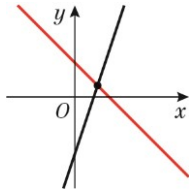


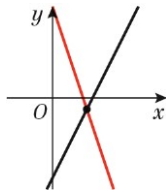
Exercise 3C

1 a i



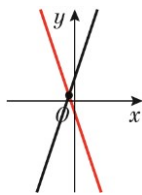
ii (2, 1)

b i



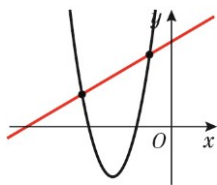
ii (3, -1)

c i Rearrange $3x + y + 1 = 0$ to give:
 $y = -3x - 1$



ii (-0.5, 0.5)

2 a Rearrange $2y = 2x + 11$ to give $y = x + \frac{11}{2}$



b (-1.5, 4) and (3.5, 9)

c Substitute values for x into each equation.

When $x = -1.5$:

$$2y = 2(-1.5) + 11 = 8, y = 4.$$

When $x = 3.5$:

$$2y = 2(3.5) + 11 = 18, y = 9.$$

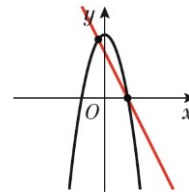
When $x = -1.5$:

$$y = 2(-1.5)^2 - 3(-1.5) - 5 = 4.5 + 4.5 - 5 = 4$$

When $x = 3.5$:

$$y = 2(3.5)^2 - 3(3.5) - 5 = 24.5 - 10.5 - 5 = 9$$

3 a $y = 9 - x^2$
 $y = -2x + 6$



b (-1, 8) and (3, 0)

c Substitute each value of x and y into each equation:

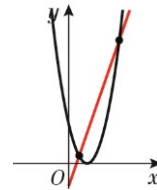
$$(-1)^2 + 8 = 1 + 8 = 9$$

$$2(-1) + 8 = -2 + 8 = 6$$

$$(3)^2 + 0 = 9$$

$$2(3) + 0 = 6$$

4 a $y = (x - 2)^2$
 $0 = (x - 2)^2$
 $x = 2$
When $x = 0$, $y = 4$



b $(x - 2)^2 = 3x - 2$
 $x^2 - 4x + 4 - 3x + 2 = 0$
 $x^2 - 7x + 6 = 0$
 $(x - 6)(x - 1) = 0$

$$x = 6 \text{ or } x = 1$$

$$\text{When } x = 1, y = 1$$

$$\text{When } x = 6, y = 16$$

(1, 1) and (6, 16) are the points of intersection.

5 $y = x - 4$

Substitute into $y^2 = 2x^2 - 17$:

$$(x - 4)^2 = 2x^2 - 17$$

$$x^2 - 8x + 16 = 2x^2 - 17$$

$$0 = x^2 + 8x - 33$$

$$0 = (x + 11)(x - 3)$$

$$x = -11 \text{ or } x = 3$$

- 5** Substitute into $y = x - 4$:
 When $x = -11$, $y = -11 - 4 = -15$
 When $x = 3$, $y = 3 - 4 = -1$
 Intersection points:
 $(-11, -15)$ and $(3, -1)$
- 6** $y = 3x - 1$
 Substitute into $y^2 - xy = 15$:
 $(3x - 1)^2 - x(3x - 1) = 15$
 $9x^2 - 6x + 1 - 3x^2 + x = 15$
 $6x^2 - 5x - 14 = 0$
 $(6x + 7)(x - 2) = 0$
 $x = -\frac{7}{6}$ or $x = 2$
 Substitute into $y = 3x - 1$:
 When $x = -\frac{7}{6}$, $y = -\frac{21}{6} - 1 = -\frac{9}{2}$
 When $x = 2$, $y = 6 - 1 = 5$
 Intersection points:
 $(-\frac{7}{6}, -\frac{9}{2})$ and $(2, 5)$
- 7 a** $6x^2 + 3x - 7 = 2x + 8$
 $6x^2 + x - 15 = 0$
 Using the discriminant:
 $b^2 - 4ac = (1)^2 - 4(6)(-15) = 361$
 $361 > 0$, therefore there are two points of intersection.
- b** $4x^2 - 18x + 40 = 10x - 9$
 $4x^2 - 28x + 49 = 0$
 Using the discriminant:
 $b^2 - 4ac = (-28)^2 - 4(4)(49) = 0$
 Thus, there is one point of intersection.
- c** Rearrange $7x + y + 3 = 0$ to give:
 $y = -7x - 3$
 $3x^2 - 2x + 4 = -7x - 3$
 $3x^2 + 5x + 7 = 0$
 Using the discriminant:
 $b^2 - 4ac = 5^2 - 4(3)(7) = -59$
 $-59 < 0$, therefore there are no points of intersection.
- 8 a** Rearrange $2x - y = 1$ and then substitute into $x^2 + 4ky + 5k = 0$:
 $y = 2x - 1$
 $x^2 + 4k(2x - 1) + 5k = 0$
 $x^2 + 8kx - 4k + 5k = 0$
 $x^2 + 8kx + k = 0$
- b** Using the discriminant,
 $b^2 - 4ac = 0$
 $(8k)^2 - 4(1)(k) = 0$
 $64k^2 - 4k = 0$
 $4k(16k - 1) = 0$
 $k = 0$ or $k = \frac{1}{16}$
 As k is a non-zero constant, $k = \frac{1}{16}$
- c** $x^2 + 8(\frac{1}{16})x + \frac{1}{16} = 0$
 $16x^2 + 8x + 1 = 0$
 $(4x + 1)^2 = 0$
 $x = -\frac{1}{4}$, $y = -\frac{3}{2}$