



GCSE MATHEMATICS

S21-C300

With Calculator Assessment Resource L

Higher Tier

Formula list

Area and volume formulae

Where r is the radius of the sphere or cone, l is the slant height of a cone and h is the perpendicular height of a cone:

Curved surface area of a cone =
$$\pi rl$$

Surface area of a sphere = $4\pi r^2$
Volume of a sphere = $\frac{4}{3}\pi r^3$
Volume of a cone = $\frac{1}{3}\pi r^2h$

Kinematics formulae

Where *a* is constant acceleration, *u* is initial velocity, *v* is final velocity, *s* is displacement from the position when t = 0 and *t* is time taken:

v = u + at $s = ut + \frac{1}{2}at^{2}$ $v^{2} = u^{2} + 2as$

1. Marie works for an optician. She records the depth of a lens in each of the 100 pairs of glasses on display.



Her results are summarised in the table.

Depth of lens, <i>x</i> mm, to the nearest mm	Number of pairs of glasses
10 ≤ <i>x</i> < 20	5
20 ≤ <i>x</i> < 30	20
30 <i>≤ x <</i> 40	23
40 ≤ <i>x</i> < 50	52

(i) Calculate an estimate for the mean depth of a lens. (a)

[4]

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(ii)	In which group does the median lie?	[1]
	. .	

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(b) In the display of 100 pairs of glasses at *Davy's Opticians*, the mean depth of a lens is exactly the same as Marie's opticians.

Marie says,

"Considering only the mean depth of a lens, our display is **certain** to be very similar to the display in *Davy's Opticians.*"

Explain why Marie is incorrect.

[1]

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	Expand and simplify $(x + 6y)(3x + 5y)$.	[3]
(b)	Factorise $x^2 - 13x + 36$.	[2]
(c)	Solve $w^2 + 7w - 18 = 0$.	[3]
(d)	Factorise $y^2 - 121$.	[1]
(e)	You are given that: • $y = x^2 + bx + c$ • $y = 16$ when $x = 0$ • $y = 0$ when $x = -2$ Find the values of <i>b</i> and <i>c</i> .	[4]

 7 cartons of apple juice and 2 cartons of grapefruit juice cost £6.15 altogether. 5 cartons of apple juice and 8 cartons of grapefruit juice cost £9.19 altogether. Use an algebraic method to calculate the total cost of 2 cartons of apple juice and 	
5 cartons of grapefruit juice.	[5]

Total cost of 2 cartons of apple juice and 5 cartons of grapefruit juice is £

4. Find the *n*th term of the following sequence.

-7, -4, 1, 8, 17,

5. (a) The diagram shows a sketch of y = f(x).

On the same diagram, sketch the curve y = -f(x). Mark clearly the coordinates of any point where this curve crosses an axis.

[2]



(b) The diagram shows a sketch of y = g(x + 2).

On the same diagram, sketch the curve y = g(x - 1). Mark clearly the coordinates of the points where this curve crosses the *x*-axis. [3]



(c) Enlarge the triangle, shown on the grid below, by a scale factor of $-\frac{1}{2}$ with (2, 1) as the centre of the enlargement. [2]



6. A cone has a radius *x* cm, a perpendicular height (x + 2) cm and a slant height 16.4 cm.



Diagram not drawn to scale

Show that x satisfies the equation $x^2 + 2x - 132 \cdot 48 = 0$ and calculate the volume of the cone. You must show all your working. [7]