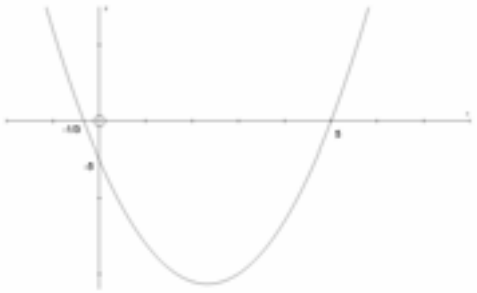


**Mark Scheme 4721
June 2007**

4 (i)	$(-4)^2 - 4 \times k \times k$ $= 16 - 4k^2$	M1 A1 2	Uses $b^2 - 4ac$ (involving k) $16 - 4k^2$
(ii)	$16 - 4k^2 = 0$ $k^2 = 4$ $k = 2$ or $k = -2$	M1 B1 B1 3 5	Attempts $b^2 - 4ac = 0$ (involving k) or attempts to complete square (involving k)
5 (i)	Length = $20 - 2x$ Area = $x(20 - 2x)$ $= 20x - 2x^2$	M1 A1 2	Expression for length of enclosure in terms of x Correctly shows that area = $20x - 2x^2$ AG
(ii)	$\frac{dA}{dx} = 20 - 4x$ For max, $20 - 4x = 0$ $x = 5$ only Area = 50	M1 M1 A1 A1 4 6	Differentiates area expression Uses $\frac{dy}{dx} = 0$
6	Let $y = (x + 2)^2$ $y^2 + 5y - 6 = 0$ $(y + 6)(y - 1) = 0$ $y = -6$ or $y = 1$ $(x + 2)^2 = 1$ $x = -1$ or $x = -3$	B1 M1 A1 M1 A1 A1 6 6	Substitute for $(x + 2)^2$ to get $y^2 + 5y - 6 (= 0)$ Correct method to find roots Both values for y correct Attempt to work out x One correct value Second correct value and no extra real values
7 (a)	$f(x) = x + 3x^{-1}$ $f'(x) = 1 - 3x^{-2}$	M1 A1 A1 A1 4	Attempt to differentiate First term correct x^{-2} soi www Fully correct answer
(b)	$\frac{dy}{dx} = \frac{5}{2}x^{\frac{3}{2}}$ When $x = 4$, $\frac{dy}{dx} = \frac{5}{2}\sqrt{4^3}$ $= 20$	M1 B1 B1 M1 A1 5 9	Use of differentiation to find gradient $\frac{5}{2}x^c$ $kx^{\frac{3}{2}}$ $\sqrt{4^3}$ soi SR If 0 scored for first 3 marks, award B1 if $\sqrt{4^n}$ correctly evaluated.

<p>8 (i)</p> $(x + 4)^2 - 16 + 15$ $= (x + 4)^2 - 1$ <p>(ii)</p> $(-4, -1)$ <p>(iii)</p> $x^2 + 8x + 15 > 0$ $(x + 5)(x + 3) > 0$ $x < -5, x > -3$	<p>B1 M1 A1 3</p> <p>B1 ft B1 ft 2</p> <p>M1 A1</p> <p>M1</p> <p>A1 4</p> <p>9</p>	<p>a = 4 15 – their a² cao in required form</p> <p>Correct x coordinate Correct y coordinate</p> <p>Correct method to find roots -5, -3</p> <p>Correct method to solve quadratic inequality eg +ve quadratic graph</p> <p>x < -5, x > -3 (not wrapped, strict inequalities, no 'and')</p>
<p>9 (i)</p> $(x - 3)^2 - 9 + y^2 - k = 0$ $(x - 3)^2 + y^2 = 9 + k$ <p>Centre (3, 0)</p> $9 + k = 4^2$ $k = 7$ <p>(ii)</p> $(3 - 3)^2 + y^2 = 16$ $y^2 = 16$ $y = 4$ $\text{Length of AB} = \sqrt{(-1 - 3)^2 + (0 - 4)^2}$ $= \sqrt{32}$ $= 4\sqrt{2}$ <p>(iii)</p> <p>Gradient of AB = 1 or $\frac{a}{4}$</p> $y - 0 = m(x + 1) \quad \text{or} \quad y - 4 = m(x - 3)$ $y = x + 1$	<p>B1 B1 M1 A1 4</p> <p>M1 A1</p> <p>M1 A1 ft A1 5</p> <p>B1 ft M1 A1 3</p> <p>12</p>	<p>$(x - 3)^2$ soi Correct centre</p> <p>Correct value for k (may be embedded)</p> <p><u>Alternative method using expanded form:</u> Centre (-g, -f) M1 Centre (3, 0) A1 $4 = \sqrt{f^2 + g^2 - (-k)}$ M1 k = 7 A1</p> <p>Attempt to substitute x = 3 into original equation or their equation y = 4 (do not allow ± 4)</p> <p>Correct method to find line length using Pythagoras' theorem $\sqrt{32}$ or $\sqrt{16 + a^2}$ cao</p> <p>Attempts equation of straight line through their A or B with their gradient Correct equation in any form with simplified constants</p>

10 (i)	$(3x + 1)(x - 5) = 0$ $x = \frac{-1}{3}$ or $x = 5$	M1 A1 A1 3	Correct method to find roots Correct brackets or formula Both values correct SR B1 for $x = 5$ spotted www
(ii)		B1 B1 B1 ft 3	Positive quadratic (must be reasonably symmetrical) y intercept correct both x intercepts correct
(iii)	$\frac{dy}{dx} = 6x - 14$ $6x - 14 = 4$ $x = 3$ On curve, when $x = 3$, $y = -20$ $-20 = (4 \times 3) + c$ $c = -32$ <u>Alternative method:</u> $3x^2 - 14x - 5 = 4x + c$ $3x^2 - 18x - 5 - c = 0$ has one solution $b^2 - 4ac = 0$ $(-18)^2 - (4 \times 3 \times (-5 - c)) = 0$ $c = -32$	M1* M1* A1 A1 ft M1dep A1 6 M1 B1 M1 M1 A1 A1 12	Use of differentiation to find gradient of curve Equating their gradient expression to 4 Finding y co ordinate for their x value N.B. dependent on both previous M marks Equate curve and line (or substitute for x) Statement that only one solution for a tangent (may be implied by next line) Use of discriminant = 0 Attempt to use a, b, c from their equation Correct equation $c = -32$