

# OCR Computer Science A Level

## 2.3.1 Algorithms for the Main Data Structures Intermediate Notes



**Specification:**

- Stacks
- Queues
- Linked lists
- Trees
- Traversal of trees
  - Depth-first (post-order)
  - Breadth-first



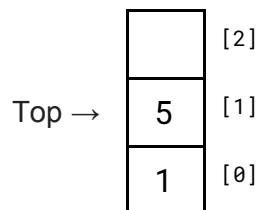
## Algorithms for the Main Data Structures

Algorithms and data structures go **hand in hand**. Each data structure has its own algorithms associated with it, allowing the data to be manipulated in useful ways.

All of the data structures mentioned in these notes are covered in greater detail in the notes for 1.4.2 Data Structures.

### Stacks

Stacks are an example of a **first in, last out** (FILO) data structure. They are often **implemented as an array** and use a **single pointer** which keeps track of the top of the stack (called the top pointer). This points to the element which is **currently at the top** of the stack.



Algorithms for stacks include adding to the stack, removing from the stack and checking whether the stack is empty/full. These have their own **special names**, as shown in the table below.

| Operation  | Name          |
|--|---------------|
| Check size   | size()        |
| Check if empty   | isEmpty()     |
| Return top element (but don't remove)                        | peek()        |
| Add to the stack   | push(element) |
| Remove top element from the stack and return removed element | pop()         |



### size()

Size returns the **number of elements** on the stack. The pseudocode is as simple as returning the value of the top pointer plus one (remember that the first element is in position 0).

```
size()
    return top + 1
```

### isEmpty()

To check whether a stack is empty, we need to check whether the top pointer is **less than 0**. If it is, then the stack is empty, otherwise there is data in the stack

```
isEmpty()
    if top < 0:
        return True
    else:
        return False
    endif
```

### peek()

To return the item at the top of the stack, **without removing it**, simply return the item at the position indicated by the top pointer. For these examples, we'll assume our stack is an array called A.

Don't forget to check that the stack **has data in it** before attempting to return data though, an empty stack could cause errors. It's useful to use the `isEmpty` function here.

```
peek()
    if isEmpty():
        return error
    else:
        return A[top]
    endif
```

### push(element)

To add an item to a stack, the new item is **passed as a parameter**. Firstly, the top pointer is updated. Then the new element can be inserted at the position of the top pointer.

```
push(element)
    top += 1
    A[top] = element
```



### pop()

To **remove an item** from a stack, the element at the position of the top pointer is recorded before being removed. Then the top pointer is **decremented by one** before the removed item is returned. As with `peek()`, it's important to check that the stack **isn't empty** before attempting a `pop`.

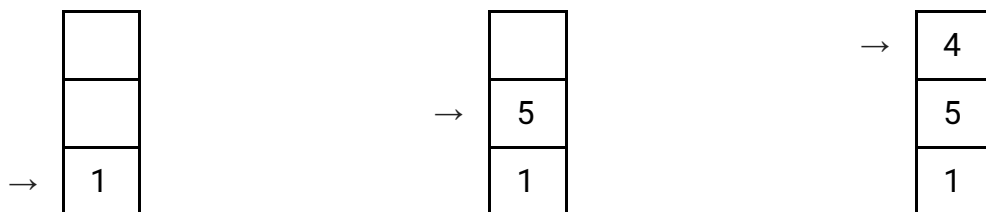
```
pop()
  if isEmpty():
    return error
  else:
    toRemove = A[top]
    A[top] = ""
    top -= 1
    return toRemove
  endif
```

### Example

What would be the result of the following operations on a 3-element stack?

```
push(1)
push(5)
push(4)
peek()
pop()
isEmpty()
```

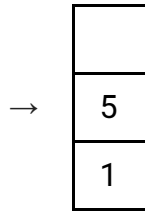
The first three operations push the items 1, 5 and 4 to the stack in that order.



The next operation is a `peek`. This returns the item at the top of the stack, but **doesn't change the appearance of the stack**. Therefore this operation returns **4** and the stack remains the same.

Next is `pop`. This **removes the item at the top of the stack** and returns it, **4**, before the top pointer moves down one place.





Finally `isEmpty` is carried out. The stack **is not empty** and so **False** is returned.

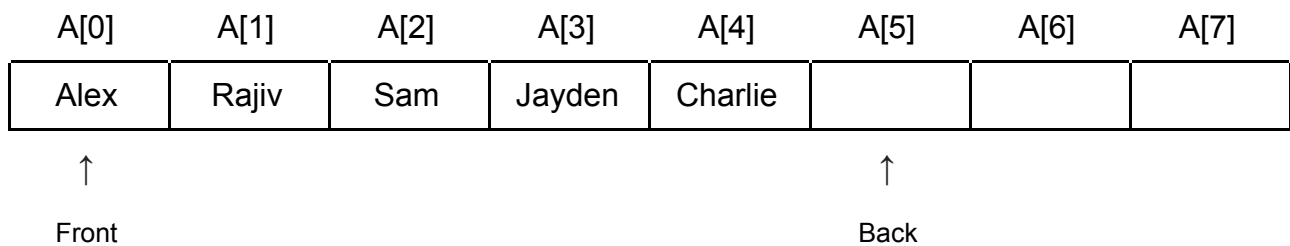
`isEmpty` doesn't affect the appearance of a stack, meaning that the final state of the stack is as shown above. The output from the operations is:

**4, 4, False**

## Queues

Queues are a type of **first in, first out** (FIFO) data structure. Just like stacks, queues are often represented as arrays. However, unlike stacks, queues make use of two pointers: **front and back**. While front holds the position of the first element, back stores the **next available space**.

Operations which can be carried out on queues are similar to those associated with stacks, but be aware - some have different names.



| Operation  | Name                          |
|--|-------------------------------|
| Check size                                       | <code>size()</code>           |
| Check if empty                                   | <code>isEmpty()</code>        |
| Return top element (but don't remove)            | <code>peek()</code>           |
| Add to the queue                                 | <code>enqueue(element)</code> |
| Remove from the queue and return removed element | <code>dequeue()</code>        |



### size()

To work out the size of a queue, simply **subtract the value of front from back**. If front is at 0 and back is at 5, there are 5 elements in the queue.

```
size()
    return back - front
```

### isEmpty()

When a queue is empty, front and back **point to the same position**. To check whether a queue is empty, just check whether the two pointers hold **the same value**.

```
isEmpty()
    if front == back:
        return True
    else:
        return False
```

### peek()

Just like a stack, peek returns the element at the front of the queue **without removing it**.

```
peek()
    return A[front]
```

### enqueue(element)

To add an element to a queue, the element is placed in the position of back and then back is **incremented by one**.

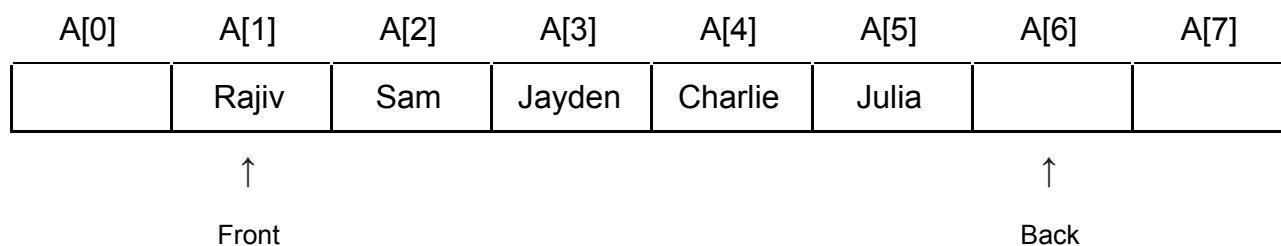
```
enqueue(element)
    A[back] = element
    back += 1
```







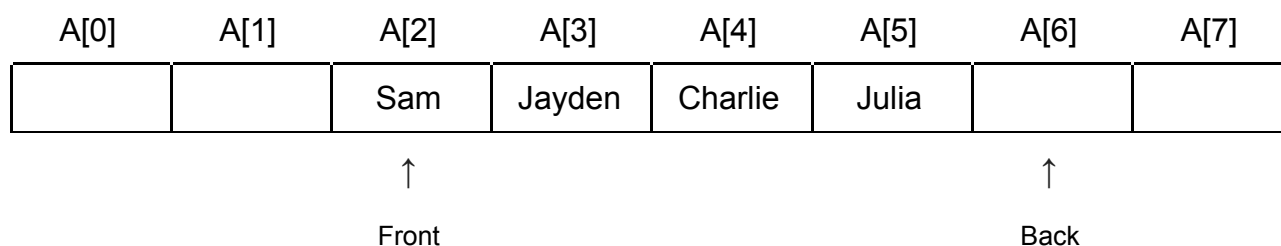
Next, Julia is enqueued. The name is added **at the position of the back pointer** and the back pointer is moved to position 6.



Now we check the size of the queue.  $6 - 1 = 5$  and so **5** is returned. The next operation is peek which returns the item at the front of the queue, **Rajiv** but does not change the queue otherwise.

The next operation is size, and because the queue hasn't changed as a result of the peek operation, **5** is returned again.

Next a dequeue is performed. Rajiv is returned, removed from the queue and the front pointer moved to Sam.



Finally, the isEmpty command is performed. Because the values of front and back **are not the same**, False is returned.

The output of the operations is therefore:

**Alex, 5, Rajiv, 5, Rajiv, False**

## Linked Lists

A linked list is composed of **nodes**, each of which has a pointer to the **next item** in the list. If a node is referred to as N, the next node can be accessed using **N.next**. The first item in a list is referred to as the **head** and the last as the **tail**.

Searching a list is performed using a **linear search**, carried out by sequential next operations until the desired element is found.



## Trees

Trees are formed from **nodes** and **edges**, which **cannot contain cycles** and **aren't directed**. Trees are useful as a data structure because they can be **traversed**.

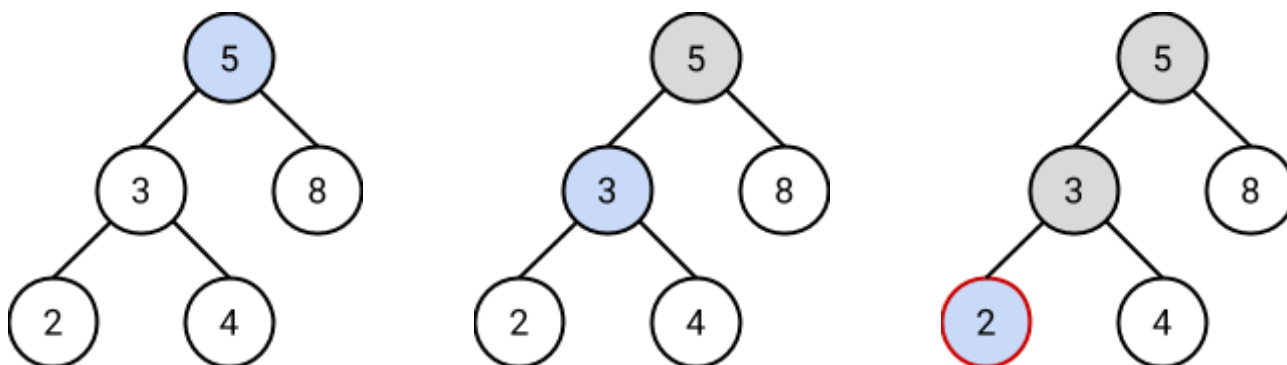
There are two types of traversal to cover: **depth first** (post-order) and **breadth first**.

### Depth first (post-order) traversal

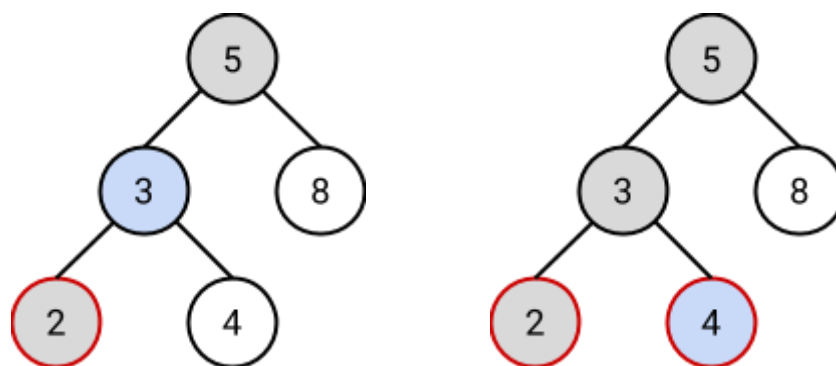
Depth first search goes **as far into the tree as possible** before backtracking. The algorithm goes to the **left child node** of the current node when it can. If there is no left child then the algorithm goes to the **right child**.

If there are no child nodes, the algorithm **visits** the current node, outputting the value of the node before backtracking to the next node and **moving right**.

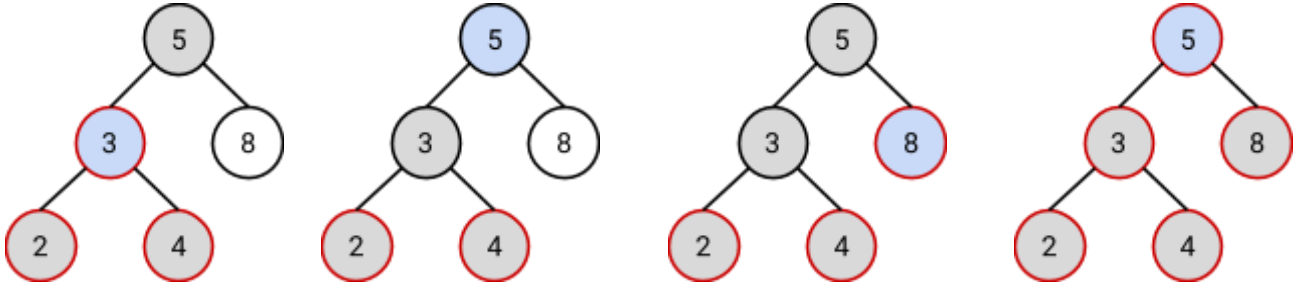
On the tree below, with depth first search starting at the node labelled 5, the algorithm moves left while it can, passing 3 before reaching 2. At this point, the algorithm can no longer move left and therefore 'visits' 2, outputting the value.



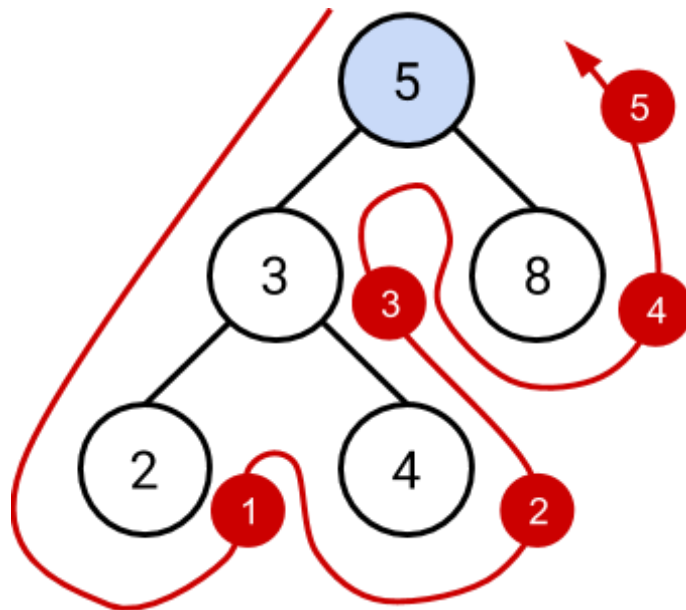
The algorithm now backtracks to 3 and moves right to 4, at which point it can progress no further. Therefore it outputs the value and backtracks again.



The algorithm backtracks from 4 to 3, which it outputs (as all of its children have been visited) and continues to 5, where it can move right to 8. It outputs 8, backtracks to 5 and outputs 5 before terminating. The order is therefore **2, 4, 3, 8, 5**.



It can be easier to think of tree traversals as **drawing a line** around the tree, outputting as the line passes the node at a particular point. In depth first traversals, nodes are output as they are passed on the right, like so:



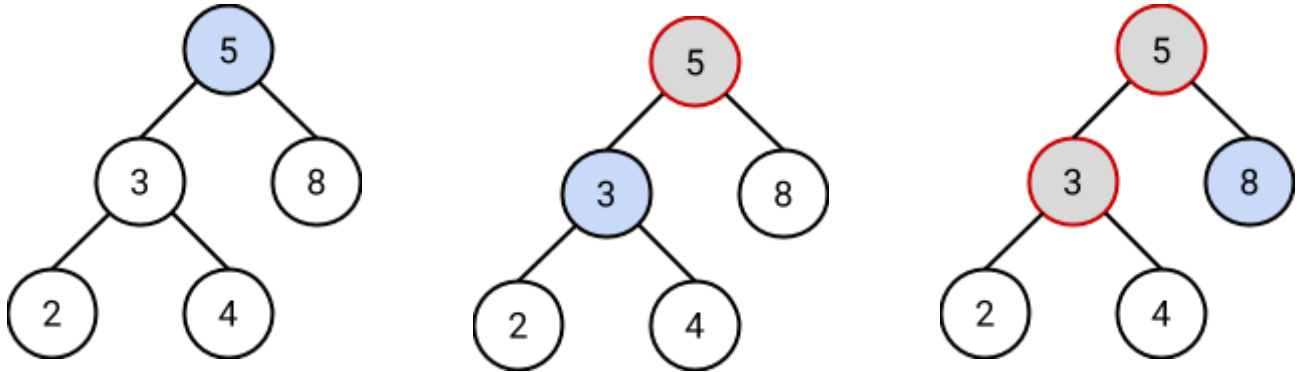
This gives the same result, **2, 4, 3, 8, 5**.



### Breadth first

Starting from the left, breadth-first visits **all the children** of the start node. The algorithm then visits all nodes **directly connected** to each of those nodes in turn, continuing until every node has been visited.

Starting at 5, which is visited immediately, the algorithm visits 3 and then 8.



As 8 has no children, the algorithm backtracks to 3 and visits its children, starting from the left. 2 and 4 are visited and the algorithm backtracks to 2, 3 and 5 before terminating.

