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Surname	Other nar	nes
Pearson Edexcel International Advanced Level	Centre Number	Candidate Number
Core Math	nematic	s C12
Advanced Subsidia	ry	
Advanced Subsidian Wednesday 23 May 2018 – Time: 2 hours 30 minutes	Morning	Paper Reference WMA01/01

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

#### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

#### **Information**

- The total mark for this paper is 125.
- The marks for each question are shown in brackets
   use this as a quide as to how much time to spend on each question.

#### **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

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1. The table below shows corresponding values of x and y for  $y = \frac{1}{\sqrt{(x+1)}}$ , with the values for y rounded to 3 decimal places where necessary.

X	0	3	6	9	12	15
y	1	0.5	0.378	0.316	0.277	0.25

- (a) Complete the table by giving the value of y corresponding to x = 15 (1)
- (b) Use the trapezium rule with all the values of y from the completed table to find an approximate value for

$$\int_0^{15} \frac{1}{\sqrt{(x+1)}} \mathrm{d}x$$

giving your answer to 2 decimal places.

(b) <u>h</u>		
3-0=3.		
6-3=3.		

2. 
$$f(x) = ax^3 + 2x^2 + bx - 3$$

where a and b are constants.

When f(x) is divided by (2x - 1) the remainder is 1

(a) Show that

$$a + 4b = 28$$

(2)

When f(x) is divided by (x + 1) the remainder is -17

(b) Find the value of a and the value of b.

$$f(\frac{1}{2}) = 1.$$

$$q(\frac{1}{2})^{3} + 2(\frac{1}{2})^{2} + b(\frac{1}{2}) - 3 = 1$$

$$\frac{1}{8} + \frac{1}{2} + \frac{b}{2} - 3 = 1.$$

$$-9+2(-1)^2+b(-1)-3$$

$$-9+2-b-3=-17$$

$$a = 16 - b$$
 $9 = 16 - 4 = 12$ 



The line  $l_1$  passes through the points A(-1, 4) and B(5, -8)

(a) Find the gradient of  $l_1$ 

(2)

The line  $l_2$  is perpendicular to the line  $l_1$  and passes through the point B(5, -8)

(b) Find an equation for l, in the form ax + by + c = 0, where a, b and c are integers.

(4)

(9)	42-41	=	-8-4
	X2-X,		51

$$\frac{1}{6} = \frac{-12}{6}$$

(b) grad of to line

y=1 n+( (5,-8)

2y = x - 21 2y - x + 21 = 0

## 4. Given that

$$y = \frac{64x^6}{25}, \ x > 0$$

express each of the following in the form  $kx^n$  where k and n are constants.

(a) 
$$y^{-\frac{1}{2}}$$

(3)

(b) 
$$(25y)^{\frac{2}{3}}$$

	(2)
4-1/2	
9	
$=\left(\frac{64\pi}{25}\right)^{-1/2}$	
64 <sup>1/2</sup> . x <sup>3</sup> 25 <sup>-1/2</sup>	
$= \frac{5}{8} x^{-3}$	
(b) 25.64x6	
(64x6)2/3	
= 64 <sup>2/3</sup> . x <sup>4</sup>	
= 1G1 4	

5. (a) Find the first 4 terms, in ascending powers of x, of the binomial expansion of

$$\left(1+\frac{x}{3}\right)^{18}$$

giving each term in its simplest form.

(4)

(b) Use the answer to part (a) to find an estimated value for  $\left(\frac{31}{30}\right)^{18}$ , stating the value of x that you have used and showing your working. Give your estimate to 4 decimal places.

(a)  $1+\binom{18}{1}\left(\frac{x}{3}\right)+\binom{18}{2}\left(\frac{x}{3}\right)^2+\binom{18}{3}\left(\frac{x}{3}\right)^3$ 

= 1+ 6x+17x2+272 x3....

(b) 
$$1+\frac{\chi}{3}=\frac{31}{30}$$

11-0-1

1+6(01)+17(01)2+272(001)3

=1.8002

### **6.** Find the exact values of x for which

$$2\log_5(x+5) - \log_5(2x+2) = 2$$

Give your answers as simplified surds.

**(7)** 

1091	(x+5)	2-109	(2x+2)
, 75,		)5	

$$\log \left( \frac{(x+5)^2}{(2x+2)} \right) = 2$$

$$25 = \frac{(x+5)^2}{2(x+1)}$$

# 7. A sequence is defined by

$$u_1 = 3$$
  
 $u_{n+1} = u_n - 5, \quad n \ge 1$ 

Find the values of

(a) 
$$u_2$$
,  $u_3$  and  $u_4$ 

(2)

(b) 
$$u_{100}$$

(3)

(c) 
$$\sum_{i=1}^{100} u_i$$

(3)

G= =-24,450

12 = -2

43 = -7

d=-5

$$=\frac{100}{2}$$
  $\left[2(3)+(-5)(99)\right]$ 

= -24,450

- 8. The equation  $(k-4)x^2 4x + k 2 = 0$ , where k is a constant, has no real roots.
  - (a) Show that k satisfies the inequality

$$k^2 - 6k + 4 > 0$$

(b) Find the exact range of possible values for k.

(4)

(3)

(9) b2-490 CO.	K 63-55
(-4) 2-4(K-4)(K-2) CO	k>3+55
(6 + [-4KH6(K-2)]	
-4K2+8K+16K-32	
16 + [-4K2+24K-32] CO	
-4K2+24K-16C0	
162-6K+430 95 reg.	
(b) solve sketch range.	
6+ 562-4(4)	
K=3+15	

9. A cyclist aims to travel a total of 1200km over a number of days.

He cycles 12km on day 1

He increases the distance that he cycles each day by 6% of the distance cycled on the previous day, until he reaches the total of 1200km.

(a) Show that on day 8 he cycles approximately 18 km.

(3)

He reaches his total of  $1200 \,\mathrm{km}$  on day N, where N is a positive integer.

(b) Find the value of N.

(4)

The cyclist stops when he reaches 1200km.

(c) Find the distance that he cycles on day N. Give your answer to the nearest km.

**(2)** 

	34-1
9 = 12.	(c) 1200-12(1.06 <sup>34-1</sup> -1)
9r=12.72 : v=1.06	1.06-1
ar	= 32km
2	

 $= 12 \times 1.06^{\circ} = 16.04$  $\approx 18 \text{ km}$ 

12(1-1.06°) = 1200.

1-1.06 = -6.

10.

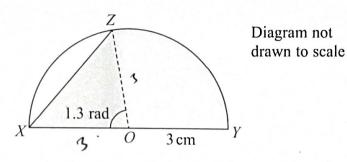


Figure 1

Figure 1 shows a semicircle with centre O and radius 3 cm. XY is the diameter of this semicircle. The point Z is on the circumference such that angle XOZ = 1.3 radians. The shaded region enclosed by the chord XZ, the arc ZY and the diameter XY is a template for a badge.

Find, giving each answer to 3 significant figures,

(a) the length of the chord XZ,

(2)

(b) the perimeter of the template XZYX,

(4)

(c) the area of the template.

9) cosine rule	(c) Area of triangle.
9 = 3 + 3 - (2x3x3 (0s(1-3))	1 x 3 x 3 Sin (1.3)
9=3.63 cm	= 4.34
(b) Arc length 24.	Avea of sector
(=YO'	1x 32x (N-1-3)
$= 3 \times (\pi - 1.3)$ = 5.52.	= 8.29.
3.63+5.52+6	= 4.34 + 8.29
= 15.2 cm	= 12.6 cm <sup>2</sup> .

11. The curve C has equation y = f(x), x > 0, where

$$f'(x) = \frac{5x^2 + 4}{2\sqrt{x}} - 5$$

It is given that the point P(4, 14) lies on C.

(a) Find f(x), writing each term in a simplified form.

**(6)** 

(b) Find the equation of the tangent to C at the point P, giving your answer in the form y = mx + c, where m and c are constants.

(9) 5x2 + 4 -5	$f(x) = x^{\sqrt{2}} + 4x^{\sqrt{2}} - 5x - 6$
$=\frac{5}{2}x^{3/2}+2x^{-1/2}-5$	(b) f'(4)
Integrate.	= 5(4) 2+4 -5
$\int \frac{5}{2} x^{3/2} + 2x^{-1/2} - 5 \int x$	= 84 -5 = 16 4
$\frac{5\pi^{5/2}}{2} + 2\pi^{1/2} - 5\pi + 7$	y=16x+C (4,14)
3/2 1/2	14=64+C C=-50.
$(x) = x^{5/2} + 4x^{1/2} - 5x + 0$	y=16x-50
When x=4 y=14.	
14:(4) 92 + 4(4) 12-5(4) +(	
c=-6,	

12. [In this question solutions based entirely on graphical or numerical methods are not acceptable.]

(i) Solve for 
$$0 \le x < 360^\circ$$
,



$$5\sin(x+65^{\circ})+2=0$$

giving your answers in degrees to one decimal place.

(4)

(ii) Find, for  $0 \le \theta < 2\pi$ , all the solutions of

$$12\sin^2\theta + \cos\theta = 6$$

giving your answers in radians to 3 significant figures.

(6)

(i) Sin (x+65) = -2.	When cos 0 = -2/3.
$n+65 = \sin^{-1}\left(-\frac{2}{5}\right)$	$0 = 2.30, 3.98$ When $\cos 0 = 3/4$
7+65 = 203.6,336.4,	O=0.723, 5.56
x=138.6,271.4°	
(i) 12(1-cos²0)+ros8=6.	
12-12(05 <sup>2</sup> 0 + (050 = 6.	
1200520-0000-6=0	
1 + S(2 - 4(12x-6) 2 x12	
(050=-43 or 3/4.	

13. The point A(9, -13) lies on a circle C with centre the origin and radius r.

(a) Find the exact value of r.

(2)

(b) Find an equation of the circle C.

(1)

A straight line through point A has equation 2y + 3x = k, where k is a constant.

(c) Find the value of k.

(1)

This straight line cuts the circle again at the point B.

(d) Find the exact coordinates of point B.

(6)

a) (x-9)2+(y+13)2=	$\left( \frac{\chi^2 + \left( \frac{1}{2} \left( -3 \times + 1 \right) \right)^2}{2} = 250.$
$\chi^2 + y^2 = \chi^2$	$\chi^{2} + \frac{1}{4} (-3 \times + 1)^{2} = 750$
tot length off.	4
V(9-0)2+(-13-0)2	$\chi^2 + 1 (9\chi^2 - 6\chi + 1) = 250$
- 5/10	1, 2, 0, 2, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
:, r=5√10	$4x^{2}+9x^{2}-6x+1=1000$ . $13x^{2}-6x-999=0$ .
(b) x2+y2=250.	6 t 162 - 4 (13x-999)
(c) $7(-13)+3(9)=k$ .	2 +13
<u>K=1</u>	7 = -111 or 9.
2y=-3x+1	x / / 2 / 2 / 2
y=-3 x +1.	$\chi = \frac{111}{13}$ $y = \frac{173}{13}$

**(1)** 

14.

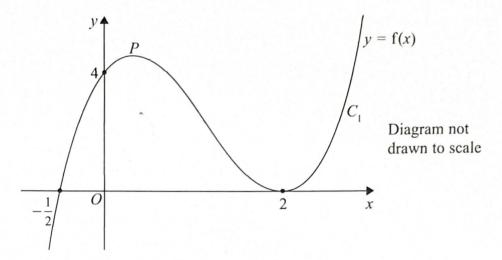


Figure 2

Figure 2 shows a sketch of the curve  $C_1$  with equation y = f(x) where

$$f(x) = (x-2)^2(2x+1), x \in \mathbb{R}$$

The curve crosses the x-axis at  $\left(-\frac{1}{2},0\right)$ , touches it at (2, 0) and crosses the y-axis at (0, 4). There is a maximum turning point at the point marked P.

(a) Use f'(x) to find the exact coordinates of the turning point P. **(7)** 

A second curve  $C_2$  has equation y = f(x + 1).

(b) Write down an equation of the curve  $C_2$ You may leave your equation in a factorised form.

(c) Use your answer to part (b) to find the coordinates of the point where the curve  $C_{\gamma}$ meets the y-axis. **(2)** 

- (d) Write down the coordinates of the two turning points on the curve  $C_2$ **(2)**
- (e) Sketch the curve  $C_2$ , with equation y = f(x + 1), giving the coordinates of the points where the curve crosses or touches the x-axis. **(3)**

 $f(x)=(x-2)^{2}(2x+1)$  f'(x)=0. Using chain rule f'(x)=0.  $(\chi-2) \left[ 2(2xH) + 2(x-2) \right] = 0$   $\frac{\chi=2 \quad (not required)}{point prom}$   $\frac{q}{q} = \frac{1}{q} \left[ \frac{1}{q} + \frac$  $2(x-2)(2x+1)+(x-2)^2.2$ 

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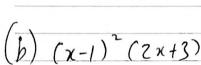
### **Question 14 continued**

$$\chi = \frac{1}{2}$$

$$f(\frac{1}{3}) = \left(\frac{1}{3} - 2\right)^{2} \left(2\left(\frac{1}{3}\right) + 1\right)$$

$$(1,0)$$
  $\left(-\frac{2}{3},125\right)$ .

$$\therefore \beta \Rightarrow \left(\frac{1}{3}, \frac{1^{25}}{17}\right)$$





$$(-1)^{2}(3)$$

$$=\frac{3}{2}$$
 (0,3).



$$2(y-1)(2x+3)+2(x-1)^{2}$$

$$=(x-1)\int 2(2x+3) + 2(x-1) = 0$$

15.

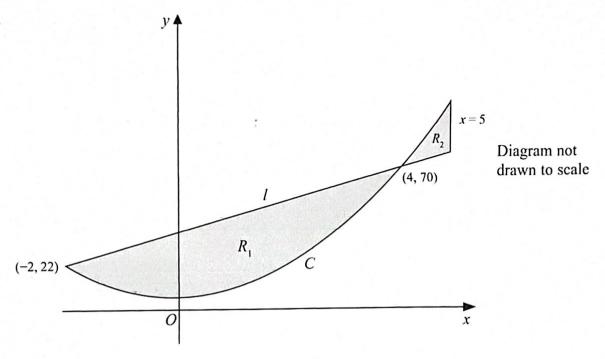


Figure 3

A design for a logo consists of two finite regions  $R_1$  and  $R_2$ , shown shaded in Figure 3.

The region  $R_1$  is bounded by the straight line l and the curve C.

The region  $R_2$  is bounded by the straight line l, the curve C and the line with equation x = 5

The line *l* has equation y = 8x + 38

The curve C has equation  $y = 4x^2 + 6$ 

Given that the line l meets the curve C at the points (-2, 22) and (4, 70), use integration to find

(a) the area of the larger lower region, labelled 
$$R_1$$

(6)

The state of the s

(b) the exact value of the total area of the two shaded regions.

(3)

Given that

$$\frac{\text{Area of } R_1}{\text{Area of } R_2} = k$$

(c) find the value of 
$$k$$
.

(1)

<b>Ouestion</b>	15	continued	

(9) Area Under Curve	Avea under line.
(4 x 2 + 6.	(5-4) (70+78)
$\left[\frac{4x^3}{3} + 6n\right]_{-7}^{4}$	= 74.
[-2	<u>262</u> - 74
$\left[\frac{4(3)^3}{3} + 6(4)\right] - \left[\frac{4(-2)^3}{3} + 6(-2)\right]$	= 40
= 132	144 : 132+40 = 436472 3 3 3
Aveg under line.	
1 x (2 + 4) x (22+ 70)	() 10.8
= 276.	
276-132	
(b) Avea of Ri	
$\left[\frac{4\pi^3+6\pi}{3}\right]_4$	
$\left(\frac{4(5)^{3}}{3}+6(5)\right)-\left(\frac{4(4)^{3}}{3}+6(4)\right)$	
262.	

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