

**PHYSICS ADMISSIONS TEST**  
**October 2023**

**Time allowed: 2 hours**

*For candidates applying to Physics, Physics and Philosophy,  
Engineering, or Materials Science*

---

**Total 26 questions [100 Marks]**

Answers should be written on the question sheet in the spaces provided,  
and you are encouraged to show your working.  
You should attempt as many questions as you can.

**No tables, or formula sheets may be used.**

Answers should be given exactly and in simplest terms  
unless indicated otherwise.

Indicate multiple-choice answers by circling the best answer.  
Partial credit may be given for correct workings in multiple choice questions.

The numbers in the margin indicate the marks expected to be assigned  
to each question. You are advised to divide your time according to  
the marks available.

You may take the gravitational field strength  
on the surface of Earth to be  $g \approx 10 \text{ m s}^{-2}$

**Do NOT turn over until told that you may do so.**

This page is left intentionally blank

1. What speed does a bull elephant (mass 4900 kg) have to move at to have the same kinetic energy as a cyclist (mass 100 kg) moving at  $30 \text{ km h}^{-1}$ ?

[2]

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>
$0.6 \text{ m s}^{-1}$	$1.2 \text{ m s}^{-1}$	$4.2 \text{ m s}^{-1}$	$8.3 \text{ m s}^{-1}$	$16.6 \text{ m s}^{-1}$

2. A seed packet contains 100 seeds. When planted, 75 will successfully become plants, but of these only a third will have flowers, and of these only one fifth will produce fruit. How many seeds produce fruiting plants?

[2]

A	B	C	D	E
5	10	15	20	25

**3.** Two black holes orbit each other and emit gravitational waves arising from the periodic nature of the orbit. The orbital separation is around 10 km, the relative speeds of the black holes are close to the speed of light, and gravitational waves travel at the speed of light. Which of the following would best describe the frequency of the emitted radiation?

[2]

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>
$10^{-2}$ Hz	10 Hz	$10^4$ Hz	$10^7$ Hz	$10^{10}$ Hz

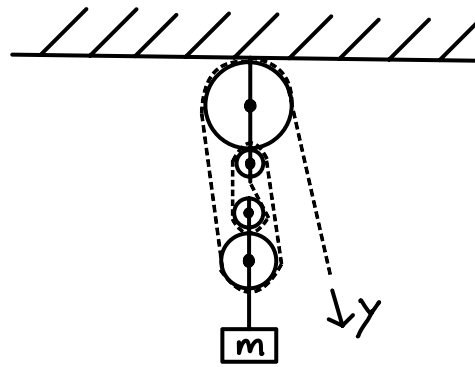
4. What is the next number in the sequence  $\frac{1}{5}, \frac{3}{25}, \frac{7}{125}, \frac{3}{125}, \frac{31}{3125}$  ?

[2]

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>
$\frac{7}{125}$	$\frac{27}{3125}$	$\frac{59}{3125}$	$\frac{59}{15625}$	$\frac{63}{15625}$

5. Consider the pulley system in the diagram, containing 4 wheels. If you pull the free end a distance  $y$ , how far will  $m$  rise by?

[2]



A	B	C	D	E
$y/16$	$y/4$	$y/2$	$2y$	$4y$

6. Consider  $f(x) = x^2$ . You want to transform the function so you get a new function  $g(x)$  stretched by a vertical scale factor of 2, with a line of symmetry about  $x = 1$  and which is never positive.  $g(x)$  would be equal to which of the following functions?

[2]

A	B	C	D	E
$-2f(x - 1)$	$-f(x - 1)$	$-2f(x + 1)$	$-f(x + 1)$	$-f(2x - 2)$



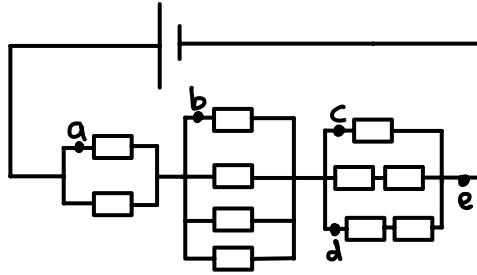
7. If  $y = \left(2 + \frac{x}{2}\right)^4$ , which of the following is  $\frac{dy}{dx}$ ?

[2]

- **A**  $4 + 2x + \frac{3x^2}{4} + \frac{x^3}{4}$
- **B**  $8 + 6x + \frac{3x^2}{2} + \frac{x^3}{8}$
- **C**  $32 + 24x + 6x^2 + \frac{x^3}{2}$
- **D**  $16 + 12x + 3x^2 + \frac{x^3}{4}$
- **E**  $2 + x + \frac{3x^2}{8} + \frac{x^3}{8}$

8. All resistors in the circuit below have the same value. If an ammeter is placed in the circuit in turn at points (a) through to (e), which of the following sets of points will give the same reading?

[2]



A	B	C	D	E
$a, b$	$a, c$	$b, e$	$c, d$	$a, b, c$

9. If  $\frac{dy}{dx} = x^2 + \frac{1}{x^3}$  and  $y = 0$  when  $x = 1$ , what is  $\int_1^3 y \, dx$ ?

[2]

A	B	C	D	E
$\frac{4}{3}$	$\frac{8}{3}$	$\frac{20}{3}$	8	$\frac{22}{3}$

**10.** A particle of mass  $m$ , travelling freely at an initial speed  $v$ , can be stopped in a distance  $d$  by a constant retarding force  $F$ . What magnitude of force (applied in a direction perpendicular to the motion) would be needed to change the trajectory of the same particle (at the same speed  $v$ ) into a circular arc of radius  $d$ ? [2]

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>
$F/2$	$F/\sqrt{2}$	$F$	$\sqrt{2}F$	$2F$

11. What is the (integer)  $m$  such that  $\sum_{n=1}^m (3 + 2n) = 140$  ?

[2]

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>
6	8	10	12	14

**12.** A device uses 3 kW of power at a voltage of 60 V. It is connected to a power supply via an ideal transformer. The transformer has  $N$  turns on the winding connected to the device and  $20N$  turns on the winding connected to the power supply. What current flows in the winding connected to the power supply?

[2]

A	B	C	D	E
1 mA	0.4 A	2.5 A	50 A	1 kA

**13.** You use some measuring scales to discover the following relationships between masses of apples (each of mass  $m_A$ ), bananas ( $m_B$ ) and carrots ( $m_C$ ):

$$2m_A + 3m_B + 4m_C = 4m_A + 3m_B + 3m_C$$

$$m_A + 4m_B + m_C = 8m_B$$

Find all combinations of apples and/or bananas that have the same mass as 5 carrots (note that only whole numbers of apples and bananas are allowed).

[6]

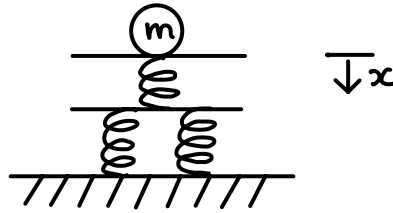
14. If  $2^{x+2y} = 16$  and  $xy = 2$ , find  $x$  and  $y$ .

[3]



15. A ball of mass  $m$  sits in equilibrium on top of a set of three identical springs of spring constant  $k$  as in the diagram (you can assume that the springs are stiff and that the ball is light). The ball is pressed down by a distance  $x$  and then released. Assuming that 90% of the stored energy is transferred to the ball, how high will the ball go above its point of release (in terms of  $m$ ,  $k$ ,  $x$  and  $g$ , where  $g$  is the acceleration due to gravity)?

[6]

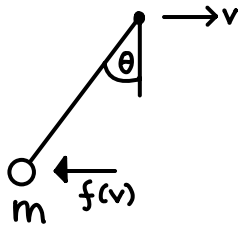


**16.** In astrophysics, the Jeans length  $\lambda_J$  is a measure of the size of a cloud of gas in which internal pressure just supports the cloud against collapse under gravity. It depends on the speed of sound in the gas,  $c_s$ , the gravitational constant  $G = 6.67 \times 10^{-11} \text{ kg}^{-1} \text{ m}^3 \text{ s}^{-2}$  and the mass density of the cloud  $\rho$ . The dependences may be expressed in the form  $\lambda_J = c_s^\alpha G^\beta \rho^\gamma$ . What values of  $\alpha$ ,  $\beta$  and  $\gamma$  are required for  $\lambda_J$  to have the correct units (or dimensions) of length?

[4]

17. A mass  $m$  on the end of a rigid rod of negligible mass hangs from a (pivot) point. The pivot point moves horizontally at speed  $v$  and the mass experiences a drag force  $f(v)$  in the direction opposite to its velocity. At speed  $v$ , the rod makes a constant angle  $\theta$  to the vertical.

- (a) Find an expression for  $f(v)$  in terms of the angle  $\theta$  that the pendulum makes to the vertical.
- (b) Sketch  $\theta$  as a function of  $v$  in the case that  $f(v)$  is proportional to  $v$ . [4]



18. A quartic polynomial function  $f(x)$  has the following properties:

$$\begin{aligned}\frac{d^2f}{dx^2} &= 0 && \text{at } x = 1 \text{ and } x = 3 \quad \mathbf{only} \\ \frac{df}{dx} &= 0 && \text{at } x = 2 \\ f(0) &= 0, \\ f(1) &= 3.\end{aligned}$$

Find  $f(x)$ .

[7]

19. Solve the following equation for real  $x$ ,

[3]

$$6e^{2x} + e^x = 15$$

**20.** A diver 5 metres under the surface of the sea looks up. They see a circle of light directly above them, where they can see what is on the surface, but outside of this circle the diver only sees a reflection of what is under the water. Explain why there is such a circle and calculate its radius. You may assume  $n_{air} = 1$  and  $n_{water} = 1.33$ .

[4]

21. Find all values of  $x$  that satisfy the equation.

[5]

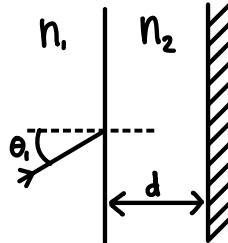
$$4 \sin x (\sin x + \cos^2 x) = 3 + \sin x$$

**22.** Two identical spacecraft of mass  $m$  are in stable circular orbits around the Earth – one at height  $R_E$  and the other at height  $2R_E$  above the surface of the Earth. What is the difference in the total energy between the two spacecraft? The radius of the Earth is  $R_E$ .

[6]



**23.** A beam of light in a medium with refractive index  $n_1$  is incident at an angle  $\theta_1$  on a slab of material of thickness  $d$  with refractive index  $n_2 > n_1$  as shown in the figure. The rear surface of the slab is mirrored and perfectly reflective.



- (a) What distance,  $l$ , does the beam transmitted into the slab travel before re-emerging from it? Express your answer in terms of  $n_1$ ,  $n_2$ ,  $\theta_1$  and  $d$ . [3]
- (b) What are the limiting values of  $l$  at large and small  $\theta_1$ ? [3]
- (c) Now consider the case in which light of wavelength (in medium 1)  $\lambda_1$  is incident normally. For what value(s) of  $d$  would light reflected from the two surfaces interfere constructively? Ignore any phase changes that might occur at reflections. [3]

**24.** A ship floating at anchor moves vertically only, as waves on the surface of the sea cause the surface height to vary with position  $x$  and time  $t$  as

$$y(x, t) = A \sin \left( \frac{2\pi}{\lambda} (x - vt) \right),$$

where  $A$ ,  $\lambda$  and  $v$  are positive constants.

- (a) What is the period  $P$  of the ship's vertical oscillations? [1]
- (b) What total vertical distance does the ship move through during a time interval equal to  $P$ ? [1]
- (c) Sketch curves for the ship's kinetic and potential energies as functions of time on the same plot, from  $t = 0$  to  $t = 2P$ . [3]

**25.** Sketch  $y = x^4 - 2x^3$  and  $y = 2x - x^2$  on the same axes, showing clearly the natures of the stationary points and labelling their coordinates. Write down an integral expression for the finite area enclosed between the two curves (you do not need to evaluate the integral).

[7]

**26.** Two separate pairs of unbiased dice are rolled. One pair consists of two eight-sided dice (with faces numbered 1-8). The other pair consists of one six-sided die (with faces numbered 1-6) and one ten-sided die (with faces numbered 1-10).

- (a) Which pair is most likely to show a total of 16? [1]
- (b) Are any totals equally likely to be rolled using the two pairs of dice? [1]
- (c) What is the smallest total that is more probable when using the pair consisting of 8-sided dice? [1]
- (d) Which pair is more likely to give a total that is divisible by 3? [2]
- (e) Given that at least one of the eight-sided dice has landed 5, is a total of 11 or 10 more likely? Give a reason for your answer. [2]

This page intentionally left blank for working.

This page intentionally left blank for working.