onto $y = g(x)$. [2]