

Exercise 1D

$$1 \text{ a } x^3 \div x^{-2} = x^{3-(-2)} \\ = x^5$$

$$\text{b } x^5 \div x^7 = x^{5-7} \\ = x^{-2}$$

$$\text{c } x^{\frac{3}{2}} \times x^{\frac{5}{2}} = x^{\frac{3+5}{2}} \\ = x^4$$

$$\text{d } (x^2)^{\frac{3}{2}} = x^{2 \times \frac{3}{2}} \\ = x^3$$

$$\text{e } (x^3)^{\frac{5}{3}} = x^{3 \times \frac{5}{3}} \\ = x^5$$

$$\text{f } 3x^{0.5} \times 4x^{-0.5} = 12x^{0.5+(-0.5)} \\ = 12x^0 \\ = 12$$

$$\text{g } 9x^{\frac{2}{3}} \div 3x^{\frac{1}{6}} = 3x^{\frac{2}{3}-\frac{1}{6}} \\ = 3x^{\frac{1}{2}}$$

$$\text{h } 5x^{\frac{7}{5}} \div x^{\frac{2}{5}} = 5x^{\frac{7}{5}-\frac{2}{5}} \\ = 5x$$

$$\text{i } 3x^4 \times 2x^{-5} = 6x^{4+(-5)} \\ = 6x^{-1}$$

$$\text{j } \sqrt{x} \times \sqrt[3]{x} = x^{\frac{1}{2}} \times x^{\frac{1}{3}} \\ = x^{\frac{1}{2}+\frac{1}{3}} \\ = x^{\frac{5}{6}} \\ = (\sqrt[6]{x})^5$$

$$\text{k } (\sqrt{x})^3 \times (\sqrt[3]{x})^4 = x^{\frac{3}{2}} \times x^{\frac{4}{3}} \\ = x^{\frac{3}{2}+\frac{4}{3}} \\ = x^{\frac{17}{6}} \\ = (\sqrt[6]{x})^{17}$$

$$1 \frac{(\sqrt[3]{x})^2}{\sqrt{x}} = x^{\frac{2}{3}} \div x^{\frac{1}{2}} \\ = x^{\frac{2}{3}-\frac{1}{2}} \\ = x^{\frac{1}{6}} \\ = \sqrt[6]{x}$$

$$2 \text{ a } 25^{\frac{1}{2}} = \sqrt{25} \\ = 5$$

$$\text{b } 81^{\frac{3}{2}} = (\sqrt{81})^3 \\ = 9^3 \\ = 729$$

$$\text{c } 27^{\frac{1}{3}} = \sqrt[3]{27} \\ = 3$$

$$\text{d } 4^{-2} = \frac{1}{4^2} \\ = \frac{1}{16}$$

$$\text{e } 9^{-\frac{1}{2}} = \frac{1}{9^{\frac{1}{2}}} \\ = \frac{1}{\sqrt{9}} \\ = \frac{1}{3}$$

$$\text{f } (-5)^{-3} = \frac{1}{(-5)^3} \\ = -\frac{1}{125}$$

$$\text{g } \left(\frac{3}{4}\right)^0 = 1$$

$$\text{h } 1296^{\frac{3}{4}} = (\sqrt[4]{1296})^3 \\ = 6^3 \\ = 216$$

$$\begin{aligned}
 2 \text{ i } \quad \left(\frac{25}{16}\right)^{\frac{3}{2}} &= \frac{(\sqrt{25})^3}{(\sqrt{16})^3} \\
 &= \frac{5^3}{4^3} \\
 &= \frac{125}{64}
 \end{aligned}$$

$$\begin{aligned}
 \text{j} \quad \left(\frac{27}{8}\right)^{\frac{2}{3}} &= \frac{(\sqrt[3]{27})^2}{(\sqrt[3]{8})^2} \\
 &= \frac{3^2}{2^2} \\
 &= \frac{9}{4}
 \end{aligned}$$

$$\begin{aligned}
 \text{k} \quad \left(\frac{6}{5}\right)^{-1} &= \left(\frac{5}{6}\right)^1 \\
 &= \frac{5}{6}
 \end{aligned}$$

$$\begin{aligned}
 \text{l} \quad \left(\frac{343}{512}\right)^{-\frac{2}{3}} &= \frac{(\sqrt[3]{512})^2}{(\sqrt[3]{343})^2} \\
 &= \frac{8^2}{7^2} \\
 &= \frac{64}{49}
 \end{aligned}$$

$$\begin{aligned}
 3 \text{ a} \quad (64x^{10})^{\frac{1}{2}} &= \sqrt{64} \times x^{10 \times \frac{1}{2}} \\
 &= 8x^5
 \end{aligned}$$

$$\begin{aligned}
 \text{b} \quad \frac{5x^3 - 2x^2}{x^5} &= \frac{5x^3}{x^5} - \frac{2x^2}{x^5} \\
 &= 5 \times x^{3-5} - 2 \times x^{2-5} \\
 &= 5x^{-2} - 2x^{-3} \\
 &= \frac{5}{x^2} - \frac{2}{x^3}
 \end{aligned}$$

$$\begin{aligned}
 \text{c} \quad (125x^{12})^{\frac{1}{3}} &= \sqrt[3]{125} \times x^{12 \times \frac{1}{3}} \\
 &= 5x^4
 \end{aligned}$$

$$\begin{aligned}
 3 \text{ d} \quad \frac{x+4x^3}{x^3} &= \frac{x}{x^3} + \frac{4x^3}{x^3} \\
 &= x^{1-3} + 4 \times x^{3-3} \\
 &= x^{-2} + 4x^0 \\
 &= \frac{1}{x^2} + 4
 \end{aligned}$$

$$\begin{aligned}
 \text{e} \quad \frac{2x+x^2}{x^4} &= \frac{2x}{x^4} + \frac{x^2}{x^4} \\
 &= 2 \times x^{1-4} + x^{2-4} \\
 &= 2x^{-3} + x^{-2} \\
 &= \frac{2}{x^3} + \frac{1}{x^2}
 \end{aligned}$$

$$\begin{aligned}
 \text{f} \quad \left(\frac{4}{9}x^4\right)^{\frac{3}{2}} &= \left(\sqrt{\frac{4}{9}}\right)^3 x^{4 \times \frac{3}{2}} \\
 &= \frac{8}{27}x^6
 \end{aligned}$$

$$\begin{aligned}
 \text{g} \quad \frac{9x^2 - 15x^5}{3x^3} &= \frac{9x^2}{3x^3} - \frac{15x^5}{3x^3} \\
 &= 3 \times x^{2-3} - 5 \times x^{5-3} \\
 &= 3x^{-1} - 5x^2 \\
 &= \frac{3}{x} - 5x^2
 \end{aligned}$$

$$\begin{aligned}
 \text{h} \quad \frac{5x+3x^2}{15x^3} &= \frac{5x}{15x^3} + \frac{3x^2}{15x^3} \\
 &= \frac{1}{3} \times x^{1-3} + \frac{1}{5} \times x^{2-3} \\
 &= \frac{1}{3}x^{-2} + \frac{1}{5}x^{-1} \\
 &= \frac{1}{3x^2} + \frac{1}{5x}
 \end{aligned}$$

$$\begin{aligned}
 4 \text{ a} \quad 81^{\frac{1}{4}} &= \sqrt[4]{81} \\
 &= 3
 \end{aligned}$$

$$\begin{aligned}
 \text{b} \quad x(2x^{\frac{1}{3}})^4 &= x \times 2^4 \times x^{\frac{1}{3} \times 4} \\
 &= 2^4 x^{\frac{4}{3}+1} \\
 &= 16x^{\frac{7}{3}}
 \end{aligned}$$

$$\begin{aligned} 5 \text{ a } y^{\frac{1}{3}} &= \left(\frac{1}{8}x^3\right)^{\frac{1}{3}} \\ &= \frac{1}{\sqrt[3]{8}}x^{3 \times \frac{1}{3}} \\ &= \frac{x}{2} \end{aligned}$$

$$\begin{aligned} \text{b } \frac{1}{2}y^{-2} &= \frac{1}{2}\left(\frac{1}{8}x^3\right)^{-2} \\ &= \frac{1}{2} \times \frac{1}{\left(\frac{1}{8}x^3\right)^2} \\ &= \frac{1}{2} \times \frac{64}{x^{3 \times 2}} \\ &= \frac{32}{x^6} \\ &= 32x^{-6} \end{aligned}$$