

1		$y = 4x + 10$	B3	M1 for $y = 4x + b$ oe and M1 for $y - 6 = \text{their } a(x + 1)$ oe or for $(-1, 6)$ subst in $y = (\text{their } a)x + b$ oe or M1 for $y = ax + 10$	condone lack of brackets and eg $y = 10, x = -2.5$ or ft isw but B0, SC1 for poor notation such as $(-2.5, 10)$ with no better answers seen Throughout the scheme, note that for evaluated rational answers, unless specified otherwise, fractional or decimal equivalents are acceptable, but not triple-decker fractions etc; integer answers must be simplified to an integer
		$(0, 10)$ or ft	B1	condone $y = 10$ isw	
		$(-10/4, 0)$ oe or ft	B1	condone $x = -10/4$ isw	
			[5]		

2		$x + 3(5x - 2) = 8$ or $y = 5(8 - 3y) - 2$	M1	for subst to eliminate one variable; condone one error;	or multn or divn of one or both eqns to get a pair of coeffs the same, condoning one error appropriate addn or subtn to eliminate a variable, condoning an error in one term; if subtracting, condone eg y instead of 0 if no other errors
		$16x = 14$ or $16y = 38$	M1	for collecting terms and simplifying; condoning one error ft	
		$(7/8, 19/8)$ oe	A2	or $x = 14/16, y = 38/16$ oe isw allow A1 for each coordinate	
			[4]		

3		<p>midpt M of AB = $\left(\frac{1+6}{2}, \frac{5-1}{2}\right)$ oe isw soi</p> <p>subst of their midpt into $y = 2x - 5$ and attempting to evaluate</p> <p>all work correct and 'Yes' oe</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>condone lack of brackets; accept in the form $x = 7/2$ oe, $y = 2$ oe</p> <p>eg $2 \times$ their $3.5 - 5 =$ their result</p> <p>accept $2 = 2 \times 3.5 - 5$</p>	<p><u>alt methods</u>: allow 2nd M1 for finding correct eqn of AB as $y = -\frac{6x}{5} + \frac{31}{5}$ oe <u>and</u> attempting to solve as simult eqn with $y = 2x - 5$ for x or y or</p> <p>allow M1 for finding in unsimplified form the eqn of the line through their midpt with gradient 2 and A1 for showing it is $y = 2x - 5$, so Yes</p>
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4		<p>$y = -0.5x + 3$ oe www isw</p>	<p>3</p> <p>[3]</p>	<p>B2 for $2y = -x + 6$ oe</p> <p>or M1 for gradient = $-\frac{1}{2}$ oe seen or used</p> <p>and M1 for $y - 1 = \textit{their } m(x - 4)$</p>	<p>for 3 marks must be in form $y = ax + b$</p> <p>or M1 for $y = \textit{their } mx + c$ and $(4, 1)$ substituted</p>
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5	(i)	<p>midpt of AB = $\left(\frac{1}{2}, \frac{5}{2}\right)$ oe www</p> <p>grad AB = $\frac{4-1}{3-(-2)}$ oe</p> <p>using gradient of AB to obtain grad perp bisector</p> <p>$y - 2.5 = \frac{-5}{3}(x - 0.5)$ oe</p>	<p>B2 allow unsimplified B1 for one coordinate correct</p> <p>M1 must be obtained independently of given line; accept 3 and 5 correctly shown eg in a sketch, followed by 3/5</p> <p>M1 for rise/run = 3/5 etc</p> <p>M0 for just 3/5 with no evidence</p> <p>M1 for use of $m_1 m_2 = -1$ soi or ft their gradient AB</p> <p>M0 for just $\frac{-5}{3}$ without AB grad found</p> <p>M1 eg M1 for $y = \frac{-5}{3}x + c$ and subst of midpt; ft their gradient of perp bisector and midpt;</p> <p>M0 for just rearranging given equation</p>	<p>if working shown, should come from $\left(\frac{3+(-2)}{2}, \frac{4+1}{2}\right)$ oe</p> <p>NB B0 for x coord. = $\frac{5}{2}$, (obtained from subtraction instead of addition)</p> <p>for those who find eqn of AB first, M0 for just $\frac{y-4}{1-4} = \frac{x-3}{-2-3}$ oe, but M1 for $y-4 = \frac{1-4}{-2-3}(x-3)$ oe</p> <p>ignore their going on to find the eqn of AB after finding grad AB</p> <p>this second M1 available for starting with given line = $\frac{-5}{3}$ and obtaining grad. of AB from it</p> <p>no ft for gradient of AB used</p>
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		completion to given answer $3y + 5x = 10$, showing at least one interim step	M1	condone a slight slip if they recover quickly and general steps are correct (eg sometimes a slip in working with the c in $y = \frac{-5}{3}x + c$ - condone $3y = -5x + c$ followed by substitution and consistent working) M0 if clearly 'fudging'	NB answer given; mark process not answer; annotate if full marks not earned eg with a tick for each mark earned scores such as B2M0M0M1M1 are possible after B2, allow full marks for complete method of showing given line has gradient perp to AB (grad AB must be found independently at some stage) and passes through midpt of AB
5	(ii)	$3y + 5(4y - 21) = 10$ $(-1, 5)$ or $y = 5, x = -1$ isw	M1	or other valid strategy for eliminating one variable attempted eg $\frac{-5}{3}x + \frac{10}{3} = \frac{x}{4} + \frac{21}{4}$; condone one error	or eg $20y = 5x + 105$ and subtraction of two eqns attempted no ft from wrong perp bisector eqn, since given allow M1 for candidates who reach $y = 115/23$ and then make a worse attempt, thinking they have gone wrong
			A2	A1 for each value; if AO allow SC1 for both values correct but unsimplified fractions, eg $\left(\frac{-23}{23}, \frac{115}{23}\right)$	NB M0A0 in this part for finding E using info from (iii) that implies E is midpt of CD
			[6]		
			[3]		

5	(iii)	<p>$(x - a)^2 + (y - b)^2 = r^2$ seen or used</p> <p>$1^2 + 4^2$ oe (may be unsimplified), from clear use of A or B</p> <p>$(x + 1)^2 + (y - 5)^2 = 17$</p> <p>showing midpt of CD = (-1, 5)</p> <p>showing CE or DE = $\sqrt{17}$ oe or showing one of C and D on circle</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p>	<p>or for $(x + 1)^2 + (y - 5)^2 = k$, or ft their E, where $k > 0$</p> <p>for calculating AE or BE or their squares, or for subst coords of A or B into circle eqn to find r or r^2, ft their E;</p> <p>for eqn of circle centre E, through A and B;</p> <p>allow A1 for $r^2 = 17$ found after $(x + 1)^2 + (y - 5)^2 = r^2$ stated and second M1 clearly earned</p> <p>if $(x + 1)^2 + (y - 5)^2 = 17$ appears without clear evidence of using A or B, allow the first M1 then M0 SC1</p> <p>alt M1 for showing $CD^2 = 68$ oe</p> <p>allow to be earned earlier as an invalid attempt to find r</p>	<p>this M not earned for use of CE or DE or $\frac{1}{2}$ CD</p> <p>NB some cand's finding $AB^2 = 34$ then obtaining 17 erroneously so M0</p> <p>SC also earned if circle comes from C or D and E, but may recover and earn the second M1 later by using A or B</p>
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				[5]		

6			<p>$y = -2x + 7$ isw (0, 7) and (3.5, 0) oe or ft their $y = -2x + c$</p>	<p>2 1</p>	<p>M1 for $y - 1 = -2(x - 3)$ or $1 = -2 \times 3 + c$ oe</p>	<p>condone lack of brackets and eg $y = 7$, $x = 3.5$ or ft isw but 0 for poor notation such as (3.5, 7) and no better answers seen</p>
				[3]		

7		$4k^2 - 4 \times 1 \times 5$ or $k^2 - 5$ [< 0] oe or $[(x + k)^2 +] 5 - k^2$ [> 0] oe $-\sqrt{5} < k < \sqrt{5}$	M2 allow $=, >, \leq$ etc instead of $<$ or M1 for $b^2 - 4ac$ soi (may be in formula) or for attempt at completing square A2 may be two separate inequalities or A1 for one 'end' correct or B1 for 'endpoint' = $\sqrt{5}$ [4]	allow M2 for $2k^2 < 20, 2k^2 - 20 = 0$ etc but M1 only for just $2k^2 - 20$ ignore rest of quadratic formula ignore $\sqrt{b^2 - 4ac} < 0$ seen if $b^2 - 4ac < 0$ then used, otherwise just M1 for $\sqrt{b^2 - 4ac} < 0$ allow SC1 for $-\sqrt{10} < k < \sqrt{10}$ following at least M1 for $2k^2 - 20$ oe
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8	(i)	<p>$AB^2 = (1 - (-1))^2 + (5 - 1)^2$</p> <p>$BC^2 = (3 - (-1))^2 + (-1 - 1)^2$</p> <p>shown equal eg $AB^2 = 2^2 + 4^2 [=20]$ and $BC^2 = 4^2 + 2^2 [=20]$ with correct notation for final comparison</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>oe, or square root of this; condone poor notation re roots; condone $(1 + 1)^2$ instead of $(1 - (-1))^2$</p> <p>allow M1 for vector $AB = \begin{pmatrix} -2 \\ -4 \end{pmatrix}$, condoning poor notation, or triangle with hyp AB and lengths 2 and 4 correctly marked</p> <p>oe, or square root of this; condone poor notation re roots; condone $(3 + 1)^2$ instead of $(3 - (-1))^2$ oe</p> <p>allow M1 for vector $BC = \begin{pmatrix} 4 \\ -2 \end{pmatrix}$, condoning poor notation, or triangle with hyp BC and lengths 4 and 2 correctly marked</p> <p>or statement that AB and BC are each the hypotenuse of a right-angled triangle with sides 2 and 4 so are equal</p> <p>SC2 for just $AB^2 = 2^2 + 4^2$ and $BC^2 = 4^2 + 2^2$ (or roots of these) with no clearer earlier working; condone poor notation</p>	<p>eg A0 for AB = 20 etc</p>
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8	(ii)	<p>[grad. of AC =] $\frac{5 - (-1)}{1 - 3}$ or $\frac{6}{-2}$ oe</p> <p>[grad. of BD =] $\frac{5 - 1}{11 - (-1)}$ or $\frac{4}{12}$ oe</p> <p>showing or stating product of gradients = -1 or that one gradient is the negative reciprocal of the other oe</p>	<p>M1</p> <p>M1</p> <p>B1</p> <p>[3]</p>	<p>award at first step shown even if errors after</p> <p>eg accept $m_1 \times m_2 = -1$ or 'one gradient is negative reciprocal of the other'</p> <p>B0 for 'opposite' used instead of 'negative' or 'reciprocal'</p>	<p>if one or both of grad AC = -3 and grad BD = 1/3 seen without better working for both gradients, award one M1 only. For M1M1 it must be clear that they are obtained independently</p> <p>may be earned independently of correct gradients, but for all 3 marks to be earned the work must be fully correct</p>
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8	(iii)	<p>midpoint E of AC = (2, 2) www</p> <p>eqn BD is $y = \frac{1}{3}x + \frac{4}{3}$ oe</p> <p>eqn AC is $y = -3x + 8$ oe</p> <p>using both lines and obtaining intersection E is (2, 2) (NB must be independently obtained from midpt of AC)</p> <p>midpoint F of BD = (5,3)</p>	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>[5]</p>	<p>condone missing brackets for both B1s</p> <p>accept any correct form isw or correct ft their gradients or their midpt F of BD</p> <p>this mark will often be gained on the first line of their working for BD</p> <p>accept any correct form isw or correct ft their gradients or their midpt E of AC</p> <p>this mark will often be gained on the first line of their working for AC</p> <p>[see appendix for alternative methods instead showing E is on BD for this M1]</p> <p>this mark is often earned earlier</p> <p>see the appendix for some common alternative methods for this question; for all methods, for A1 to be earned, all work for the 5 marks must be correct</p>	<p>0 for $((5+ -1)/2, (1+3)/2) = (2, 2)$</p> <p>may be earned using (2, 2) but then must independently show that B or D or (5, 3) is on this line to be eligible for A1</p> <p>if equation(s) of lines are seen in part ii, allow the M1s if seen/used in this part</p> <p>[see appendix for alternative ways of gaining these last two marks in different methods]</p> <p>for all methods show annotations M1 B1 etc then omission mark or A0 if that mark has not been earned</p>
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9		<p>grad = $-1/5$ oe</p> <p>$y - 6 = \text{their } m(x - 1)$ or $6 = \text{their } m[\times 1] + c$</p> <p>$y = -0.2x + 6.2$ oe isw</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>terms collected, with y as subject</p> <p>or for $a = -0.2, b = 6.2$ oe</p>	<p>allow embedded eg $5 \times -\frac{1}{5} = -1$</p> <p>if first M1 not earned, allow second M1 for $y - 6 = k(x - 1)$ oe, k any number except 0 and 1</p> <p>allow A1 for $c = 6.2$ oe if $y = -0.2x + c$ oe already seen</p> <p>condone $y = \frac{-x + 31}{5}$ for A1</p>
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