

8. The curve C_1 has equation

$$y = x^2(x + 2)$$

(a) Find $\frac{dy}{dx}$

(2)

(b) Sketch C_1 , showing the coordinates of the points where C_1 meets the x -axis.

(3)

(c) Find the gradient of C_1 at each point where C_1 meets the x -axis.

(2)

The curve C_2 has equation

$$y = (x - k)^2(x - k + 2)$$

where k is a constant and $k > 2$

(d) Sketch C_2 , showing the coordinates of the points where C_2 meets the x and y axes.

(3)



Question 8 continued



P 4 0 0 8 2 A 0 1 9 2 8

9. A company offers two salary schemes for a 10-year period, Year 1 to Year 10 inclusive.

Scheme 1: Salary in Year 1 is £ P .
Salary increases by £ $(2T)$ each year, forming an arithmetic sequence.

Scheme 2: Salary in Year 1 is £ $(P + 1800)$.
Salary increases by £ T each year, forming an arithmetic sequence.

(a) Show that the **total** earned under Salary Scheme 1 for the 10-year period is

$$\pounds(10P + 90T) \quad (2)$$

For the 10-year period, the **total** earned is the same for both salary schemes.

(b) Find the value of T . (4)

For this value of T , the salary in Year 10 under Salary Scheme 2 is £29 850

(c) Find the value of P . (3)



10.

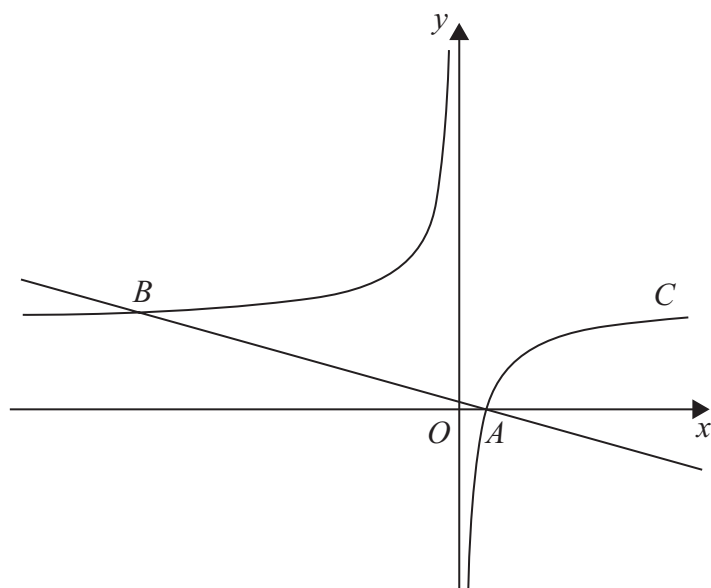


Figure 2

Figure 2 shows a sketch of the curve C with equation

$$y = 2 - \frac{1}{x}, \quad x \neq 0$$

The curve crosses the x -axis at the point A .

(a) Find the coordinates of A . (1)

(b) Show that the equation of the normal to C at A can be written as

$$2x + 8y - 1 = 0 \quad (6)$$

The normal to C at A meets C again at the point B , as shown in Figure 2.

(c) Find the coordinates of B . (4)



