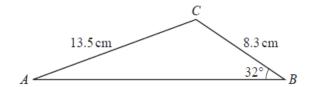


A Level Mathematics A

H240/03 Pure Mathematics and Mechanics

Question Set 3



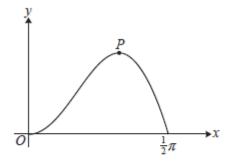
The diagram shows triangle ABC, with $AC = 13.5 \,\text{cm}$, $BC = 8.3 \,\text{cm}$ and angle $ABC = 32^{\circ}$.

- A circle with centre C has equation $x^2 + y^2 6x + 4y + 4 = 0$.
 - (a) Find

- (b) Determine the set of values of k for which the line y = kx 3 does not intersect or touch the circle. [5]
- (a) In this question you must show detailed reasoning.

Solve the inequality
$$|x-2| \le |2x-6|$$
. [4]

(b) Give full details of a sequence of two transformations needed to transform the graph of y = |x-2| to the graph of y = |2x-6|. [3]



The diagram shows the part of the curve $y = 3x \sin 2x$ for which $0 \le x \le \frac{1}{2}\pi$.

The maximum point on the curve is denoted by P.

- (a) Show that the x-coordinate of P satisfies the equation $\tan 2x + 2x = 0$. [3]
- (b) Use the Newton-Raphson method, with a suitable initial value, to find the x-coordinate of P, giving your answer correct to 4 decimal places. Show the result of each iteration. [4]
- (c) The trapezium rule, with four strips of equal width, is used to find an approximation to $\int_0^{\frac{1}{2}\pi} 3x \sin 2x \, dx.$

Show that the result can be expressed as $k\pi^2(\sqrt{2}+1)$, where k is a rational number to be determined. [4]

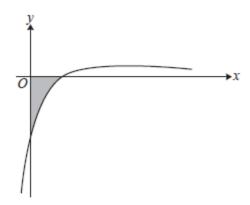
(d) (i) Evaluate
$$\int_{0}^{\frac{1}{2}\pi} 3x \sin 2x \, dx$$
. [1]

- (ii) Hence determine whether using the trapezium rule with four strips of equal width gives an under- or over-estimate for the area of the region enclosed by the curve $y = 3x \sin 2x$ and the x-axis for $0 \le x \le \frac{1}{2}\pi$. [1]
- (iii) Explain briefly why it is not easy to tell from the diagram alone whether the trapezium rule with four strips of equal width gives an under- or over-estimate for the area of the region in this case.

5 In this question you must show detailed reasoning.

(a) Prove that
$$(\cot \theta + \csc \theta)^2 = \frac{1 + \cos \theta}{1 - \cos \theta}$$
. [4]

(b) Hence solve, for
$$0 < \theta < 2\pi$$
, $3(\cot \theta + \csc \theta)^2 = 2\sec \theta$. [5]



The diagram shows part of the curve $y = \frac{2x-1}{(2x+3)(x+1)^2}$.

Find the exact area of the shaded region, giving your answer in the form $p+q \ln r$, where p and q are positive integers and r is a positive rational number. [10]

Total Marks for Question Set 3: 50 Marks



work is used in this paper. To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced in the OCR Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download from our public website (www.ocr.org.uk) after the live examination series.

If OCR has unwittingly failed to correctly acknowledge or clear any third-party content in this assessment material, OCR will be happy to correct its mistake at the earliest possible opportunity.

For queries or further information please contact The OCR Copyright Team, The Triangle Building, Shaftesbury Road, Cambridge CB2 8EA.

OCR is part of the Cambridge Assessment Group; Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge