

# C1 Differentiation

## 1. June 2010 qu. 6

Find the gradient of the curve  $y = 2x + \frac{6}{\sqrt{x}}$  at the point where  $x = 4$ . [5]

## 2. June 2010 qu. 10

(i) Find the coordinates of the stationary points of the curve  $y = 2x^3 + 5x^2 - 4x$ . [6]

(ii) State the set of values for  $x$  for which  $2x^3 + 5x^2 - 4x$  is a decreasing function. [2]

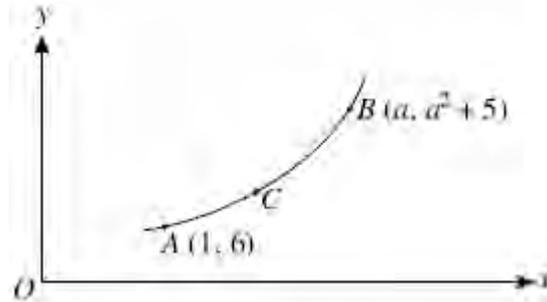
(iii) Show that the equation of the tangent to the curve at the point where  $x = \frac{1}{2}$  is  $10x - 4y - 7 = 0$ . [4]

(iv) Hence, with the aid of a sketch, show that the equation  $2x^3 + 5x^2 - 4x = \frac{5}{2}x - \frac{7}{4}$  has two distinct real roots. [2]

## 3. Jan 2010 qu. 3

Find the equation of the normal to the curve  $y = x^3 - 4x^2 + 7$  at the point  $(2, -1)$ , giving your answer in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers. [7]

## 4. Jan 2010 qu. 6



Not to scale

The diagram shows part of the curve  $y = x^2 + 5$ . The point  $A$  has coordinates  $(1, 6)$ . The point  $B$  has coordinates  $(a, a^2 + 5)$ , where  $a$  is a constant greater than 1. The point  $C$  is on the curve between  $A$  and  $B$ .

(i) Find by differentiation the value of the gradient of the curve at the point  $A$ . [2]

(ii) The line segment joining the points  $A$  and  $B$  has gradient 2.3. Find the value of  $a$ . [4]

(iii) State a possible value for the gradient of the line segment joining the points  $A$  and  $C$ . [1]

## 5. Jan 2010 qu. 9

Given that  $f(x) = \frac{1}{x} - \sqrt{x} + 3$ ,

(i) find  $f'(x)$ , [3]

(ii) find  $f''(4)$ . [5]

## 6. June 2009 qu. 1

Given that  $y = x^5 + \frac{1}{x^2}$ , find

(i)  $\frac{dy}{dx}$ , [3]

(ii)  $\frac{d^2y}{dx^2}$ . [2]

## 7. June 2009 qu. 10

(i) Solve the equation  $9x^2 + 18x - 7 = 0$ . [3]

(ii) Find the coordinates of the stationary point on the curve  $y = 9x^2 + 18x - 7$ . [4]

- (iii) Sketch the curve  $y = 9x^2 + 18x - 7$ , giving the coordinates of all intercepts with the axes. [3]  
 (iv) For what values of  $x$  does  $9x^2 + 18x - 7$  increase as  $x$  increases? [1]

**8. June 2009 qu. 11**

The point  $P$  on the curve  $y = k\sqrt{x}$  has  $x$ -coordinate 4. The normal to the curve at  $P$  is parallel to the line  $2x + 3y = 0$ .

- (i) Find the value of  $k$ . [6]  
 (ii) This normal meets the  $x$ -axis at the point  $Q$ . Calculate the area of the triangle  $OPQ$ , where  $O$  is the point  $(0, 0)$ . [5]

**9. Jan 2009 qu. 5**

Find  $\frac{dx}{dy}$  in each of the following cases:

- (i)  $y = 10x^{-5}$ , [2]  
 (ii)  $y = \sqrt[4]{x}$ , [3]  
 (iii)  $y = x(x + 3)(1 - 5x)$ . [4]

**10. Jan 2009 qu. 9**

The curve  $y = x^3 + px^2 + 2$  has a stationary point when  $x = 4$ . Find the value of the constant  $p$  and determine whether the stationary point is a maximum or minimum point. [7]

**11. Jan 2009 qu. 10**

A curve has equation  $y = x^2 + x$ .

- (i) Find the gradient of the curve at the point for which  $x = 2$ . [2]  
 (ii) Find the equation of the normal to the curve at the point for which  $x = 2$ , giving your answer in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers. [4]  
 (iii) Find the values of  $k$  for which the line  $y = kx - 4$  is a tangent to the curve. [6]

**12. June 2008 qu. 5**

Find the gradient of the curve  $y = 8\sqrt{x} + x$  at the point whose  $x$ -coordinate is 9. [5]

**13. Jan 2008 qu. 8**

- (i) Find the coordinates of the stationary points on the curve  $y = x^3 + x^2 - x + 3$ . [6]  
 (ii) Determine whether each stationary point is a maximum point or a minimum point. [3]  
 (iii) For what values of  $x$  does  $x^3 + x^2 - x + 3$  decrease as  $x$  increases? [2]

**14. June 2007 qu. 5**



The diagram shows a rectangular enclosure, with a wall forming one side. A rope, of length 20 metres, is used to form the remaining three sides. The width of the enclosure is  $x$  metres.

- (i) Show that the enclosed area,  $A \text{ m}^2$ , is given by  $A = 20x - 2x^2$ . [2]  
 (ii) Use differentiation to find the maximum value of  $A$ . [4]

**15. Jan 2007 qu. 7**

Find  $\frac{dy}{dx}$  in each of the following cases.

- (i)  $y = 5x + 3$  [1]  
(ii)  $y = \frac{2}{x^2}$  [3]  
(iii)  $y = (2x + 1)(5x - 7)$  [4]

**16. June 2006 qu. 1**

The points  $A(1, 3)$  and  $B(4, 21)$  lie on the curve  $y = x^2 + x + 1$ .

- (i) Find the gradient of the line  $AB$ . [2]  
(ii) Find the gradient of the curve  $y = x^2 + x + 1$  at the point where  $x = 3$ . [2]

**17. June 2006 qu. 8**

A cuboid has a volume of  $8 \text{ m}^3$ . The base of the cuboid is square with sides of length  $x$  metres. The surface area of the cuboid is  $A \text{ m}^2$ .

- (i) Show that  $A = 2x^2 + \frac{32}{x}$ . [3]  
(ii) Find  $\frac{dA}{dx}$ . [3]  
(iii) Find the value of  $x$  which gives the smallest surface area of the cuboid, justifying your answer. [4]

**18. Jan 2006 qu. 6**

- (i) Find the coordinates of the stationary points on the curve  $y = x^3 - 3x^2 + 4$ . [6]  
(ii) Determine whether each stationary point is a maximum point or a minimum point. [3]  
(iii) For what values of  $x$  does  $x^3 - 3x^2 + 4$  increase as  $x$  increases? [2]

**19. June 2005 qu. 10**

- (i) Given that  $y = \frac{1}{3}x^3 - 9x$ , find  $\frac{dy}{dx}$ . [2]  
(ii) Find the coordinates of the stationary points on the curve  $y = \frac{1}{3}x^3 - 9x$ . [3]  
(iii) Determine whether each stationary point is a maximum point or a minimum point. [3]  
(iv) Given that  $24x + 3y + 2 = 0$  is the equation of the tangent to the curve at the point  $(p, q)$ , find  $p$  and  $q$ . [5]