

## Core 1 Basic Algebra Questions – Mainly Quadratics

- 3 (a) (i) Express  $x^2 - 4x + 9$  in the form  $(x - p)^2 + q$ , where  $p$  and  $q$  are integers. *(2 marks)*
- (ii) Hence, or otherwise, state the coordinates of the minimum point of the curve with equation  $y = x^2 - 4x + 9$ . *(2 marks)*
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- 4 The quadratic equation  $x^2 + (m + 4)x + (4m + 1) = 0$ , where  $m$  is a constant, has equal roots.
- (a) Show that  $m^2 - 8m + 12 = 0$ . *(3 marks)*
- (b) Hence find the possible values of  $m$ . *(2 marks)*
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- 2 (a) Express  $x^2 + 8x + 19$  in the form  $(x + p)^2 + q$ , where  $p$  and  $q$  are integers. *(2 marks)*
- (b) Hence, or otherwise, show that the equation  $x^2 + 8x + 19 = 0$  has no real solutions. *(2 marks)*
- (c) Sketch the graph of  $y = x^2 + 8x + 19$ , stating the coordinates of the minimum point and the point where the graph crosses the  $y$ -axis. *(3 marks)*
- (d) Describe geometrically the transformation that maps the graph of  $y = x^2$  onto the graph of  $y = x^2 + 8x + 19$ . *(3 marks)*
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- (ii) Find the values of  $k$  for which the equation

$$x^2 - 2(k + 1)x + 2k^2 - 7 = 0$$

has equal roots. *(4 marks)*

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- 7 The quadratic equation  $(k + 1)x^2 + 12x + (k - 4) = 0$  has real roots.
- (a) Show that  $k^2 - 3k - 40 \leq 0$ . *(3 marks)*
- (b) Hence find the possible values of  $k$ . *(4 marks)*
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- 3 (a) (i) Express  $x^2 + 10x + 19$  in the form  $(x + p)^2 + q$ , where  $p$  and  $q$  are integers. *(2 marks)*
- (ii) Write down the coordinates of the vertex (minimum point) of the curve with equation  $y = x^2 + 10x + 19$ . *(2 marks)*
- (iii) Write down the equation of the line of symmetry of the curve  $y = x^2 + 10x + 19$ . *(1 mark)*
- (iv) Describe geometrically the transformation that maps the graph of  $y = x^2$  onto the graph of  $y = x^2 + 10x + 19$ . *(3 marks)*
- (b) Determine the coordinates of the points of intersection of the line  $y = x + 11$  and the curve  $y = x^2 + 10x + 19$ . *(4 marks)*
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7 The quadratic equation

$$(2k - 3)x^2 + 2x + (k - 1) = 0$$

where  $k$  is a constant, has real roots.

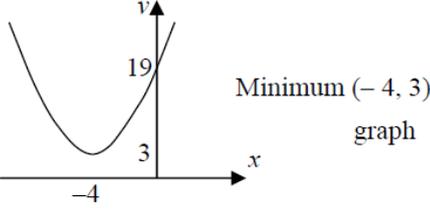
- (a) Show that  $2k^2 - 5k + 2 \leq 0$ . *(3 marks)*
- (b) (i) Factorise  $2k^2 - 5k + 2$ . *(1 mark)*
- (ii) Hence, or otherwise, solve the quadratic inequality

$$2k^2 - 5k + 2 \leq 0 \quad \text{span style="float: right;">*(3 marks)*$$

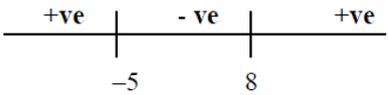
## Core 1 Basic Algebra Answers – Mainly Quadratics

<b>3(a)(i)</b>	$(x-2)^2 + 5$	B1 B1	2	p = 2 q = 5
<b>(ii)</b>	Minimum point (2, 5) or x = 2, y = 5	B2✓	2	B1 for each coordinate correct or ft <b>Alt method</b> M1, A1 sketch, differentiation

<b>4(a)</b>	$(m+4)^2 = m^2 + 8m + 16$ $b^2 - 4ac = (m+4)^2 - 4(4m+1) = 0$ $m^2 + 8m + 16 - 16m - 4 = 0$ $\Rightarrow m^2 - 8m + 12 = 0$	B1 M1 A1	3	Condone $4m + 4m$ $b^2 - 4ac$ (attempted and involving m's and no x's) or $b^2 - 4ac = 0$ stated <b>AG</b> (be convinced – all working correct = 0 appearing more than right at the end)
<b>(b)</b>	$(m-2)(m-6) = 0$ $m = 2, m = 6$	M1 A1	2	Attempt at factors or quadratic formula <b>SC B1</b> for 2 or 6 only without working
<b>Total</b>			<b>5</b>	

<b>2(a)</b>	$(x+4)^2 + 3$	B1 B1	2	p = 4 q = 3
<b>(b)</b>	$(x+4)^2 = -3$ or “their” $(x+p)^2 = -q$ No real square root of -3	M1 A1	2	Or discriminant = $64 - 76$ Disc < 0 so no real roots (all correct figs)
<b>(c)</b>		B1✓ B1 B1	3	ft their -p and q (or correct) Parabola (vertex roughly as shown) Crossing at y = 19 marked or (0, 19) stated
<b>(d)</b>	Translation (and no additional transf n) through $\begin{bmatrix} -4 \\ 3 \end{bmatrix}$	E1 M1 A1	3	Not shift, move, transformation, etc One component correct eg 3 units up All correct – if not vector – must say 4 units in negative x- direction, to left etc
<b>Total</b>			<b>10</b>	

<b>(ii)</b>	$4(k+1)^2 - 4(2k^2 - 7)$ $4k^2 - 8k - 32 = 0$ or $k^2 - 2k - 8 = 0$ $(k-4)(k+2) = 0$ $k = -2, k = 4$	M1 A1 m1 A1	4	“ $b^2 - 4ac$ ” in terms of k (either term correct) $b^2 - 4ac = 0$ correct quadratic equation in k Attempt to factorise, solve equation SC B1, B1 for -2, 4 (if M0 scored)
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7(a)	$b^2 - 4ac = 144 - 4(k+1)(k-4)$	M1	3	Clear attempt at $b^2 - 4ac$ Condone slip in one term of expression
	Real roots when $b^2 - 4ac \geq 0$ $36 - (k^2 - 3k - 4) \geq 0$ $\Rightarrow k^2 - 3k - 40 \leq 0$	B1 A1		
(b)	$(k-8)(k+5)$ Critical points 8 and -5	M1 A1	4	Factors attempt or formula  
	Sketch or sign diagram <b>correct</b> , must have 8 and -5 $-5 \leq k \leq 8$	M1 A1		
	A0 for $-5 < k < 8$ or two separate inequalities unless word AND used			
<b>Total</b>			<b>7</b>	

3(a)(i)	$(x+5)^2$ -6	B1 B1	2	$p = 5$ $q = -6$
	(ii) $x_{\text{vertex}} = -5$ (or their $-p$ ) $y_{\text{vertex}} = -6$ (or their $q$ )	B1✓ B1✓		
(iii)	$x = -5$	B1	1	may differentiate but must have $x = -5$ and $y = -6$ . Vertex $(-5, -6)$  and NO other transformation stated either component correct M1, A1 independent of E mark
(iv)	Translation (not shift, move etc) through $\begin{bmatrix} -5 \\ -6 \end{bmatrix}$ (or 5 left, 6 down)	E1 M1 A1	3	
(b)	$x+11 = x^2 + 10x + 19$ $\Rightarrow x^2 + 9x + 8 = 0$ or $y^2 - 13y + 30 = 0$ $(x+8)(x+1) = 0$ or $(y-3)(y-10) = 0$ $\left. \begin{array}{l} x = -1 \\ y = 10 \end{array} \right\}$ or $\left. \begin{array}{l} x = -8 \\ y = 3 \end{array} \right\}$	M1 m1 A1 A1	4	
<b>Total</b>			<b>12</b>	quadratic with all terms on one side of equation  attempt at formula (1 slip) or to factorise both $x$ values correct both $y$ values correct and linked SC $(-1, 10)$ B2, $(-8, 3)$ B2 no working

7(a)	$b^2 - 4ac = 4 - 4(k-1)(2k-3)$ Real roots when $b^2 - 4ac \geq 0$ $4 - 4(2k^2 - 5k + 3) \geq 0$ $\Rightarrow -2k^2 + 5k - 3 + 1 \geq 0$ $\Rightarrow 2k^2 - 5k + 2 \leq 0$	M1 E1  A1	3	(or seen in formula) condone one slip must involve $f(k) \geq 0$ (usually M1 must be earned)  at least one step of working justifying $\leq 0$ AG
(b)(i)	$(2k-1)(k-2)$	B1	1	
(ii)	(Critical values) $\frac{1}{2}$ and 2  $\Rightarrow 0.5 \leq k \leq 2$	B1✓  M1 A1	3	ft their factors or correct values seen on diagram, sketch or inequality or stated  use of sketch / sign diagram M1A0 for $0.5 < k < 2$ or $k \geq 0.5, k \leq 2$
<b>Total</b>			7	