Q	uestio	n	Answer	Marks	Guidar	nce
1	(i)		$kx^{\frac{1}{3}-1}$ oe	M1	<i>k</i> is any non-zero constant	
			$4x^{\frac{-2}{3}}$ isw cao	A1	ignore $+ c$	allow any equivalent exact simplified form
				[2]		
1	(ii)		kx^{-3+1} oe	M1	<i>k</i> is any non-zero constant	
			$-3x^{-2}$ isw	A1		allow any equivalent exact simplified form
			+ <i>c</i>	A1 [3]		
				[3]		

2		$3x^2 - 6$ seen	B1		
		<i>their</i> $y' = 0$ or $y' > 0$ or $y' \ge 0$	M1	must be quadratic with at least one of only two terms correct	
		$\sqrt{2}$ and $-\sqrt{2}$ identified	A1	may be implied by use with inequalities or by $\pm 1.41[4213562]$ to 3 sf or more	$ x = \sqrt{2}$ implies A1
		$x < -\sqrt{2}$ or $x \le -\sqrt{2}$ isw	A1	if A1A0A0 , allow SC1 for fully correct answer in decimal form to 3 sf or more	NB just $-\sqrt{2} > x > \sqrt{2}$ or $\sqrt{2} < x < -\sqrt{2}$ or
		$x > \sqrt{2}$ or $x \ge \sqrt{2}$	A1 [5]	or A2 for $ x > \sqrt{2}$ or $ x \ge \sqrt{2}$	$x > \pm \sqrt{2}$ implies the first A1 then A0A0

3	$\frac{2.4-3.6}{2.2-2}$ oe	M1	M1 may be embedded eg in equation of straight line
	- 6 cao	A1	B2 if unsupported ignore subsequent work irrelevant to finding the gradient
		[2]	

4	(i)	$-10x^{-6}$ isw	B1		if B0B0 then SC1 for $-5 \times 2x^{-5-1}$ or
			B1	for x^{-6}	better soi
				ignore $+ c$ and $y =$	
			[2]		
4	(ii)	$y = x^{\frac{1}{3}}$ soi	B1	condone $y' = x^{\frac{1}{3}}$ if differentiation follows ft their fractional <i>n</i>	
		kx^{n-1}	M1	It their fractional n	
		$\frac{1}{3}x^{-\frac{2}{3}}$ isw	A1	ignore $+ c$ and $y =$	allow 0.333 or better
			[3]		

5	(i)	ruled line touching curve at $x = 2$	M1		intent to touch, but must not clearly cut
		their $\frac{y_2 - y_1}{x_2 - x_1}$ from their <i>tangent</i>	M1	may be on graph or in working; must use correct points from their line their tangent may be at another point	curve M0 for reciprocal,
		answer in range 2.5 to 3.0 inclusive	A1 [3]	both M1s must be awarded	(value is approx 2.773)
5	(ii)	3.482202253 and 4.59479342 rot to 3 or more sf	B1		
		2.78 to 2.7815 or 2.8	B1 [2]	mark the final answer	2.781477917

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6	$\frac{1}{2}x^{-\frac{1}{2}} - 3x^{-2}$ oe; isw	B3	need not be simplified B2 for one term correct ignore $+ c$	if B0 allow M1 for either $x^{1/2}$ or x^{-1} seen before differentiation deduct one mark for extra term in x
		[3]		deduct one mark for extra term m x

7	(i) $m = \sqrt{1+2\times4.1} - \sqrt{1+2\times4}$	M1	no marks for use of Chain Rule or any other attempt to differentiate
	$grad = \frac{\frac{4.1 - 4}{\sqrt{9.2} - \sqrt{9}}}{4.1 - 4} \text{ s.o.i}$	M1	SC2 for 0.33 appearing only embedded in equation of chord
	4.1-4 0.3315 cao	A1	
7	(ii) selection of value in (4, 4.1) and 4 or of two values in [3.9, 4.1] centred on 4	M1	allow selection of 4 and value in (3.9, 4)
	answer closer to 1/3 than 0.3315()	A1	

8	attempt to integrate $6x^2 + 12x^{\frac{1}{2}}$ [y =] $2x^3 + 8x^{1.5} + c$	M1 A2	accept un-simplified; A1 for 2 terms correct
	Substitution of (4, 10)	M1	dependent on attempted integral with
	$[y =] 2x^3 + 8a^{1.5} - 182 \text{ or } c = -182$	A1	+ c term

9	$[f'(x) =] 12 - 3x^{2}$ their f'(x) > 0 or = 0 soi -2 < x < 2	B1 M1 A1	condone $-2 \le x \le 2$ or "between -2 and 2"	3
			-2 and 2"	

10	$y' = 6 \times \frac{3}{2} x^{\frac{1}{2}}$ or $9x^{\frac{1}{2}}$ o.e.	2	1 if one error in coeff or power, or extra term	
	$y'' = \frac{9}{2}x^{-\frac{1}{2}}$ o.e. $\sqrt{36} = 6$ used interim step to obtain $\frac{3}{4}$	1 M1 A1	f.t. their y' only if fractional power f.t. their y" www answer given	5

11	$[y =] 3x - x^{3}/3$ + c subst of (6, 1) in their eqn with c $y = 3x - x^{3}/3 + 55$ c.a.o	B1 B1 M1 A1	Dep't on integration attempt Dep't on B0B1 Allow $c = 55$ isw	4

12	$\sqrt{x} = x^{\frac{1}{2}}$ soi	B1		
	$18x^2$, $\frac{1}{2}x^{-\frac{1}{2}}$	B1B1	-1 if d/dx(3) not = 0	
	36 <i>x</i>	B1		5
	$Ax^{-3/2}$ (from $Bx^{-\frac{1}{2}}$)	B1	any A,B	