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1. Simplify

$$\frac{7 + \sqrt{5}}{\sqrt{5} - 1}$$

giving your answer in the form $a + b\sqrt{5}$, where a and b are integers.

(4)

Q1

(Total 4 marks)



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2. Find

$$\int \left(10x^4 - 4x - \frac{3}{\sqrt{x}} \right) dx$$

giving each term in its simplest form.

(4)

Q2

(Total 4 marks)

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4. A sequence a_1, a_2, a_3, \dots is defined by

$$\begin{aligned} a_1 &= 4 \\ a_{n+1} &= k(a_n + 2), \quad \text{for } n \geq 1 \end{aligned}$$

where k is a constant.

(a) Find an expression for a_2 in terms of k . (1)

Given that $\sum_{i=1}^3 a_i = 2,$

(b) find the two possible values of k . (6)



6. The straight line L_1 passes through the points $(-1, 3)$ and $(11, 12)$.

(a) Find an equation for L_1 in the form $ax + by + c = 0$,

where a, b and c are integers.

(4)

The line L_2 has equation $3y + 4x - 30 = 0$.

(b) Find the coordinates of the point of intersection of L_1 and L_2 .

(3)



8.

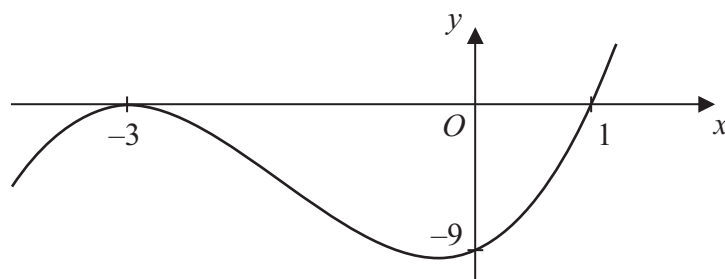
**Figure 1**

Figure 1 shows a sketch of the curve with equation $y = f(x)$ where

$$f(x) = (x + 3)^2 (x - 1), \quad x \in \mathbb{R}.$$

The curve crosses the x -axis at $(1, 0)$, touches it at $(-3, 0)$ and crosses the y -axis at $(0, -9)$

- (a) In the space below, sketch the curve C with equation $y = f(x + 2)$ and state the coordinates of the points where the curve C meets the x -axis. **(3)**
- (b) Write down an equation of the curve C . **(1)**
- (c) Use your answer to part (b) to find the coordinates of the point where the curve C meets the y -axis. **(2)**



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9.

$$f'(x) = \frac{(3 - x^2)^2}{x^2}, \quad x \neq 0$$

(a) Show that $f'(x) = 9x^{-2} + A + Bx^2$,
where A and B are constants to be found. (3)

(b) Find $f''(x)$. (2)

Given that the point $(-3, 10)$ lies on the curve with equation $y = f(x)$,

(c) find $f(x)$. (5)



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Question 9 continued

Area containing horizontal lines for writing.

(Total 10 marks)

Q9

Two small boxes for marking.



11.

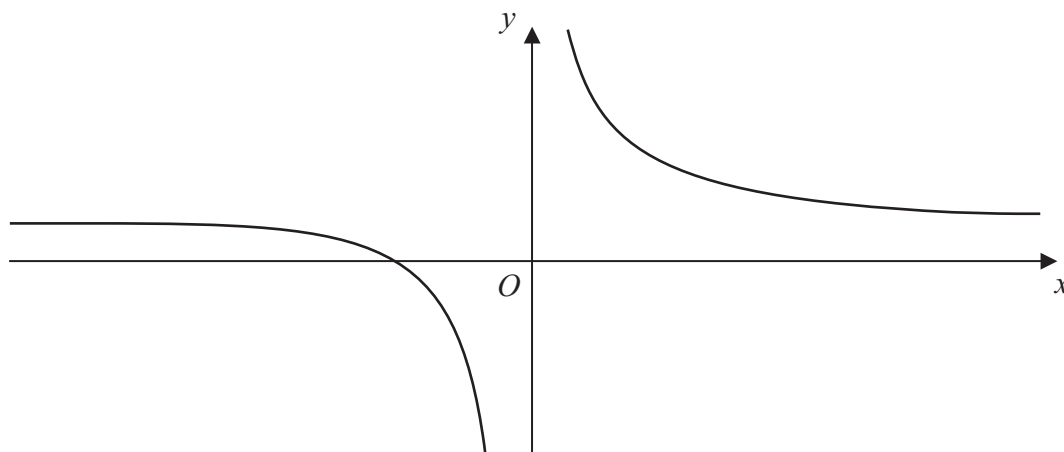
**Figure 2**

Figure 2 shows a sketch of the curve H with equation $y = \frac{3}{x} + 4$, $x \neq 0$.

- (a) Give the coordinates of the point where H crosses the x -axis. **(1)**
- (b) Give the equations of the asymptotes to H . **(2)**
- (c) Find an equation for the normal to H at the point $P(-3, 3)$. **(5)**

This normal crosses the x -axis at A and the y -axis at B .

- (d) Find the length of the line segment AB . Give your answer as a surd. **(3)**



Question 11 continued

Lined area for writing the answer to Question 11.

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Q11

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(Total 11 marks)

TOTAL FOR PAPER: 75 MARKS

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