

1. (a) (i)  $C_p = 2 + 4 = 6 \mu\text{F}$  A1
- (ii)  $1/C = 1/2 + 1/4$  C1  
 $C_s = 4/3 = 1.33 \mu\text{F}$  A1
- (b) (i) 6.0 V A1
- (ii)  $Q = C_p V$  C1  
 $= 6 \times 6 = 36 \mu\text{C}$  A1
- (c)  $E = \frac{1}{2} C_s V^2$  C1  
 $= 24 \times 10^{-6}$  A1
- (d) (i) The capacitors discharge through the voltmeter. B1
- (ii)  $V = V_0 e^{-t/CR}$   
 $1/4 = e^{-t/(6 \times 12)}$  C1  
 $\ln 4 = t / 72$  C1  
 $t = 72 \ln 4 \approx 100 \text{ s}$  A1
- [12]**
2. (a)  $Q_0 = CV = 1.2 \times 10^{-11} \times 5.0 \times 10^3; = 6.0 \times 10^{-8}; \text{C (3)}$  3
- (b) (i)  $RC = 1.2 \times 10^{15} \times 1.2 \times 10^{-11} \text{ or } = 1.44 \times 10^4 \text{ (s) (1)}$  1
- (ii)  $I = V/R = 5000/1.2 \times 10^{15} \text{ or } = 4.16 \times 10^{-12} \text{ (A) (1)}$  1
- (iii)  $t = Q_0/I; = 6 \times 10^{-8} / 4.16 \times 10^{-12} = 1.44 \times 10^4 \text{ (s)}$  2
- (iv)  $Q = Q_0 e^{-1}; Q = 0.37 Q_0 \text{ so } Q \text{ lost} = 0.63 Q_0$  2
- (c) (i) capacitors in parallel come to same voltage (1)  
so Q stored  $\propto$  C of capacitor (1)  
capacitors in ratio  $10^3$  so only  $10^{-3} Q_0$  left on football (1) 3
- (ii)  $V = Q/C = 6.0 \times 10^{-8} / 1.2 \times 10^{-8} \text{ or } 6.0 \times 10^{-11} / 1.2 \times 10^{-11} \text{ or only } 10^{-3}$   
Q left so  $10^{-3} V$  left; = 5.0 (V) 2

3. (a) (i)  $Q = VC$ ;  $W = \frac{1}{2} VC.V (= \frac{1}{2} CV^2)$  (2)  
 (ii) parabolic shape passing through origin (1)  
 plotted accurately as  $W = 1.1 V^2$  (1) 4
- (b) (i)  $T = RC$ ;  $= 6.8 \times 10^3 \times 2.2 = 1.5 \times 10^4 \text{ s} = 4.16 \text{ h}$  2  
 (ii)  $\Delta W = \frac{1}{2} C(V_1^2 - V_2^2) = 1.1(25 - 16)$ ;  $= 9.9 \text{ (J)}$  2
- (iii)  $4 = 5 \exp(-t/1.5 \times 10^4)$ ; giving  $t = 1.5 \times 10^4 \times \ln 1.25 = 3.3 \times 10^3 \text{ (s)}$  2
- (iv)  $P = \Delta W/\Delta t = 9.9/3.3 \times 10^3 = 3.0 \text{ mW}$  *ecf b(ii) and (iii)* 1  
*allow*  $P = V_{av}^2/R = 4.5^2/6.8 \times 10^3 = 2.98 \text{ mW}$

[11]

4. (a) (i)

capacitor	capacitance / $\mu\text{F}$	charge / $\mu\text{C}$	p.d. / V	energy / $\mu\text{J}$
X	5	30	$= Q/C$ $= 6 \text{ (V) (1)}$	$= \frac{1}{2} CV^2(1)$ $= \frac{1}{2} \times 5 \times 6^2$ $= 90 \text{ (1)}$
Y	25	$= CV$ $= 25 \times 6$ $= 150 \text{ (}\mu\text{C) (1)}$	$= 6 \text{ (V) (1)}$	$= 450 \text{ (1)}$
Z	10	$30 + 150 =$ $180 \text{ (}\mu\text{C) (1)}$	$= Q/C$ $= 180/10$ $= 18 \text{ (V) (1)}$	$= 1620 \text{ (1)}$

Each box correctly calculated scores (1) + (1) for  $\frac{1}{2} CV^2$  9

- (ii) 1  $18 \text{ V} + 6 \text{ V} = 24 \text{ (V) (1)}$   
 2  $180 \text{ (}\mu\text{C) (1)}$   
 3  $180 / 24 = 7.5 \text{ (1)}$   
 4  $90 + 450 + 1620 = 2160 \text{ (}\mu\text{J) (1)}$  4
- (b) (i) Kirchoff's second law OR conservation of energy (1) 1  
 (ii) Kirchoff's first law OR conservation of charge (1) 1
- (c) (i) time constant =  $CR$  (1)  
 $= 7.5 \times 10^{-6} \times 200\,000 = 1.5 \text{ (s) (1)}$  2
- (ii)  $Q = Q_0 e^{-\frac{4CR}{CR}}$  (1)

$$Q/Q_0 = e^{-4} = 0.0183 \text{ (1)}$$

2

**[19]**

5. (i)  $C_p = C + C = 6 \mu\text{F}$ ;  $1/C_s = 1/2C + 1/C = 3/2C$  giving  $C_s = 2C/3 = (2 \mu\text{F})$

3

(ii) 2 sets of (3 in series) in parallel/ 3 sets of (2 in parallel) in series

2

**[5]**