## Module 2 4.2.1

## **Circular Motion**

- <u>Candidates should be able to</u> :
  - Define the **radian**.
  - Convert angles from degrees into radians and vice versa.
  - **Explain** that a force perpendicular to the velocity of an object will make the object describe a circular path.
  - Explain what is meant by centripetal acceleration and centripetal force.
  - Select and apply the equations for :



• Select and apply the equation for :

Centripetal force :



*Circular motion* is an integral part of our everyday experience. Most of our transport makes use of the wheel to convert rotational into linear motion.



Music and film is readily available to us courtesy of spinning CD's and DVD's, and many fairground rides, such as the Big Wheel, thrill us by giving us a real feel of the centripetal force.





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Circular motion is as common to our description of the atom as it is to that of the motion of planets and galaxies.





UN	IT <i>G</i> 484	Module 2	4.2.1	<b>Circular Motion</b>	5	Cyclists racing in the Olympic		3
• 1 2	<ul> <li>PRACTICE QUESTIONS (1)</li> <li>Calculate the angular displacement of the tip of the minute hand on a watch in (i) Degrees and (ii) Radians, in a time of : <ul> <li>(a) 5 minutes, (b) 15 minutes, (c) 1 hour.</li> </ul> </li> <li>(a) Calculate the number of radians in : (i) 60°, (ii) 145°.</li> <li>(b) Calculate the number of degrees in : (i) 0.8 radian. (ii) π/4 radian.</li> <li>(c) Express 30°, 60° and 90° as multiples of π radians.</li> </ul>					<ul> <li>veloarone of ren reach speeds</li> <li>of 18 m s<sup>-1</sup> on bikes having wheels of diameter 700 mm.</li> <li>Calculate :</li> <li>(a) The time taken for one complete revolution of the wheels.</li> <li>(b) (i) The rotational frequence (ii) The number of complete in 4 minutes.</li> <li>(iii) The distance travelle</li> </ul>	The wheels. The productions made the formula of the cyclist in 4 o	heels. bras made by the wheels
3	<ul> <li>The wheels on a racing car turn at a frequency of 10 Hz. Calculate</li> <li>(a) The time period (T).</li> <li>(b) The angular displacement in radians in a time of : <ul> <li>(i) 25 ms,</li> <li>(ii) 100 ms.</li> </ul> </li> <li>At some point in the past, when the Earth was in its initial stages of formation, it took 18 hours to complete one revolution about its axis. Given that the Earth's diameter is 12800 km, calculate : <ul> <li>(a) The speed of rotation of a point on the equator.</li> <li>(b) The angular displacement of this point in a time of 30 minutes, (i) in radians and (ii) in degrees.</li> </ul> </li> </ul>				6	<ul> <li>The Earth has an orbits the Sun at an average radius of 1.5 x 10<sup>11</sup> m. Given that it completes its orbit in 365.3 days, calculate the Earth's orbital :</li> <li>(a) Frequency.</li> <li>(b) Linear speed.</li> <li>(c) Angular speed in radians per second.</li> </ul>		
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Consider a ball attached to the end of a string and whirled in a horizontal circle at constant speed (v).

- The ball's velocity is always directed along the tangent to the circle (i.e. at **90°** to the string).
- Since the speed is constant, the magnitude of the velocity stays the same, but the direction of the velocity is continually changing.
- Since a change in direction constitutes an acceleration, the ball has an acceleration which is directed towards the centre of the circular path.

This is the CENTRIPETAL ACCELERATION (a<sub>c</sub>).

• According to NEWTON'S FIRST LAW, an object continues to move in a straight line unless a resultant force acts on it.

In this case the resultant force, which is called the **CENTRIPETAL FORCE (F**<sub>c</sub>), acts on the ball towards the centre of the circle giving it a **CENTRIPETAL ACCELERATION**.

The centripetal force is provided by the tension in the string.



• The centripetal force does NO WORK on the object moving in a circular path. This is because it acts at right angles to the object's direction of motion, so there is no actual motion in the force direction.

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L1 G464     Module 2     4.2.1     Circular Motion					
EXAMPLES OF CENTRIPETAL FORCE					
Situ	ation in which a cer force acts	ntripetal	What provides the centripetal force		
A plane: around	A planet in orbit around the Sun.		The gravitational attraction force acting between the planet and the Sun.		
An object on the Earth's surface.			The force of gravity acting the object (i.e. its weight).	g on	
A car ro bend in	bunding a the road.		The frictional force acting between the tyres and the	road.	
An elect	tron in orbit the nucleus.	Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Restance Res	The electrostatic attractic force acting between the negatively charged electro and the positively charged nucleus.	on n	
Charged moving magneti at right directio of the p	d particles through a ic field acting angles to the on of motion particles.		The magnetic force acting the charged particles.	on	



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UNI	T G484	Module 2	4.2.1	<b>Circular Motion</b>	4	Venus orbits the Sun once every 7			
•	HOMEWORK QUESTIONS A proton of mass $1.67 \times 10^{-27} kg$ moving at a constant speed of					225 days at an average distance of $1.05 \times 10^{11}$ m. Given that the mass of Venus is $4.92 \times 10^{24}$ kg, Calculate :			
	<ul> <li>2.5 x 10<sup>7</sup> m s<sup>-1</sup> enters a uniform magnetic field at right angles to its path and as a result it is caused to move in a circular path of radius 275 mm. Calculate for the proton :</li> <li>(a) The <i>time taken</i> for 1 complete orbit.</li> </ul>					<ul> <li>(a) Its orbital speed.</li> <li>(b) Its centripetal acceleration.</li> <li>(c) The gravitational force exerted on Venus by the Sun.</li> </ul>			
	(b) The <i>centripetal acceleration.</i> (c) The <i>force</i> exerted on it by the magnetic field.					A pulley wheel of			
2	An objec (a) (b)	t moves in a circular path The <i>velocity</i> of the obje though its speed remain The object <i>accelerates</i> constant.	n at <i>const</i> a act is cont s constant even thou	ant speed. Explain why : inually changing even gh its speed remains		diameter 24 mm fitted to an electric motor in a machine rotates at a frequency of 30 Hz. A belt fitted to the wheel is used to drive a drum in the machine as shown opposite. (a) Calculate :			
3	The turning circle of an aircraft, when flying horizontally at a constant speed of 600 m s <sup>-1</sup> , has a radius of 65 km. Given that the total mass of the aircraft is $1.2 \times 10^4$ kg, Calculate the ratio of centripetal force to weight for the aircraft. Take $g = 9.81$ N kg <sup>-1</sup> .					<ul> <li>(i) The speed of the belt on the wheel.</li> <li>(ii) The centripetal acceleration of the belt attached to the wheel as it moves round the 24 mm pulley wheel.</li> <li>(b) The belt drives the drum via another pulley wheel of diameter 60 mm attached to the drum axle. Calculate : <ul> <li>(i) The frequency of rotation of the 60 mm pulley wheel.</li> <li>(ii) The centripetal acceleration of the belt as it passes round the 60 mm pulley wheel.</li> </ul> </li> </ul>			

