

Additional Assessment Materials
Summer 2021

Pearson Edexcel GCE in As Mathematics 8MA0_01 (Public release version)

Resource Set 1: Topic 5

Trigonometry

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General guidance to Additional Assessment Materials for use in 2021

Context

- Additional Assessment Materials are being produced for GCSE, AS and A levels (with the exception of Art and Design).
- The Additional Assessment Materials presented in this booklet are an optional part of the range of evidence teachers may use when deciding on a candidate's grade.
- 2021 Additional Assessment Materials have been drawn from previous examination materials, namely past papers.
- Additional Assessment Materials have come from past papers both published (those materials available publicly) and unpublished (those currently under padlock to our centres) presented in a different format to allow teachers to adapt them for use with candidate.

Purpose

- The purpose of this resource to provide qualification-specific sets/groups of questions covering the knowledge, skills and understanding relevant to this Pearson qualification.
- This document should be used in conjunction with the mapping guidance which will map content and/or skills covered within each set of questions.
- These materials are only intended to support the summer 2021 series.

1.

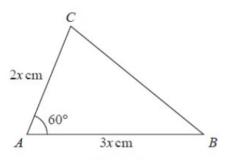


Figure 1

Figure 1 shows a sketch of a triangle ABC with AB = 3x cm, AC = 2x cm and angle $CAB = 60^{\circ}$

Given that the area of triangle ABC is $18\sqrt{3}$ cm²

(a) show that $x = 2\sqrt{3}$

(3)

(b) Hence find the exact length of BC, giving your answer as a simplified surd.

(3)

(Total for Question 1 is 6 marks)

2.

. (i) Solve, for $-90^{\circ} \leqslant \theta < 270^{\circ}$, the equation,

$$\sin(2\theta + 10^{\circ}) = -0.6$$

giving your answers to one decimal place.

(5)

(Total for Question 2 is 5 marks)

3.

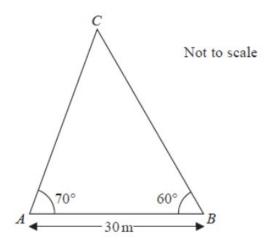


Figure 1

A triangular lawn is modelled by the triangle ABC, shown in Figure 1. The length AB is to be 30 m long.

Given that angle $BAC = 70^{\circ}$ and angle $ABC = 60^{\circ}$,

(a) calculate the area of the lawn to 3 significant figures.

(4)

(b) Why is your answer unlikely to be accurate to the nearest square metre?

(1)

(Total for Question 3 is 5 marks)

4.

In a triangle ABC, side AB has length 10 cm, side AC has length 5 cm, and angle BAC = θ where θ is measured in degrees. The area of triangle ABC is 15 cm²

(a) Find the two possible values of $\cos \theta$

(4)

Given that BC is the longest side of the triangle,

(b) find the exact length of BC.

(2)

(Total for Question 4 is 5 marks)

Solve, for $360^{\circ} \leqslant x < 540^{\circ}$,

$$12\sin^2 x + 7\cos x - 13 = 0$$

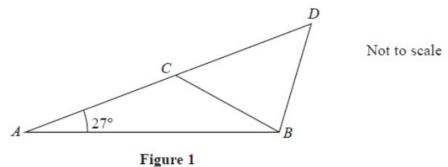
Give your answers to one decimal place.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(5)

(Total for Question 5 is 5 marks)

6.



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Figure 1 shows the design for a structure used to support a roof.

The structure consists of four steel beams, AB, BD, BC and AD.

Given $AB = 12 \,\text{m}$, $BC = BD = 7 \,\text{m}$ and angle $BAC = 27^{\circ}$

(a) find, to one decimal place, the size of angle ACB.

(3)

The steel beams can only be bought in whole metre lengths.

(b) Find the minimum length of steel that needs to be bought to make the complete structure.

(3)

Total for Question 6 is 6 marks)

7.

(ii) (a) A student's attempt at the question

"Solve, for
$$-90^{\circ} < x < 90^{\circ}$$
, the equation $7 \tan x = 8 \sin x$ "

is set out below.

$$7 \tan x = 8 \sin x$$

$$7 \times \frac{\sin x}{\cos x} = 8 \sin x$$

$$7 \sin x = 8 \sin x \cos x$$

$$7 = 8 \cos x$$

$$\cos x = \frac{7}{8}$$

$$x = 29.0^{\circ} \text{ (to 3 sf)}$$

Identify two mistakes made by this student, giving a brief explanation of each mistake.

(2)

(b) Find the smallest positive solution to the equation

$$7\tan(4\alpha + 199^\circ) = 8\sin(4\alpha + 199^\circ)$$
(2)

Total for Question 7 is 4 marks)

8.

(a) Show that

$$\frac{10\sin^2\theta - 7\cos\theta + 2}{3 + 2\cos\theta} \equiv 4 - 5\cos\theta \tag{4}$$

(b) Hence, or otherwise, solve, for $0 \le x < 360^{\circ}$, the equation

$$\frac{10\sin^2 x - 7\cos x + 2}{3 + 2\cos x} = 4 + 3\sin x \tag{3}$$

Total for Question 8 is 7 marks)

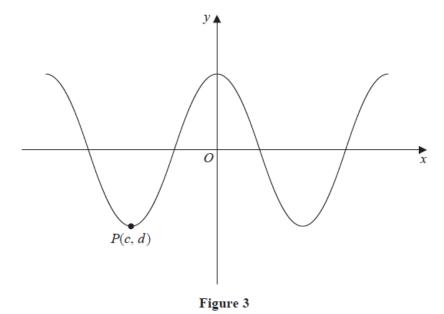


Figure 3 shows part of the curve with equation $y = 3\cos x^{\circ}$.

The point P(c, d) is a minimum point on the curve with c being the smallest negative value of x at which a minimum occurs.

(a) State the value of c and the value of d.

(1)

(b) State the coordinates of the point to which P is mapped by the transformation which transforms the curve with equation $y = 3\cos x^{\circ}$ to the curve with equation

(i)
$$y = 3\cos\left(\frac{x^{\circ}}{4}\right)$$

(ii)
$$y = 3\cos(x - 36)^{\circ}$$

(2)

(c) Solve, for $450^{\circ} \le \theta < 720^{\circ}$,

$$3\cos\theta = 8\tan\theta$$

giving your solution to one decimal place.

In part (c) you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(5)

. (a) Show that the equation

$$4\cos\theta - 1 = 2\sin\theta\tan\theta$$

can be written in the form

$$6\cos^2\theta - \cos\theta - 2 = 0$$

(4)

(b) Hence solve, for $0 \le x < 90^{\circ}$

$$4\cos 3x - 1 = 2\sin 3x \tan 3x$$

giving your answers, where appropriate, to one decimal place.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(4)

Total for Question 10 is 8 marks)