

OCR Maths M2

Topic Questions from Papers

Projectiles

Answers

<b>1</b>		$v^2 = 2 \times 9.8 \times 10$	M1		energy: $\frac{1}{2}mv^2 = \frac{1}{2}mu^2 + mgh$	
		$v = 14$	A1		$\frac{1}{2}v^2 = \frac{1}{2}.36 + 9.8 \times 10$	
		speed = $\sqrt{(14^2 + 6^2)}$	M1		(must be $6^2$ ) $v^2 = 36 + 196 = 232$	
		speed = $15.2 \text{ ms}^{-1}$	A1			
		$\tan\theta = 14/6$	M1		$\cos^{-1}(6/15.2)$ etc	
		$\theta = 66.8^\circ$ (below) horiz.	A1	6	or $23.2^\circ$ to the vertical	<b>6</b>

(Q2, June 2005)

<b>2</b>	(i)	$x = 49\cos\theta \cdot t$	B1			
		$y = 49\sin\theta \cdot t - \frac{1}{2} \cdot 9.8 \cdot t^2$	B1			
		$y = x\tan\theta - 4.9x^2/49^2 \cdot \cos^2\theta$	M1		aef (eliminating t)	
		$y = x\tan\theta - x^2(1+\tan^2\theta)/490$	A1	4	AG	
	(ii)	$30 = 70\tan\theta - 10(1+\tan^2\theta)$	M1			
		$\tan\theta = (70 \pm \sqrt{3300}) \div 20$	M1		(6.37/0.628)	
		$81.1^\circ$	A1		$\theta_1$ or $\theta_2$	
		$32.1^\circ$	A1	4	“	
	(iii)	$x^2(1+\tan^2\theta)/490 = x\tan\theta$	M1		set $y = 0$	
		$x = 490\tan\theta/(1+\tan^2\theta)$	A1			
		$x = 75.0$	A1			
		$x = 221$ (220.6)	A1			
		$d = 146 \text{ m}$	A1	5	✓	<b>13</b>
			✓			
	(iii)	Alternatively (1 <sup>st</sup> 2 marks)				
		$t = 49\sin\theta/4.9$ and (9.88/5.31) $x = 49\cos\theta \cdot t$	M1		$s = ut + \frac{1}{2}at^2$ and $x = 49\cos\theta \cdot t$ or $R = u^2\sin 2\theta/g$ (precise)	
		$x = 490\sin\theta\cos\theta$	A1		$245\sin 2\theta$	

(Q8, June 2005)

<b>3</b>	(i)	$0 = 50 \sin 25^\circ t - 4.9t^2$	M1		or $0 = 50\sin 25^\circ - 9.8t$ & $2t : 2 \times 2.16$	
			A1			
		$t = 4.31 \text{ s}$	A1	3		
	(ii)	$d = 50\cos 25^\circ \times 4.31$	M1		or $u^2\sin(2 \times 25^\circ)/g$	
		$195 \text{ m}$	A1 ✓	2	✓ $50\cos 25^\circ \times$ their t	<b>5</b>

(Q2, Jan 2006)

4	(i)	$x = 7t$	B1		
		$y = -4.9t^2$ or $-\frac{1}{2}gt^2$	M1		some attempt at vertical motion
			A1		sc $y = x \tan \theta - \frac{gx^2}{2V^2 \cos^2 \theta}$
		$y = -x^2/10$ <b>AG</b> (no fiddles)	A1	4	with $\theta=0$ M1 then A1 (max = 2)
	(ii)	$-20 = -x^2/10$	M1		or $t = \sqrt{(20/4.9)}$ & $x=7t$
		14.1 m	A1	2	sc B1 for 14.1 after wrong work
	(iii)	$\frac{1}{2}mv^2 = \frac{1}{2}m7^2 + mgx20$ n.b. $v^2 = u^2$	M1		<b>OR</b> $v_h = 7$ (B1)
		+2as gets M0	A1		$v_v = \pm 19.8$ (B1) $14\sqrt{2}, 2\sqrt{98}$ etc
	$v = 21 \text{ ms}^{-1}$	A1		$v = 21$ (B1)	
	$dy/dx = -2x/10$ & $\tan \theta$	M1		<b>OR</b> $\tan \theta = 19.8/7$ or	
		A1		$\cos \theta = 7/21$ or $\sin \theta = 19.8/21$	
	70.5° to horizontal	A1	6	or 19.5° to vertical	<b>12</b>

(Q6, Jan 2006)

5	(i)	$v \sin 50^\circ$	B1	3	initial vertical component or $mx9.8 \times 13 = \frac{1}{2}m(v \sin 50^\circ)^2$
		$0 = v^2 \sin^2 50^\circ - 2 \times 9.8 \times 13$ (must be 13)	M1		
		$v = 20.8 \text{ ms}^{-1}$	A1		
	(ii)	$45 = v \cos 50^\circ \cdot t$	M1	6	sin/cos mix ok for above M1 see alternative below other methods include other $t_s$
	$t = 3.36$ ✓ their v (3.13 for $v=22.4$ )	A1 ✓			
	$s = v \sin 50^\circ \times t - \frac{1}{2} \times 9.8 \times t^2$	M1			
	$s = -1.6$ to $-2.0$ inclusive (-1.68)	A1			
		ht above ground = 0.320 m	A1		ignore ht adjustments can be their v and their t can be implied from next A1
	(iii)	$v_v = v \sin 50^\circ - 9.8 \times t$	M1	4	or $v_v^2 = 2g(15 - \text{their ans to ii})$ ✓ above for $v_v$
	$v_v = -17.0$ ✓ their v, t (-13.5 for 22.4)	A1 ✓			
speed = $\sqrt{(v_v^2 + (v \cos 50^\circ)^2)}$	M1				
	speed = $21.6 \text{ ms}^{-1}$ ✓ their v and $v_v$ (19.7 for $v = 22.4$ )	A1 ✓		or $\frac{1}{2}mv^2 - mgx1.68 = \frac{1}{2}m \times 20.8^2$ (4 marks) M1/A1 ✓ s,v /M1 solve/ A1 ✓	
(ii)	$y = x \tan \theta - \frac{gx^2}{2v^2 \cos^2 \theta}$	B1	13	<b>Alternative 1<sup>st</sup> 5 marks</b> substitute v and $50^\circ$ and $x=45$	
	$y = 45 \tan 50^\circ - \frac{9.8 \times 45^2}{2 \cdot v^2 \cos^2 50^\circ}$	M1			
	calculate y	A1			
	$y = -1.6$ to $-2.0$ inclusive	A1			
		A1		can be their v should be $-1.68$	

(Q7, June 2006)

6	(i)	$v_v = 42\sin 30^\circ (=21)$	B1		
		$0 = 21^2 - 2 \times 9.8xh$	M1		
		$h = 22.5$	A1	3	
	(ii)	$v_h = 42\cos 30^\circ (=36.4)$	B1		
		$v_v = \pm v_h \times \tan 10^\circ$	M1		
		$v_v = \pm 6.41$ or $21\sqrt{3} \tan 10^\circ$	A1		or $42\cos 30^\circ \cdot \tan 10^\circ$
		$-6.41 = 42\sin 30^\circ - 9.8t$	M1	**	must be $-6.41$ (also see "or" x 2)
		$t = 2.80$	A1	**	
		$y = 42\sin 30^\circ \times 2.8 - 4.9 \times 2.8^2$	M1	**	
		$y = 20.4$	A1✓	**	✓ their t
		$x = 42\cos 30^\circ \times 2.80$	M1		
		$x = 102$	A1✓		✓ their t
		$\sqrt{(x^2 + y^2)}$	M1		
		$d = 104$	A1	11	
		or $6.41^2 = 21^2 + 2 \times -9.8s$	M1	**	vert dist first then time
		$s = 20.4$	A1	**	
		$20.4 = 21t + \frac{1}{2} \cdot -9.8t^2$	M1	**	
	$t = 2.80$	A1	**		
	or $22.5 - s$ and $6.41^2 = 2 \times 9.8s$	M1	**	dist from top (s = 2.096)	
	$y = 20.4$	A1	**		
	$22.5 \& 2.1 = \frac{1}{2} \cdot 9.8t^2$	M1	**	2 separate times (2.143, 0.654)	
	$t = 2.80$	A1	**	2.143 + 0.654	
	<b>alternatively</b>				
	(ii) $y = x/\sqrt{3} - x^2/270$ aef	B1		$y = x \tan 30^\circ - 9.8x^2/2 \cdot 42^2 \cdot \cos^2 30^\circ$	
	$dy/dx = 1/\sqrt{3} - x/135$	M1		for differentiating	
		A1		aef	
	$dy/dx = -\tan 10^\circ$	M1		must be $-\tan 10^\circ$	
	$1/\sqrt{3} - x/135 = -\tan 10^\circ$	A1			
	solve for x	M1			
	$x = 102$	A1✓		✓ on their dy/dx	
	$y = x/\sqrt{3} - x^2/270$	M1			
	$y = 20.4$	A1✓		✓ their x	
	$\sqrt{(x^2 + y^2)}$	M1			
	$d = 104$	A1	(11)		

(Q8, Jan 2007)

7	$0 = 12\sin 27^\circ t - 4.9t^2$ any correct.	M1	or $R = u^2 \sin 2\theta / g$ (B2)
	$t = 1.11$ .....method for total time	A1	correct formula only
	$R = 12\cos 27^\circ \times t$	M1	$12^2 \times \sin 54^\circ / 9.8$ sub in values
	11.9	A1 4	11.9 4

(Q2, June 2007)

8 (i)	$x = 7t$	B1	
	$y = 21t - 4.9t^2$	M1	or $-g/2$
		A1	
	$y = 21 \cdot x/7 - 4.9 x^2/49$	M1	
	$y = 3x - x^2/10$	A1 5	AG
(ii)	$-25 = 3x - x^2/10$ (must be -25)	M1	or method for total time (5.26)
	solving quadratic	M1	or 7 x total time
	36.8 m	A1 3	8

(Q4, June 2007)

<b>9 (i)</b>	$12 \times \cos 55^\circ$ $6.88 \text{ m s}^{-1}$	M1 A1 <b>2</b>	
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(Q1, Jan 2008)

<b>10(i)</b>	$0 = (175\sin\theta)^2 - 2 \times 9.8 \times 650$ $\theta = 40.2^\circ$	M1 A1 A1 <b>3</b>	
<b>(ii)</b>	Attempt at $t_1, t_2, t_{\text{top}}$ or $t_{\text{total}}$ 5.61, 23.65, 14.63, 29.26 $t_2 - t_1$ or $2(t_{\text{top}} - t_1)$ or $t_{\text{total}} - 2t_1$  time difference = 18.0	M1 A1 M1 A1  A1 <b>5</b>	$650 = 175\sin 55^\circ \cdot t - 4.9t^2$ etc
<b>(iii)</b>	$v_h = 175\cos 55^\circ$ (100.4) $v_v = 175\sin 55^\circ - 9.8 \times 5.61$ speed = $\sqrt{(88.4^2 + 100.4^2)}$ $134 \text{ m s}^{-1}$	B1 M1 M1 A1 <b>4</b>	or KE $\frac{1}{2}mv^2$ (B1) PE $mx9.8 \times 650$ $v = \sqrt{(175^2 - 2 \times 9.8 \times 650)}$ <b>12</b>

(Q7, Jan 2008)

<b>11(i)</b>	$0 = 35\sin\theta \times t - 4.9t^2$ $t = 35\sin\theta/4.9$ $50\sin\theta/7$ $R = 35\cos\theta \times t$ aef  $R = 35^2\sin\theta \cdot \cos\theta/4.9$  $R = 125\sin 2\theta$	M1 A1 B1  M1  A1 <b>5</b>	$R = u^2\sin 2\theta/g$ only ok if proved or $70\sin\theta/g$ aef  their t  eliminate t  <b>AG</b>
<b>(ii)</b>	$110 = 125\sin 2\theta$ $\theta = 30.8^\circ$ or $59.2^\circ$ $t = 3.66 \text{ s}$ or $6.13 \text{ s}$	M1 A1+1 A1+1 <b>5</b>	<b>10</b>

(Q4, June 2008)

<b>12 (ii)</b>	$v_h = 2$ $v_v^2 = 2 \times 9.8 \times 4$ $v_v = 8.85$ $(14\sqrt{10}/5)$  speed = $\sqrt{(8.85^2 + 2^2)}$ $9.08 \text{ m s}^{-1}$ $\tan^{-1}(8.85/2)$ $77.3^\circ$ to horizontal	B1 M1 A1  M1 A1 M1 A1 <b>7</b>	or (B1) $\frac{1}{2}mx2^2$ (B1) $\frac{1}{2}mxv^2$  (B1) $mx9.8 \times 4$ $v = \sqrt{(2^2 + 2 \times 9.8 \times 4)}$  or $\cos^{-1}(2/9.08)$ $12.7^\circ$ to vertical <b>13</b>
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(Q7, June 2008)

<b>13</b>	$(20 \sin \theta)^2 = 2 \times 9.8 \times 17$	M1	or B2 for $\max ht = v^2 \sin^2 \theta / 2g$
		A1	
	$\sin \theta = \sqrt{(2 \times 9.8 \times 17) \div 20}$	M1	subst. values in above
	$\theta = 65.9^\circ$	A1	<b>4</b>

(Q1, Jan 2009)

<b>14 (i)</b>	$x = v \cos \theta t$	B1	
	$y = v \sin \theta t - \frac{1}{2} \times 9.8 t^2$	B1	or g
	substitute $t = x/v \cos \theta$	M1	
	$y = x \tan \theta - 4.9x^2/v^2 \cos^2 \theta$	A1	<b>4</b> <b>AG</b>
<b>(ii)</b>	Sub $y = -h$ , $x = h$ , $v = 14$ , $\theta = 30$	M1	signs must be correct
	$-h = h/\sqrt{3} - h^2/30$	A1	aef
	solving above	M1	
	$h = 47.3$	A1	<b>4</b>
<b>(iii)</b>	$v_v^2 = (14 \sin 30^\circ)^2 - 2 \times 9.8 \times (-47.3)$	M1	$14 \cos 30^\circ t = 47.3 \text{ ft}$ & $v_v = 14 \sin 30^\circ - 9.8t$
	(double negative needed) ft their -47.3	A1	ft $t = 3.90$ (or $dy/dx = 1/\sqrt{3} - x/15$ etc ft)
	$v_v = \pm 31.2$	A1	$v_v = \pm 31.2$ ( $\tan \alpha = 1/\sqrt{3} - 47.3/15$ )
	$\tan^{-1}(31.2/14 \cos 30^\circ)$	M1	$\tan^{-1}(31.2/14 \cos 30^\circ)$
	$\alpha = 68.8^\circ$ below horiz/21.2° to d'vert.	A1	<b>5</b> 68.8°/.....
<b>(iv)</b>	$\frac{1}{2} m \times 14^2 + m \times 9.8 \times 47.3 = \frac{1}{2} m v^2$	M1	ft $(12.1^2 + 31.2^2)$
	$v = 33.5$	A1	<b>2</b> 33.5 <b>15</b>

(Q6, Jan 2009)

<b>15 (i)</b>	$9 = 17 \cos 25^\circ \times t$	M1	B1 $y = x \tan \theta - 4.9x^2/v^2 \cos^2 \theta$ M1/A1 $y = 9 \tan(-25^\circ) - 4.9 \times 9^2/17^2 \cos^2 25^\circ$  A1 $y = -5.87$ 2.13
	$t = 0.584$ (or $9/17 \cos 25^\circ$ )	A1	
	$d = 17 \sin 25^\circ \times 0.584 + \frac{1}{2} \times 9.8 \times 0.584^2$ (d = ht lost (5.87))	M1	
	$h = 2.13$	A1	
<b>(ii)</b>	$v_h = 17 \cos 25^\circ$ (15.4)	B1	M1/A1 $dy/dx = \tan \theta - 9.8x/v^2 \cos^2 \theta$  A1 $dy/dx = -0.838$ M1 $\tan^{-1}(-.838)$ or 50.0° to vertical
	$v_v = 17 \sin 25^\circ + 9.8 \times 0.584$	M1	
	$v_v^2 = (17 \sin 25^\circ)^2 + 2 \times 9.8 \times 5.87$		
	$v_v = 12.9$	A1	
	$\tan \theta = 12.9/15.4$	M1	
	$\theta = 40.0^\circ$ below horizontal	A1	<b>5</b>
<b>(iii)</b>	speed = $\sqrt{(12.9^2 + 15.4^2)}$	M1	(20.1)  NB 0.3 instead of 0.7 gives 11.0 (M0)
		A1	
	$\frac{1}{2} m v^2 = \frac{1}{2} m \times 20.1^2 \times 0.7$	M1	
	$v = 16.8 \text{ m s}^{-1}$	A1	

(Q7, June 2009)

<b>16 (i)</b>	$30^2 = V_1^2 \sin^2 \theta_1 - 2 \times 9.8 \times 250$ $V_1^2 \sin^2 \theta_1 = 5800$ AEF $V_1 \cos \theta_1 = 40$ $V_1 = 86.0$ $\theta_1 = 62.3^\circ$	M1 A1 B1 A1 A1 <b>[5]</b>	$\frac{1}{2}m V_1^2 = \frac{1}{2}m 50^2 + m \times 9.8 \times 250$  <b>AG</b> <b>AG</b>
<b>(ii)</b>	$0 = \sqrt{5800} t_p - 4.9 t_p^2$ $t_p = 15.5$  $-\sqrt{5800} = 30 - 9.8 t_q$  $t_q = 10.8$	M1 A1  M1  A1 <b>[4]</b>	$30 = V_1 \sin \theta_1 - 9.8 t$  $t = 4.71$
<b>(iii)</b>	$R = 40 \times 15.5$ $R = 621$ $V_2 \cos \theta_2 \times 10.8 = 621$ $0 = V_2 \sin \theta_2 \times 10.8 - 4.9 \times 10.8^2$ $V_2 \sin \theta_2 = 53.1$ or $53.0$ Method to find a value of $V_2$ or $\theta_2$ $\theta_2 = 42.8^\circ$ $V_2 = 78.2 \text{ m s}^{-1}$ or $78.1 \text{ m s}^{-1}$	M1 A1 B1 M1 A1 M1 A1 A1 <b>[8]</b>	$(620, 622)$ $V_2 \cos \theta_2 = 57.4$  $(52.9, 53.1)$  $42.6^\circ$ to $42.9^\circ$ or $78.1^\circ$

(Q6, Jan 2010)

<b>17</b>	$v^2 = 2 \times 9.8 \times 10$ $v = 14 \text{ m s}^{-1}$ speed = $\sqrt{7^2 + 14^2}$ $15.7$ or $7\sqrt{5} \text{ m s}^{-1}$ $\tan^{-1}(14/7)$ or $\tan^{-1}(7/14)$ $63.4^\circ$ to the horizontal	M1 A1 M1 A1 M1 A1 <b>6</b>	Using $v^2 = u^2 + 2as$ with $u = 0$  Method to find speed using their “v”  Method to find angle using their “v” $26.6^\circ$ to vertical <b>6</b>
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(Q1, June 2010)

<p><b>18 (i)</b></p> <p>Or last 4 marks of (i)</p>	<p><math>R = 0.2 \times 9.8 \times \cos 30^\circ (= 1.70)</math>  <math>F = 0.1 \times 9.8 \times \cos 30^\circ (= 0.849)</math> FT</p> <p><math>\frac{1}{2} \times 0.2 \times 11^2 - \frac{1}{2} \times 0.2 v^2 =</math>  <math>0.2 \times 9.8 \times 5 \sin 30 + 5 \times 0.849</math>  <math>v = 5.44 \text{ m s}^{-1}</math></p> <p><math>F + 0.2g \sin 30 = \pm 0.2a</math>  <math>a = \pm 9.1</math>  <math>v^2 = 11^2 + 2 \times a \times 5</math>  <math>v = 5.44 \text{ m s}^{-1}</math></p>	<p>B1            B1            M1            A1            A1            A1 <b>6</b>            M1            A1            M1            A1</p>	<p>FT on their R, but not <math>R = 0.2g</math>            Use of conservation of energy</p> <p><b>AG</b></p> <p>Use of N2L, 3 terms</p> <p>Complete method to find v</p>
<p><b>(ii)</b></p> <p>Or first 5 marks of (ii)</p>	<p><math>t = 5 \cos 30^\circ / 5.44 \cos 30^\circ</math>  <math>t = 0.919 \text{ s}</math>  <math>u = 5.44 \sin 30^\circ (= 2.72)</math>  <math>s = 2.72 \times 0.919 - 4.9 \times 0.919^2</math>  <math>s = -1.6</math> (or better)            Ht drop to C = <math>5 \sin 30^\circ = 2.5 \text{ m}</math>            Ball does not hit the roof</p> <p><math>y = x \tan \theta - gx^2 \sec^2 \theta / 2V^2</math>            substitute values  <math>V = 5.44 \quad \theta = 30^\circ \quad x = 5 \cos 30^\circ</math>  <math>y = 2.5 - 9.8 \times 25 \times 3 / 4 \times 4 / 3 / (2 \times 5.44^2)</math>  <math>y = -1.6</math> (or better)</p>	<p>M1            A1            B1            M1            A1            B1            A1 <b>7</b>            B1            M1            A1            A1            A1</p>	<p>time to lateral position over C</p> <p>Ht dropped</p> <p><b>13</b></p> <p>all 3 correct</p>
<p><b>OR (ii)</b></p>	<p><math>u = 5.44 \sin 30^\circ (= 2.72)</math>  <math>-2.5 = 5.44 \sin 30 t - 4.9 t^2</math></p> <p><math>t = 1.04</math>  <math>x = 5.44 \cos 30 \times 1.04 = 4.9</math> (or better)            Horizontal distance from B to C =  <math>5 \cos 30 = 4.3</math> (or better)            Ball does not hit the roof</p>	<p>B1            M1            A1            A1            A1            B1            A1 <b>7</b></p>	<p>aef            time to position level with AC</p>
<p><b>OR (ii)</b></p>	<p><math>y = x \tan \theta - gx^2 \sec^2 \theta / 2V^2</math>            substitute values  <math>-2.5 = 0.577x - 0.221x^2</math>            Attempt to solve quadratic for x  <math>x = 4.9</math> (or better)            Horizontal distance from B to C =  <math>5 \cos 30 = 4.3</math> (or better)            Ball does not hit the roof</p>	<p>B1            M1            A1            M1            A1            B1            A1 <b>7</b></p>	<p>aef</p>
<p><b>OR (ii)</b></p>	<p><math>u = 5.44 \sin 30^\circ = 2.72</math>  <math>-2.5 = 5.44 \sin 30 t - 4.9 t^2</math></p> <p><math>t = 1.0</math> (or better)  <math>T = 5 \cos 30^\circ / 5.44 \cos 30^\circ</math>  <math>T = 0.92</math> (or better)            Ball does not hit the roof</p>	<p>B1            M1            A1            A1            M1            A1            A1 <b>7</b></p>	<p>aef            time to position level with AC            time to lateral position over C</p>



<b>19</b>	<b>(i)</b>	$0 = (14\sin 30)^2 - 2gh$ $h = 2.5 \text{ m}$	M1 A1 [2]	$h = (14\sin 30)x1/1.4 - g(1/1.4)^2/2$ or use $(u^2\sin^2\theta)/2g$
	<b>(ii)</b>	$0.4x15 = 0.4(14\cos 30) + I$ $I = 1.15$	M1 A1 A1 [3]	Impulse = change in momentum Not 14 or 0 for horizontal speed before impulse aef
	<b>(iii)</b>	$v^2 = (14\sin 30)^2 + 15^2$ $v = 16.6 \text{ ms}^{-1}$ $\tan\theta = 14\sin 30/15$ OR $\tan\psi = 15/14\sin 30$  $\theta = 25(.0)^\circ$ OR $\psi = 65(.0)^\circ$	M1 A1 M1  A1 [4]	Not $(14\sin 30)^2 + (14\cos 30)^2$ Allow $\sqrt{274}$ Correct trig to find an appropriate angle; not $14\cos 30$ for 15
	<b>(iv)</b>	$t = 14\sin 30/g (= 1/1.4 = 0.7142..)$ $T = 1.43 \text{ s}$ $R = 14\cos 30/1.4 + 15/1.4$ $R = 19.4 \text{ m}$	M1 A1 M1A1 A1 [5]	Rise or fall time (not to be given in (i)) Accept 10/7 $(14^2\sin(2x30) + 16.6^2\sin(2x25))/2g$ . 14 resolved, 15 not

(Q6, Jan 2011)

<b>20</b>	<b>i</b>	$x = (7\cos 30)t$ $y = (7\sin 30)t - gt^2/2$  $y = x\tan 30 - gx^2/(2x7^2\cos^2 30)$	B1 B1 M1 A1 [4]	Attempt to eliminate t $y = x/\sqrt{3} - 2x^2/15$ or $y = 0.577x - 0.133x^2$ aef
	<b>ii</b>	$2x^2/15 - x/\sqrt{3} + 0.6 = 0$ or $9.8t^2 - 7t + 1.2 = 0$ $x = 1.73 \text{ m}$ or $\sqrt{3} \text{ m}$ $2.6(0) \text{ m}$ or $3\sqrt{3}/2 \text{ m}$	M1 M1 A1 A1 [4]	Create a 3 term Q.E. in x or t with $y = 0.6$ Solve 3 term Q.E. for x or t
	<b>iii</b>	$v^2 = (7\sin 30)^2 - 2x9.8x0.6$ $v = 0.7 \text{ ms}^{-1}$ $\tan\theta = 0.7/(7\cos 30)$ $\theta = 6.59^\circ$ to horizontal or $83.4^\circ$ to vertical	M1 A1 M1 A1 [4]	Using $v^2 = u^2 - 2gs$ with u a component of 7; can find t first from their x in (i), and then use $v = u + at$ . Use component of 7
	<b>OR</b>	Attempt to differentiate equation of trajectory $\tan 30 - gx/(7^2\cos^2 30)$ Substitute $x = \sqrt{3}$ and equate to $\tan\theta$ $\theta = 6.59^\circ$ to horizontal or $83.4^\circ$ to vertical	M1 A1 M1 A1 [4]	Allow $1/\sqrt{3} - 4x/15$ or $y' = 0.577 - 0.267x$

(Q5, June 2011)

<b>21</b>		$v_x = 40\cos 35$ $v_y = 40\sin 35 - 9.8 \times 3$ $v = \sqrt{32.8^2 + 6.46^2}$ or $\tan\theta = 6.46/32.8$ $v = 33.4 \text{ ms}^{-1}$ $\theta = 11.1^\circ$ below horizontal	B1 B1 M1 A1 A1 [5]	Expect 32.8, need not be evaluated. Expect -6.46, need not be evaluated. Use of Pythagoras or relevant trig on cv( $v_x$ ) and cv( $v_y$ )  AEF; allow 11.2
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(Q1, Jan 2012)

<b>22</b>	(i)	$For P \ 4.9t^2 = 60$ $t = 3.5(0)$ $For Q \ 0 = 25\sin\theta \times t - \frac{1}{2} \times 9.8 \times t^2$ $\theta = 43.3$ $PQ = (25\cos\theta - 15) \times t_c$ $= 11.2$	M1 A1 M1 A1 M1 A1 [6]	Signs must be consistent. aef
	(ii)	$25\cos\theta(t) = 15(t)$ and solving for $\theta$ $\theta = 53.1$ $For Q \ s_{y1} = 25\sin\theta \times t - \frac{1}{2} \times 9.8 \times t^2$ $For P \ s_{y2} = \pm \frac{1}{2} \times 9.8 \times t^2$ Using $s_{y1} + s_{y2} = 60$ Solving for $t$ $t = 3$ $v = 25\sin\theta - 9.8 \times 3$ $v = -9.4$ therefore falling.	M1 A1 B1 B1 *M1 M1dep* A1 M1 A1 [9]	Equating horizontal components of velocity (or displacement) and solving for $\theta$ .  Other methods include finding time to max height for Q.
<b>OR</b>	(ii)	$25\cos\theta(t) = 15(t)$ and solving for $\theta$ $\theta = 53.1$ $For Q \ y = x \tan\theta - \frac{gx^2}{2 \times (25)^2 \cos^2\theta}$ $For P \ y = (60 - ) - \frac{gx^2}{2 \times (15)^2}$ Equate $y$ and solve for $x$ Use $x = u\cos\theta$ to find $t$ $t = 3$ $v = 25\sin\theta - 9.8 \times 3$ $v = -9.4$ therefore falling.	M1 A1 B1 B1 *M1 M1dep* A1 M1 A1 [9]	Equating horizontal components of velocity (or displacement) and solving for $\theta$ .  Must include 60.  Other methods include finding time to max height for Q.

(Q7, Jan 2012)

<b>23</b>	(i)	$\frac{1}{2} \times 9.8 \times t^2 = 0.2$ $t = 0.2(02)$ $s = 14.4 \times t_c$ $s = 2.91 \text{ m}$	M1 A1 M1 A1 [4]	Using SUVAT to find $t$ , consistent signs for $g$ and $0.2$ aef Using their value of $t$
	OR	Use equation of trajectory $-0.2 = x \tan\theta - \frac{gx^2 \sec^2\theta}{2 \times 14.4^2}$ Solve quadratic for $x$ $x = 2.91$	M1 A1 M1 A1 [4]	B1 for correct equation of the trajectory seen anywhere but award in part (ii) unless different method seen; consistent signs for $g$ and $0.2$
	(ii)	$U\sin 15 \times t - \frac{1}{2} \times 9.8 \times t^2 = -0.2$ $U\cos 15 \times t = 6$ Eliminate $t$ Attempt to solve to find $U$ $U = 10.2 \text{ ms}^{-1}$	*M1 A1 B1 Dep*M1 Dep*M1 A1 [6]	Using $s = ut + \frac{1}{2} at^2$ with $s = \pm 0.2$ and $a = \pm g$  Eliminate $U$ Attempt to solve to find $t (= 0.607)$
	OR	$y = x \tan\theta - \frac{gx^2 \sec^2\theta}{2U^2}$ Substitute values for $y, x, \theta$ $-0.2 = 6 \tan 15 - \frac{g \cdot 6^2 \sec^2 15}{2U^2}$ Attempt to solve for $U$ $U = 10.2 \text{ ms}^{-1}$	*B1 Dep*M1 A1 Dep*M2 A1 [6]	

(Q4, June 2012)

<b>24</b>	(i)	$x = u\cos\theta$ $y = u\sin\theta t - \frac{1}{2}gt^2$ Eliminate $t$ Get $y = x \tan\theta - \frac{gx^2 \sec^2\theta}{2u^2}$ [AG]	B1 B1 M1 A1 [4]	www	
	(ii)	Substitute $x = 22, y = -2.1$ and $u = 14$ Use $\sec^2\theta = 1 + \tan^2\theta$ Tidy to $12.1 \tan^2\theta - 22 \tan\theta + 10 = 0$ [AG]  Solve QE for $\tan\theta$ $\theta = 42.3$	M1 B1 A1  M1 A1 [5]	May start again of course  www  allow in radians (0.738)	
	(iii)	$t = 22/14\cos\theta$ $t = 2.12s$	M1 A1 [2]	May work vertically, but must solve for $t$ to get M1	

(Q7, Jan 2013)

25		(i)	$u \cos \theta = 14 \cos 20$  $-14 \sin 20 = u \sin \theta - 1.4g$ $u^2 = (1.4g - 14 \sin 20)^2 + (14 \cos 20)^2$ $u = 15.9$ <b>AG</b> $\tan \theta = (1.4g - 14 \sin 20) / 14 \cos 20$ $\theta = 34.2$	B1 M1  A1 M1 A1 M1 A1 A1 [7]	$U_x = 13.15...$ Horizontal component of initial velocity, could use $U_x$ , could use $U_y$ Complete method to find vertical component of initial velocity, could use $U_y$ $U_y = 8.9317...$ Method to find $u$ cwo Method to find $\theta$ or a relevant angle SC M1A1 for $-\tan 20 = (u \sin \theta - 1.4g) / u \cos \theta$ <b>OR</b> $14^2 = (u \sin \theta - 1.4g)^2 + (u \cos \theta)^2$ B1M1A1 for both.
		(ii)	$\frac{1}{2} m(15.9^2 - 14^2) = mgy$ $y = 2.9 \text{ m}$	M1 A1 A1 [3]	Method to find Level of P above A
	<b>OR</b>	(ii)	$(14 \sin 20)^2 = (15.9 \sin \theta)^2 - 2gs$ or $s = 15.9 \sin \theta \times 1.4 - \frac{1}{2}g \times 1.4^2$ $s = 2.9 \text{ m}$	M1 A1ft A1 [3]	Use constant acc formulae, a complete method needed. ft their $\theta$ from (i). no $\theta$ value used then M1A0.
		(iii)	$-2.9 = v \sin 20.t - 9.8t^2/2$ $2.9 \tan 20 = v \cos 20.t$ Eliminate $t$ to obtain equation in $v$ only Solve for $v$ $v = 1.37$	B1ft B1ft M1 M1 A1 [5]	ft their 2.9 ft their 2.9 Eliminate $v$ to obtain equation in $t$ only and solve for $t$ Substitute $t$ to find $v$
	<b>OR</b>	(iii)	$-2.9 = (2.9 \tan 20) \times \tan 20 - g(2.9 \tan 20)^2 / 2v^2 \cos^2 20$ Solve for $v$ $v = 1.37$	M2 A1ft M1 A1 [5]	Using equation of trajectory method.
	<b>OR</b>	(iii)	$2.9 / \cos 20 = \frac{1}{2}g \cos 20 \times t^2$ $0 = vt - \frac{1}{2}g \sin 20 \times t^2$ Eliminate $t$ Solve for $v$ $v = 1.37$	B1ft B1 M1 M1 A1 [5]	$t = 0.817$
		(iv)	$e = 0.098$	B1ft [1]	ft their $v$ from (iii), must be $v/14$ .

(Q7, June 2013)