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Additional Assessment Materials
Summer 2021

Pearson Edexcel GCE in Mathematics 9MA0 (Public release version)

Resource Set 1: Topic 3
Coordinate Geometry

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## General guidance to Additional Assessment Materials for use in 2021

 Context- Additional Assessment Materials are being produced for GCSE, AS and A levels (with the exception of Art and Design).
- The Additional Assessment Materials presented in this booklet are an optional part of the range of evidence teachers may use when deciding on a candidate's grade.
- 2021 Additional Assessment Materials have been drawn from previous examination materials, namely past papers.
- Additional Assessment Materials have come from past papers both published (those materials available publicly) and unpublished (those currently under padlock to our centres) presented in a different format to allow teachers to adapt them for use with candidate.


## Purpose

- The purpose of this resource to provide qualification-specific sets/groups of questions covering the knowledge, skills and understanding relevant to this Pearson qualification.
- This document should be used in conjunction with the mapping guidance which will map content and/or skills covered within each set of questions.
- These materials are only intended to support the summer 2021 series.

1. A curve has parametric equations

$$
x=6 t+1, \quad y=5-\frac{4}{3 t}, \quad t \neq 0 .
$$

Show that the Cartesian equation of the curve can be expressed in the form

$$
y=\frac{a x+b}{x-1}, \quad x \neq k
$$

where $a, b$ and $k$ are constants to be found.
2. A circle $C$ has equation

$$
x^{2}+y^{2}-4 x+10 y=k
$$

where $k$ is a constant.
(a) Find the coordinates of the centre of $C$.
(b) State the range of possible values for $k$.
3.


Figure 1
Figure 1 shows a rectangle $A B C D$.
The point $A$ lies on the $y$-axis and the points $B$ and $D$ lie on the $x$-axis as shown in Figure 1.
Given that the straight line through the points $A$ and $B$ has equation $5 y+2 x=10$,
(a) show that the straight line through the points $A$ and $D$ has equation $2 y-5 x=4$,
(b) find the area of the rectangle $A B C D$.
(Total for Question 3 is 7 marks)
4. A curve $C$ has parametric equations

$$
x=2 t-1, y=4 t-7+\frac{3}{t}, \quad t \neq 0
$$

Show that the Cartesian equation of the curve $C$ can be written in the form

$$
y=\frac{2 x^{2}+a x+b}{x+1}, \quad x \neq-1
$$

where $a$ and $b$ are integers to be found.
5.


Figure 3

The circle $C$ has centre $A$ with coordinates $(7,5)$.
The line $l$, with equation $y=2 x+1$, is the tangent to $C$ at the point $P$, as shown in Figure 3.
(a) Show that an equation of the line $P A$ is $2 y+x=17$.
(b) Find an equation for $C$.

The line with equation $y=2 x+k, k \neq 1$, is also a tangent to $C$.
(c) Find the value of the constant $k$.
6.


Figure 2
The curve $C_{1}$ with parametric equations

$$
x=10 \cos t, \quad y=4 \sqrt{2} \sin t, \quad 0 \leqslant t<2 \pi
$$

meets the circle $C_{2}$ with equation

$$
x^{2}+y^{2}=66
$$

at four distinct points as shown in Figure 2.
Given that one of these points, $S$, lies in the 4th quadrant, find the Cartesian coordinates of $S$.
7.


Figure 4
A circle with centre $(9,-6)$ touches the $x$-axis as shown in Figure 4.
(a) Write down an equation for the circle.

A line $l$ is parallel to the $x$-axis. The line $l$ cuts the circle at points $P$ and $Q$.
Given that the distance $P Q$ is 8 ,
(b) find the two possible equations for $l$.
8. A curve $C$ has parametric equations

$$
x=3+2 \sin t, \quad y=4+2 \cos 2 t, \quad 0 \leq t<2 \pi .
$$

(a) Show that all points on $C$ satisfy $y=6-(x-3)^{2}$.
(b) (i) Sketch the curve $C$.
(ii) Explain briefly why $C$ does not include all points of $y=6-(x-3)^{2}, x \in \mathbb{R}$.

The line with equation $x+y=k$, where $k$ is a constant, intersects $C$ at two distinct points.
(c) State the range of values of $k$, writing your answer in set notation.

