

BLANK PAGE

2. (i) Given that $y = 5x^3 + 7x + 3$, find

(a) $\frac{dy}{dx}$, (3)

(b) $\frac{d^2y}{dx^2}$. (1)

(ii) Find $\int \left(1 + 3\sqrt{x} - \frac{1}{x^2}\right) dx$. (4)

6.

Figure 1

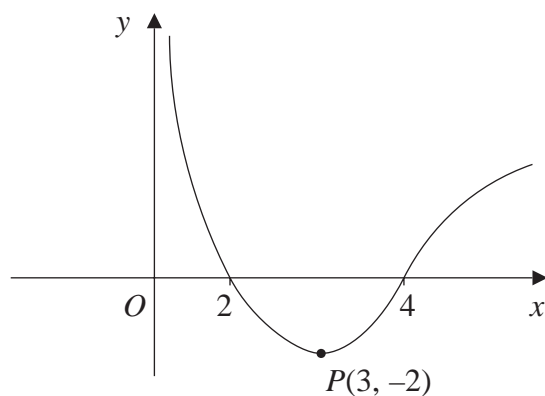


Figure 1 shows a sketch of the curve with equation $y = f(x)$. The curve crosses the x -axis at the points $(2, 0)$ and $(4, 0)$. The minimum point on the curve is $P(3, -2)$.

In separate diagrams sketch the curve with equation

(a) $y = -f(x)$, (3)

(b) $y = f(2x)$. (3)

On each diagram, give the coordinates of the points at which the curve crosses the x -axis, and the coordinates of the image of P under the given transformation.

Leave
blank

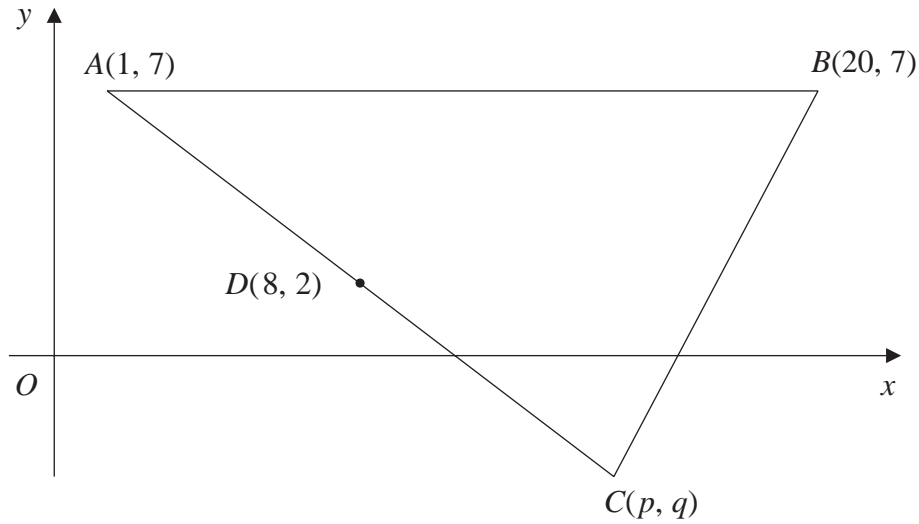
Question 6 continued

Q6

(Total 6 marks)

8.

Figure 2



The points $A(1, 7)$, $B(20, 7)$ and $C(p, q)$ form the vertices of a triangle ABC , as shown in Figure 2. The point $D(8, 2)$ is the mid-point of AC .

(a) Find the value of p and the value of q .

(2)

The line l , which passes through D and is perpendicular to AC , intersects AB at E .

(b) Find an equation for l , in the form $ax + by + c = 0$, where a , b and c are integers.

(5)

(c) Find the exact x -coordinate of E .

(2)

9. The gradient of the curve C is given by

$$\frac{dy}{dx} = (3x - 1)^2.$$

The point $P(1, 4)$ lies on C .

(a) Find an equation of the normal to C at P . (4)

(b) Find an equation for the curve C in the form $y = f(x)$. (5)

(c) Using $\frac{dy}{dx} = (3x - 1)^2$, show that there is no point on C at which the tangent is parallel to the line $y = 1 - 2x$. (2)

Question 10 continued

Leave
blank

Q10

--	--

(Total 12 marks)

TOTAL FOR PAPER: 75 MARKS

END

BLANK PAGE