

| Question | | | Answer | Marks | Guidance |
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| 1 | | | $[r =] \sqrt{\frac{A}{\pi(x+y)}}$ or $[r =] \sqrt{\frac{A}{\pi x + \pi y}}$ as final answer | 2 [2] | square root symbol must extend below fraction line; accept to power $\frac{1}{2}$ with appropriate brackets M1 for a triple decker fraction or for $r^2 = \frac{A}{\pi(x+y)}$ or for $[r =] \pm \sqrt{\frac{A}{\pi(x+y)}}$ or for their final answer for r ft their r^2 condone missing end bracket in denominator eg M1 for $[r =] \sqrt{\frac{A}{\pi(x+y)}}$ |

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| 2 | (i) | | $9x^2 = h^2 + 4x^2 + 4x + 1$ and completion to given answer, $h^2 = 5x^2 - 4x - 1$ | B1 B1 [2] | for a correct Pythagoras statement for this triangle, in terms of x , with correct brackets for correct expansion, with brackets or correct signs; must complete to the given answer with no errors in any interim working may follow $3x^2 = h^2 + (2x + 1)^2$ oe for B0 B1 condone another letter instead of h for one mark but not both unless recovered at some point eg B1 for $h^2 = 9x^2 - (4x^2 + 4x + 1)$ and completion to correct answer but B0 for $h^2 = 9x^2 - 4x^2 + 4x + 1$ |
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| 3 | (i) | $3x^2 + 12x + 13 = 2x + k$ $3x^2 + 10x + 13 - k [= 0]$ $b^2 - 4ac > 0$ oe soi $100 - 4 \times 3 \times (13 - k) (> 0)$ oe $k > 14/3$ oe | M1 M1 M1 M1 A1 [5] | oe eg M1 for $3x^2 + 10x + 13 = k$ for rearranging to 0; condone one error in adding/subtracting; but M0 for $3x^2 + 10x + 13 = k$ or $3x^2 + 10x + 13 - k = y$ may be earned near end with correct inequality sign used there for correct substitution ft into $b^2 - 4ac$, dep on second M1 earned; brackets / signs must be correct accept $k > 56/12$ or better, isw incorrect conversion of fraction but not wrong use of inequalities if A0, allow B1 for $56/12$ oe obtained with equality or wrong inequality (ie 3 rd M1 has not been earned) | condone $3x^2 + 10x + 13 - k = y$ for this M1 $3x^2 + 10x + 13 - k [= 0]$ will also earn the first M1 if a separate statement has not already done so allow ' $b^2 - 4ac$ is positive' oe; 0 for just 'discriminant > 0 ' unless implied by later work can be earned with equality or wrong inequality, or in formula M0 for trials of values of k in $b^2 - 4ac$ |
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| 3 | (ii) | | $3(x + 2)^2 + 1$ www as final answer y-minimum = 1 [hence curve is above x-axis] | B4 B1 [5] | B1 for $a = 3$ and B1 for $b = 2$ and B2 for $c = 1$ or M1 for $13 - 3 \times$ their b^2 or for $13/3 -$ their b^2 or B3 for $3 \left[(x + 2)^2 + \frac{1}{3} \right]$ Stating min pt is $(-2, 1)$ is sufft allow ft if their $c > 0$ B0 for only showing that discriminant is negative oe; need also to justify that it is all above not all below x -axis B0 for stating min point = 1 or ft | condone omission of square symbol; ignore equating to zero in working or answer must be done in this part; ignore wrong x -coordinate |
| 3 | (iii) | | 5 cao | B2 [2] | M1 for substitution of their $(-2, 1)$ in $y = 2x + k$ | allow M1 ft their $3(x + 2)^2 + 1$; or use of $(-2, 1)$ found using calculus; M0 if they use an incorrect minimum point inconsistent with their completed square form |

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| 4 | | $3a + 12 [= ac + 5f]$ | M1 | for expanding brackets correctly | annotate this question if partially correct ft only if two a terms ft only if two a terms, needing factorising may be earned before 2 nd M1 |
| | | $3a - ac = 5f - 12$ or ft | M1 | for collecting a terms on one side, remaining terms on other | |
| | | $a(3 - c) = 5f - 12$ or ft | M1 | for factorising a terms; may be implied by final answer | |
| | | $[a =] \frac{5f - 12}{3 - c}$ oe or ft as final answer | M1 | for division by their two-term factor; for all 4 marks to be earned, work must be fully correct | |
| | | | [4] | | |

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| 5 | | substitution to eliminate one variable | M1 | or multiplication to make one pair of coefficients the same; condone one error in either method | independent of first M1 |
| | | simplification to $ax = b$ or $ax - b = 0$ form, or equivalent for y | M1 | or appropriate subtraction / addition; condone one error in either method | |
| | | $(0.7, 0.1)$ oe or $x = 0.7, y = 0.1$ oe isw | A2 | A1 each | |
| | | | [4] | | |

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| 6 | | $3(x-2)^2 - 7$ isw or $a = 3, b = 2, c = 7$ www -7 or ft | 4 B1 [5] | B1 each for $a = 3, b = 2$ oe and B2 for $c = 7$ oe or M1 for $[-]\frac{7}{3}$ or for $5 - \text{their } a(\text{their } b)^2$ or for $\frac{5}{3} - (\text{their } b)^2$ soi B0 for $(2, -7)$ | condone omission of square symbol; ignore '= 0' may be implied by their answer may be obtained by starting again eg with calculus |
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| 7 | | $4x^4y^{-3}$ or $\frac{4x^4}{y^3}$ as final answer | 3 [3] | B1 each 'term'; or M1 for numerator = $64x^{15}y^3$ and M1 for denominator = $16x^{11}y^6$ | B0 if obtained fortuitously mark B scheme or M scheme to advantage of candidate, but not a mixture of both schemes |
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| 8 | | $4 + 2k + c = 0$ or $2^2 + 2k + c = 0$ $9 - 3k + c = 35$ correct method to eliminate one variable from their eqns $k = -6, c = 8$ or $[x^2 + kx + c =] (x - 2)(x - a)$ $-5 \times (-3 - a) = 35$ oe $a = 4$ $k = -6, c = 8$ | B1 B1 M1 A1 or M1 M1 A1 A1 [4] | may be rearranged may be rearranged; the $(-3)^2$ must be evaluated / used as 9 eg subtraction or substitution for c ; condone one error from fully correct method, allowing recovery from slips or or $(x - 2)(x + b)$ | condone -3^2 seen if used as 9 M0 for addition of eqns unless also multiplied appropriately if no errors and no method seen, allow correct answers to imply M1 provided B1B1 has been earned |
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| 9 | | $5c + 9t = 2ac + at$ | M1 | for correct expansion of brackets | <p>for each M, ft previous errors if their eqn is of similar difficulty;</p> <p>may be earned before t terms collected</p> <p>treat as MR if t is the subject, with a penalty of 1 mark from those gained, marking similarly</p> |
| | | $5c - 2ac = at - 9t$ oe | M1 | for correct collection of terms, ft eg after M0 for $5c + 9t = 2ac + t$ allow this M1 for $5c - 2ac = -8t$ oe | |
| | | $c(5 - 2a) = at - 9t$ oe | M1 | for correctly factorising, ft; must be $c \times$ a two-term factor | |
| | | $[c =] \frac{at - 9t}{5 - 2a}$ or $\frac{t(a - 9)}{5 - 2a}$ oe as final answer | M1 | for correct division, ft their two-term factor | |
| | | | [4] | | |

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| 10 | | $\frac{x-3}{x+2}$ or $1 - \frac{5}{x+2}$ as final answer www | 3 | B2 for correct answer seen and then spoilt M1 for $(x+3)(x-3)$ and M1 for $(x+2)(x+3)$ | |
| | | | [3] | | |

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| 11 | | $4h + ha^2 = 9a - 5$ $h(4 + a^2) = 9a - 5$ $[h =] \frac{9a - 5}{4 + a^2} \text{ oe as final answer}$ | <p>M1</p> <p>M1</p> <p>M1</p> <p>[3]</p> | <p>correctly collecting h terms on one side, remaining terms on other</p> <p>for factorising, ft eg sign error</p> <p>for division by their factor; ft only for equiv difficulty</p> | <p>M0 if seen and spoilt, eg by incorrect 'cancelling'</p> |
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