

Question		Answer	Marks	Guidance
1	(i)	$y = (x + 5)(x + 2)(2x - 3)$ or $y = 2(x + 5)(x + 2)(x - 3/2)$	2 [2]	<p>M1 for $y = (x + 5)(x + 2)(x - 3/2)$ or $(x + 5)(x + 2)(2x - 3)$ with no equation or $(x + 5)(x + 2)(2x - 3) = 0$ but M0 for $y = (x + 5)(x + 2)(2x - 3) - 30$ or $(x + 5)(x + 2)(2x - 3) = 30$ etc</p> <p>allow 'f(x) =' instead of 'y = ' ignore further work towards (ii) but do not award marks for (i) in (ii)</p>
1	(ii)	<p>correct expansion of a pair of their linear two-term factors ft isw</p> <p>correct expansion of the correct linear and quadratic factors and completion to given answer $y = 2x^3 + 11x^2 - x - 30$</p>	M1 M1 [2]	<p>ft their factors from (i); need not be simplified; may be seen in a grid</p> <p>M1 must be working for this step before given answer or for direct expansion of all three factors, allow M2 for $2x^3 + 10x^2 + 4x^2 - 3x^2 + 20x - 15x - 6x - 30$ oe (M1 if one error) or M1M0 for a correct direct expansion of $(x + 5)(x + 2)(x - 3/2)$</p> <p>condone lack of brackets if used as if they were there</p> <p>allow only first M1 for expansion if their (i) has an extra -30 etc do not award 2nd mark if only had $(x - 3/2)$ in (i) and suddenly doubles RHS at this stage condone omission of 'y =' or inclusion of '= 0' for this second mark (some cand have already lost a mark for that in (i)) allow marks if this work has been done in part (i) – mark the copy of part (i) that appears below the image for part (ii)</p>

Question		Answer	Marks	Guidance
1	(iii)	<p>ruled line drawn through $(-2, 0)$ and $(0, 10)$ and long enough to intersect curve at least twice</p> <p>-5.3 to -5.4 and 1.8 to 1.9</p>	<p>B1</p> <p>B2</p> <p>[3]</p>	<p>tolerance half a small square on grid at $(-2, 0)$ and $(0, 10)$</p> <p>B1 for one correct ignore the solution -2 but allow B1 for both values correct but one extra or for wrong 'coordinate' form such as $(1.8, -5.3)$</p> <p>insert BP on spare copy of graph if not used, to indicate seen – this is included as part of image, so scroll down to see it accept in coordinate form ignoring any y coordinates given;</p>
1	(iv)	<p>$2x^3 + 11x^2 - x - 30 = 5x + 10$</p> <p>$2x^3 + 11x^2 - 6x - 40 [= 0]$</p> <p>division by $(x + 2)$ and correctly obtaining $2x^2 + x - 20$</p> <p>substitution into quadratic formula or for completing the square used as far as</p> <p>$x + \frac{7}{4} = \frac{209}{16}$ oe</p> <p>$[x =] \frac{-7 \pm \sqrt{209}}{4}$ oe isw</p>	<p>M1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[5]</p>	<p>for equating curve and line; correct eqns only</p> <p>for rearrangement to zero, condoning one error</p> <p>or showing that $(x + 2)(2x^2 + 7x - 20) = 2x^3 + 1x^2 - 6x - 40$, with supporting working</p> <p>condone one error eg a used as 1 not 2, or one error in the formula, using given $2x^2 + 7x - 20 = 0$</p> <p>dependent only on 4th M1</p> <p>annotate this question if partially correct</p>

2	(i)	$y = 2x + 3$ drawn accurately (-1.6 to -1.7, -0.2 to -0.3) (2.1 to 2.2, 7.2 to 7.4)	M1 B1 B1 [3]	at least as far as intersecting curve twice intersections may be in form $x = \dots, y = \dots$	ruled straight line and within 2mm of (2, 7) and (-1, 1) if marking by parts and you see work relevant to (ii), put a yellow line here and in (ii) to alert you to look
2	(ii)	$\frac{1}{x-2} = 2x + 3$ $1 = (2x + 3)(x - 2)$ $1 = 2x^2 - x - 6$ oe $\frac{1 \pm \sqrt{1^2 - 4 \times 2 \times -7}}{2 \times 2}$ oe $\frac{1 \pm \sqrt{57}}{4}$ isw	M1 M1 A1 M1 A1 [5]	or attempt at elimination of x by rearrangement and substitution condone lack of brackets for correct expansion; need not be simplified; NB A0 for $2x^2 - x - 7 = 0$ without expansion seen [given answer] use of formula or completing square on given equation, with at most one error is eg coordinates; after completing square, accept $\frac{1}{4} \pm \sqrt{\frac{57}{16}}$ or better	may be seen in (i) – allow marks; the part (i) work appears at the foot of the image for (ii) so show marks there rather than in (i) implies first M1 if that step not seen implies second M1 if that step not seen after $\frac{1}{x-2} = 2x + 3$ seen completing square attempt must reach at least [2] $(x - a)^2 = b$ or $(2x - c)^2 = d$ stage oe with at most one error

2	(iii)	$\frac{1}{x-2} = -x + k$ and attempt at rearrangement $x^2 - (k+2)x + 2k + 1 [= 0]$ $b^2 - 4ac = 0$ oe seen or used $[k =] 0$ or 4 as final answer, both required	M1 M1 M1 A1 [4]	for simplifying and rearranging to zero; condone one error; collection of x terms with bracket not required SC1 for 0 and 4 found if 3 rd M1 not earned (may or may not have earned first two Ms)	eg M1 bod for $x^2 - (k+2)x + 2k$ or M1 for $x^2 - 2kx + 2k + 1 [= 0]$ = 0 may not be seen, but may be implied by their final values of k eg obtained graphically or using calculus and/or final answer given as a range
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3	(i)	<p>(-1, 6) (0,1) (1,-2) (2,-3) (3,-2) (4, 1) (5,6) seen plotted</p> <p>smooth curve through all 7 points</p> <p>(0.3 to 0.5, -0.3 to -0.5) and (2.5 to 2.7, -2.5 to -2.7) and (4, 1)</p>	<p>B2</p> <p>B1 dep</p> <p>B2</p> <p>[5]</p>	<p>or for a curve within 2 mm of these points; B1 for 3 correct plots or for at least 3 of the pairs of values seen eg in table</p> <p>dep on correct points; tolerance 2 mm;</p> <p>may be given in form $x = \dots, y = \dots$ B1 for two intersections correct or for all the x values given correctly</p>	<p>use overlay; scroll down to spare copy of graph to see if used [or click 'fit height']</p> <p>also allow B1 for $(2 \pm \sqrt{3}, 0)$ and $(2, -3)$ seen or plotted and curve not through other correct points</p> <p>condone some feathering/ doubling (deleted work still may show in scans); curve should not be flat-bottomed or go to a point at min. or curve back in at top;</p>
3	(ii)	$\frac{1}{x-3} = x^2 - 4x + 1$ $1 = (x-3)(x^2 - 4x + 1)$ <p>at least one further correct interim step with '=1' or '=0', as appropriate, leading to given answer, which must be stated correctly</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>condone omission of brackets only if used correctly afterwards, with at most one error;</p> <p>there may also be a previous step of expansion of terms without an equation, eg in grid</p> <p>if M0, allow SC1 for correct division of given cubic by quadratic to gain $(x-3)$ with remainder -1, or vice-versa</p>	<p>condone omission of '=1' for this M1 only if it reappears</p> <p>allow for terms expanded correctly with at most one error</p> <p>NB mark method not answer - given answer is $x^3 - 7x^2 + 13x - 4 = 0$</p>

Question		er	Marks	Guidance	
3	(iii)	quadratic factor is $x^2 - 3x + 1$	B2	found by division or inspection; allow M1 for division by $x - 4$ as far as $x^3 - 4x^2$ in the working, or for inspection with two terms correct	
		substitution into quadratic formula or for completing the square used as far as $(x - \frac{3}{2})^2 = \frac{5}{4}$	M1	condone one error	no ft from a wrong 'factor';
		$\frac{3 \pm \sqrt{5}}{2}$ oe	A2	A1 if one error in final numerical expression, but only if roots are real	isw factors
			[5]		

4	(i) $x + 4x^2 + 24x + 31 = 10$ oe $4x^2 + 25x + 21 [= 0]$ $(4x + 21)(x + 1)$ $x = -1$ or $-21/4$ oe isw $y = 11$ or $61/4$ oe isw	M1 M1 M1 A1 A1	for subst of x or y or subtraction to eliminate variable; condone one error; for collection of terms and rearrangement to zero; condone one error; for factors giving at least two terms of their quadratic correct or for subst into formula with no more than two errors [dependent on attempt to rearrange to zero]; or A1 for $(-1, 11)$ and A1 for $(-21/4, 61/4)$ oe	or $4y^2 - 105y + 671 [= 0]$; eg condone spurious $y = 4x^2 + 25x + 21$ as one error (and then count as eligible for 3 rd M1); or $(y - 11)(4y - 61)$; [for full use of completing square with no more than two errors allow 2nd and 3rd M1 s simultaneously]; from formula: accept $x = -1$ or $-42/8$ oe isw
4	(ii) $4(x + 3)^2 - 5$ isw	4	B1 for $a = 4$, B1 for $b = 3$, B2 for $c = -5$ or M1 for $31 - 4 \times$ their b^2 soi or for $-5/4$ or for $31/4 -$ their b^2 soi	eg an answer of $(x + 3)^2 - 5/4$ earns B0 B1 M1 ; $1(2x + 6)^2 - 5$ earns B0 B0 B2 ; $4($ earns first B1 ; condone omission of square symbol
4	(iii)(A) $x = -3$ or ft ($-$ their b) from (ii)	1		0 for just -3 or ft; 0 for $x = -3, y = -5$ or ft
4	(iii)(B) -5 or ft their c from (ii)	1	allow $y = -5$ or ft	0 for just $(-3, -5)$; bod 1 for $x = -3$ stated then $y = -5$ or ft

5 (i)	$(2x - 3)(x + 1)$ $x = 3/2$ and -1 obtained	M2 B1	M1 for factors with one sign error or giving two terms correct allow M1 for $2(x - 1.5)(x + 1)$ with no better factors seen or ft their factors
5 (ii)	graph of quadratic the correct way up and crossing both axes crossing x -axis only at $3/2$ and -1 or ft from their roots in (i), or their factors if roots not given crossing y -axis at -3	B1 B1 B1	for $x = 3/2$ condone 1 and 2 marked on axis and crossing roughly halfway between; intns must be shown labelled or worked out nearby
5 (iii)	use of $b^2 - 4ac$ with numbers subst (condone one error in substitution) (may be in quadratic formula) $25 - 40 < 0$ or -15 obtained	M1 A1	may be in formula or $(x - 2.5)^2 = 6.25 - 10$ or $(x - 2.5)^2 + 3.75 = 0$ oe (condone one error) or $\sqrt{-15}$ seen in formula or $(x - 2.5)^2 = -3.75$ oe or $x = 2.5 \pm \sqrt{-3.75}$ oe

5 (iv)	$2x^2 - x - 3 = x^2 - 5x + 10$ o.e. $x^2 + 4x - 13 [= 0]$ use of quad. formula on resulting eqn (do not allow for original quadratics used) $-2 \pm \sqrt{17}$ cao	M1 M1 M1 A1	attempt at eliminating y by subst or subtraction or $(x + 2)^2 = 17$; for rearranging to form $ax^2 + bx + c [= 0]$ or to completing square form condone one error for each of 2 nd and 3 rd M1s or $x + 2 = \pm\sqrt{17}$ o.e. 2 nd and 3 rd M1s may be earned for good attempt at completing square as far as roots obtained
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6		$y = 2x + 3$ drawn on graph $x = 0.2$ to 0.4 and -1.7 to -1.9	M1 A2	1 each; condone coords; must have line drawn	3
	ii	$1 = 2x^2 + 3x$ $2x^2 + 3x - 1 [= 0]$	M1 M1	for multiplying by x correctly for correctly rearranging to zero (may be earned first) or suitable step re completing square if they go on	
		attempt at formula or completing square $x = \frac{-3 \pm \sqrt{17}}{4}$	M1 A2	ft, but no ft for factorising A1 for one soln	5
	iii	branch through $(1,3)$, branch through $(-1,1)$, approaching $y = 2$ from below	1	and approaching $y = 2$ from above	
iv	-1 and $\frac{1}{2}$ or ft intersection of their curve and line [tolerance 1 mm]	1 2	and extending below x axis 1 each; may be found algebraically; ignore y coords.	2 2	