| Q 1 |  | mark |  | Sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | Acceleration is $8 \mathrm{~m} \mathrm{~s}^{-2}$ <br> speed is $0+0.5 \times 4 \times 8=16 \mathrm{~m} \mathrm{~s}^{-1}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ |  | 2 |
| (ii) | $a=2 t$ | B1 |  | 1 |
| (iii) | $t=7$ <br> $a>0$ for $t<7$ and $a<0$ for $t>7$ | $\begin{aligned} & \text { B1 } \\ & \text { E1 } \end{aligned}$ | Full reason required | 2 |
| (iv) | Area under graph $0.5 \times 2 \times 8-0.5 \times 1 \times 4=6 \text { so } 6 \mathrm{~m} \mathrm{~s}^{-1}$ <br> Increase | M1 <br> B1 <br> E1 | Both areas under graph attempted. Accept both positive areas. If $2 \times 3$ seen accept ONLY IF reference to average accn has been made. Award for $v=-2 t^{2}+28 t+c$ seen or 24 and 30 seen Award if 6 seen. Accept ' 24 to 30 '. <br> This must be clear. Mark dept. on award of M1 | 3 |
|  | total | 8 |  |  |


| Q 2 |  | mark |  | Sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $a=24-12 t$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | Differentiate cao | 2 |
| (ii) | Need $24 t-6 t^{2}=0$ $t=0,4$ | M1 <br> A1 | Equate $v=0$ and attempt to factorise (or solve). Award for one root found. Both. cao. | 2 |
| (iii) | $\begin{aligned} & s=\int_{0}^{4}\left(24 t-6 t^{2}\right) \mathrm{d} t \\ & =\left[12 t^{2}-2 t^{3}\right]_{0}^{4} \\ & (12 \times 16-2 \times 64)-0 \\ & =64 \mathrm{~m} \end{aligned}$ | M1 <br> A1 <br> M1 <br> A1 | Attempt to integrate. No limits required. <br> Either term correct. No limits required <br> Sub $t=4$ in integral. Accept no bottom limit substituted or arb const assumed 0 . Accept reversed limits. FT their limits. <br> cao. Award if seen. <br> [If trapezium rule used. <br> M1 At least 4 strips: M1 enough strips for 3 s. f. <br> A1 (dep on $2^{\text {nd }} \mathrm{M} 1$ ) One strip area correct: A1 cao] | 4 |
|  | total | 8 |  |  |


| Q 3 |  | mark |  | Sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $\begin{aligned} & \mathbf{R}+\binom{-3}{4}+\binom{21}{-7}=\binom{0}{0} \\ & \mathbf{R}=\binom{-18}{3} \end{aligned}$ | M1 <br> A1 | Sum to zero <br> Award if seen here or in (ii) or used in (ii). [SC1for $\binom{18}{-3}$ ] | 2 |
| (ii) | $\begin{aligned} & \|\mathbf{R}\|=\sqrt{18^{2}+3^{2}} \\ & =18.248 \ldots \text { so } 18.2 \mathrm{~N}(3 \mathrm{s.f.}) \\ & \text { angle is } 180-\arctan \left(\frac{3}{18}\right)=170.53 \ldots{ }^{\circ} \\ & \text { so } 171^{\circ}(3 \mathrm{~s} . \mathrm{f} .) \end{aligned}$ | M1 <br> A1 <br> M1 <br> A1 | Use of Pythagoras <br> Any reasonable accuracy. FT R (with 2 non-zero cpts) <br> Allow arctan $\left(\frac{ \pm 3}{ \pm 18}\right)$ or $\arctan \left(\frac{ \pm 18}{ \pm 3}\right)$ <br> Any reasonable accuracy. FT R provided their angle is obtuse but not $180^{\circ}$ | 4 |
|  | total | 6 |  |  |


| Q 4 |  | mark |  | Sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) |  | B1 | All forces present. No extras. Accept mg, wetc. All labelled with arrows. Accept resolved parts only if clearly additional. <br> Accept no angles | 1 |
| (ii) | Resolve parallel to the plane $10+T \cos 30=4 g \cos 30$ $T=27.65299 \ldots \text { so } 27.7 \mathrm{~N} \text { (3 s. f.) }$ | M1 <br> A1 <br> A1 | All terms present. Must be resolution in at least 1 term. Accept $\sin \leftrightarrow \cos$. If resolution in another direction there must be an equation only in $T$ with no forces omitted. No extra forces. <br> All correct <br> Any reasonable accuracy | 3 |
| (iii) | Resolve perpendicular to the plane $R+0.5 T=2 g$ $R=5.7735 \ldots \text { so } 5.77 \mathrm{~N} \text { (3 s. f.) }$ | M1 <br> A1 <br> A1 | At least one resolution correct. Accept resolution horiz or vert if at least 1 resolution correct. All forces present. No extra forces. Correct. FT $T$ if evaluated. Any reasonable accuracy. cao. | 3 |
|  | total | 7 |  |  |


| Q 5 |  | mark |  | Sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $\begin{aligned} & x=2 \Rightarrow t=4 \\ & t=4 \Rightarrow y=16-1=15 \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { F1 } \end{aligned}$ | cao <br> FT their $t$ and $y$. Accept $15 \mathbf{j}$ | 2 |
| (ii) | $x=\frac{1}{2} t \text { and } y=t^{2}-1$ <br> Eliminating $t$ gives $y=\left((2 x)^{2}-1\right)=4 x^{2}-1$ | M1 <br> E1 | Attempt at elimination of expressions for $x$ and $y$ in terms of $t$ <br> Accept seeing $(2 x)^{2}-1=4 x^{2}-1$ | 2 |
| (iii) | either <br> We require $\frac{\mathrm{d} y}{\mathrm{~d} x}=1$ <br> so $8 x=1$ <br> $x=\frac{1}{8}$ and the point is $\left(\frac{1}{8},-\frac{15}{16}\right)$ <br> or <br> Differentiate to find $\mathbf{v}$ equate $\mathbf{i}$ and $\mathbf{j}$ cpts <br> so $t=\frac{1}{4}$ and the point is $\left(\frac{1}{8},-\frac{15}{16}\right)$ | M1 <br> B1 <br> A1 <br> M1 <br> M1 <br> A1 | This may be implied <br> Differentiating correctly to obtain $8 x$ <br> Equating the $\mathbf{i}$ and $\mathbf{j}$ cpts of their $\mathbf{v}$ | 3 |
|  | total | 7 |  |  |


| Q 6 |  | mark |  | Sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $2000=1000 a \text { so } a=2 \text { so } 2 \mathrm{~m} \mathrm{~s}^{-2}$ $12.5=5+2 t \text { so } t=3.75 \text { so } 3.75 \mathrm{~s}$ | B1 <br> M1 <br> A1 | Use of appropriate uvast for $t$ cao | 3 |
| (ii) | $\begin{aligned} & 2000-R=1000 \times 1.4 \\ & R=600 \text { so } 600 \mathrm{~N} \text { (AG) } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { E1 } \end{aligned}$ | N2L. Accept $F=m g a$. Accept sign errors. Both forces present. Must use $a=1.4$ | 2 |
| (iii) | $2000-600-S=1800 \times 0.7$ $S=140 \text { so } 140 \mathrm{~N} \text { (AG) }$ | M1 <br> A1 <br> E1 | N2L overall or 2 paired equations. $F=m a$ and use 0.7. Mass must be correct. Allow sign errors and 600 omitted. <br> All correct <br> Clearly shown | 3 |
| (iv) | $T-140=800 \times 0.7$ $T=700 \text { so } 700 \mathrm{~N}$ | M1 <br> B1 <br> A1 | N2L on trailer (or car). $F=800 a$ ( or 1000a). Condone missing resistance otherwise all forces present. Condone sign errors. <br> Use of 140 (or $2000-600$ ) and 0.7 |  |
| (v) | N2L in direction of motion car and trailer $-600-140-610=1800 a$ $a=-0.75$ <br> For trailer $T-140=-0.75 \times 800$ <br> so $T=-460$ so 460 <br> thrust | M1 <br> A1 <br> A1 <br> M1 <br> A1 <br> F1 | Use of $F=1800 a$ to find new accn. Condone 2000 included but not $T$. Allow missing forces. All forces present; no extra ones Allow sign errors. Accept $\pm$. cao. <br> N2L with their $a(\neq 0.7)$ on trailer or car. Must have correct mass and forces. Accept sign errors cao. Accept $\pm 460$ <br> Dep on M1. Take tension as +ve unless clear other convention |  |
|  | total | 17 |  |  |


| Q 7 |  | mark |  | Sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $\begin{aligned} & u=\sqrt{10^{2}+12^{2}}=15.62 . . \\ & \theta=\arctan \left(\frac{12}{10}\right)=50.1944 \ldots \text { so } 50.2(3 \text { s.f. }) \end{aligned}$ | B1 <br> M1 <br> A1 | Accept any accuracy 2 s . f. or better Accept $\arctan \left(\frac{10}{12}\right)$ (Or their $15.62 \cos \theta=10$ or their $15.62 \sin \theta=12$ ) <br> [FT their 15.62 if used] <br> [If $\theta$ found first M1 A1 for $\theta$ F1 for $u$ ] <br> [If B 0 M 0 SC 1 for both $u \cos \theta=10$ and $u \sin \theta=12$ seen] | 3 |
| (ii) | $\text { vert } \quad 12 t-0.5 \times 10 t^{2}+9$ $=12 t-5 t^{2}+9 \quad(\mathrm{AG})$ <br> horiz $10 t$ | M1 <br> A1 <br> E1 <br> B1 | Use of $s=u t+0.5 a t^{2}, a= \pm 9.8$ or $\pm 10$ and $u=12$ or 15.62.. Condone $-9=12 t-0.5 \times 10 t^{2}$, condone $y=9+12 t-0.5 \times 10 t^{2}$. Condone $g$. <br> All correct with origin of $u=12$ clear; accept 9 omitted Reason for 9 given. Must be clear unless $y=s_{0}+\ldots$ used. | 4 |
| (iii) | $\begin{aligned} & 0=12^{2}-20 s \\ & s=7.2 \text { so } 7.2 \mathrm{~m} \end{aligned}$ | M1 <br> A1 | Use of $v^{2}=u^{2}+2 a s$ or equiv with $u=12, v=0$. Condone $u \leftrightarrow v$ <br> From CWO. Accept 16.2. | 2 |
| (iv) | We require $0=12 t-5 t^{2}+9$ Solve for $t$ the + ve root is 3 range is 30 m | M1 <br> M1 <br> A1 <br> F1 | Use of $y$ equated to 0 <br> Attempt to solve a 3 term quadratic <br> Accept no reference to other root. cao. <br> FT root and their $x$. <br> [If range split up M1 all parts considered; M1 valid method for each part; A1 final phase correct; A1] | 4 |
| (v) | Horiz displacement of B: $20 \cos 60 t=10 t$ <br> Comparison with Horiz displacement of A | B1 <br> E1 | Condone unsimplified expression. Award for $20 \cos 60=10$ <br> Comparison clear, must show $10 t$ for each or explain. | 2 |
| (vi) | vertical height is $20 \sin 60 t-0.5 \times 10 t^{2}=10 \sqrt{3} t-5 t^{2}(\mathrm{AG})$ | A1 | Clearly shown. Accept decimal equivalence for $10 \sqrt{3}$ (at least 3 s. f.). Accept $-5 t^{2}$ and $20 \sin 60=10 \sqrt{3}$ not explained. | 1 |
| (vii) | $\begin{aligned} & \text { Need } 10 \sqrt{3} t-5 t^{2}=12 t-5 t^{2}+9 \\ & \Rightarrow t=\frac{9}{10 \sqrt{3}-12} \\ & t=1.6915 \ldots \text { so } 1.7 \mathrm{~s}(2 \mathrm{s.f.}) \text { (AG) } \end{aligned}$ | M1 <br> A1 <br> E1 | Equating the given expressions <br> Expression for $t$ obtained in any form <br> Clearly shown. Accept 3 s. f. or better as evidence. Award M1 A1 E0 for 1.7 sub in each ht | 3 |
|  | total | 19 |  |  |

