| Question |  | Answer | Marks |  |  |  |
| :--- | :--- | :--- | :--- | :---: | :--- | :--- |
| $\mathbf{1}$ | (i) |  | $k x^{\frac{1}{3}-1}$ oe | M1 | $k$ is any non-zero constant |  |
| $\mathbf{1}$ | (ii) |  | $k x^{\frac{-2}{3}}$ isw cao | A1 | ignore $+c$ | allow any equivalent exact simplified |



| 3 |  | $\frac{2.4-3.6}{2.2-2}$ oe <br> -6 cao | M1 |
| :--- | :--- | :--- | :---: | :---: | :--- | :--- |
| A1 |  | M1 may be embedded eg in <br> equation of straight line <br> B2 if unsupported |  |
| ignore subsequent work irrelevant |  |  |  |
| to finding the gradient |  |  |  |


| 4 | (i) | $-10 x^{-6}$ isw | B1 <br> B1 <br> [2] | $\begin{aligned} & \text { for }-10 \\ & \text { for } x^{-6} \\ & \text { ignore }+c \text { and } y= \end{aligned}$ | if B0B0 then SC1 for $-5 \times 2 x^{-5-1}$ or better soi |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | (ii) | $\begin{aligned} & y=x^{1 / 3} \text { soi } \\ & k x^{n-1} \\ & \frac{1}{3} x^{-\frac{2}{3}} \text { isw } \end{aligned}$ | B1 <br> M1 <br> A1 <br> [3] | condone $y^{\prime}=x^{1 / 3}$ if differentiation follows ft their fractional $n$ <br> ignore $+c$ and $y=$ | allow 0.333 or better |


| 5 | (i) | ruled line touching curve at $x=2$ their $\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$ from their tangent answer in range 2.5 to 3.0 inclusive | M1 <br> M1 <br> A1 <br> [3] | may be on graph or in working; must use correct points from their line <br> their tangent may be at another point <br> both M1s must be awarded | intent to touch, but must not clearly cut curve <br> M0 for reciprocal, <br> ( value is approx 2.773) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | (ii) | 3.482202253... and 4.59479342... rot to 3 or more sf <br> 2.78 to 2.7815 or 2.8 | B1 <br> B1 <br> [2] | mark the final answer | 2.781477917.. |

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| $\mathbf{6}$ |  | $\frac{1}{2} x^{-\frac{1}{2}}-3 x^{-2}$ oe; isw <br> [3] | Beed not be simplified <br> B2 for one term correct <br> ignore $+c$ | if B0 allow M1 for either $x^{1 / 2}$ or $x^{-1}$ seen <br> before differentiation <br> deduct one mark for extra term in $x$ |
| :--- | :--- | :--- | :--- | :---: | :--- | :--- |


| 7 | $\begin{aligned} & \text { (i) } m= \\ & \quad \frac{\sqrt{1+2 \times 4.1}-\sqrt{1+2 \times 4}}{4.1-4} \text { s.o.i } \\ & \text { grad }=\frac{\sqrt{9.2}-\sqrt{9}}{4.1-4} \text { s.o.i } \\ & 0.3315 \text { cao } \end{aligned}$ | M1 <br> M1 <br> A1 |  | no marks for use of Chain Rule or any other attempt to differentiate <br> SC2 for $0.33 \ldots$. appearing only embedded in equation of chord |
| :---: | :---: | :---: | :---: | :---: |
| 7 | (ii) selection of value in $(4,4.1)$ and 4 or of two values in [3.9, 4.1] centred on 4 <br> answer closer to $1 / 3$ than $0.3315(.$. ) | M1 A1 |  | allow selection of 4 and value in (3.9, 4) |


| $\mathbf{8}$ | attempt to integrate $6 x^{2}+12 x^{\frac{1}{2}}$ <br> $[y=] 2 x^{3}+8 x^{1.5}+\mathrm{c}$ | M1 <br> A2 | accept un-simplified; A1 for 2 terms <br> correct |
| :--- | :--- | :--- | :--- |
| Substitution of $(4,10)$ |  |  |  |
| $[y=] 2 x^{3}+8 a^{1.5}-182$ or $\mathbf{c}=-182$ | A1 | M1 <br> dependent on attempted integral with <br> $+c$ term |  |


| 9 | $\left[f^{\prime}(x)=\right] 12-3 x^{2}$ | B1 |
| :--- | :--- | :--- | :--- | :--- |
| their $\mathrm{f}^{\prime}(x)>0$ or $=0$ soi |  |  |
| $-2<x<2$ |  |  |$\quad$| M1 |
| :--- |
| A1 |$\quad$| condone $-2 \leq x \leq 2$ or "between |
| :--- |
| -2 and 2" |$\quad 3$


| 10 | $y^{\prime}=6 \times \frac{3}{2} x^{\frac{1}{2}}$ or $9 x^{\frac{1}{2}}$ o.e. | 2 | 1 if one error in coeff or power, or extra <br> term |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $y^{\prime \prime}=\frac{9}{2} x^{-\frac{1}{2}}$ o.e. <br> $\sqrt{3} 36=6$ used <br> interim step to obtain $\frac{3}{4}$ | M1 <br> A1 | f.t. their $y^{\prime}$ only if fractional power <br> www answer given | 5 |


| 11 | $[y=] 3 x-x^{3} / 3$ <br> $+c$ <br> subst of $(6,1)$ in their eqn with $c$ <br> $y=3 x-x^{3} / 3+55$ c.a.o | B1 <br> B1 <br> M1 <br> A1 | Dep't on integration attempt <br> Dep't on B0B1 <br> Allow $c=55$ isw | 4 |
| :--- | :--- | :--- | :--- | :--- |


| 12 | $\sqrt{ }=x^{1 / 2}$ soi | B1 |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $18 x^{2}, 1 / 2 x^{-1 / 2}$ | B1B1 | -1 if $\mathrm{d} / \mathrm{d} x(3)$ not $=0$ | 5 |
|  | $36 x^{3 / 2}$ | B1 |  |  |
|  | Ax $x^{-3 / 2}\left(\right.$ from $\left.B x^{-1 / 2}\right)$ | B1 | any A,B |  |

