

Edexcel Maths C1

Topic Questions from Papers

Series

9. An arithmetic series has first term a and common difference d .

(a) Prove that the sum of the first n terms of the series is

$$\frac{1}{2}n[2a + (n-1)d]. \tag{4}$$

Sean repays a loan over a period of n months. His monthly repayments form an arithmetic sequence.

He repays £149 in the first month, £147 in the second month, £145 in the third month, and so on. He makes his final repayment in the n th month, where $n > 21$.

(b) Find the amount Sean repays in the 21st month. (2)

Over the n months, he repays a total of £5000.

(c) Form an equation in n , and show that your equation may be written as

$$n^2 - 150n + 5000 = 0. \tag{3}$$

(d) Solve the equation in part (c). (3)

(e) State, with a reason, which of the solutions to the equation in part (c) is **not** a sensible solution to the repayment problem. (1)



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2. The sequence of positive numbers u_1, u_2, u_3, \dots is given by:

$$u_{n+1} = (u_n - 3)^2, \quad u_1 = 1.$$

(a) Find u_2, u_3 and u_4 . **(3)**

(b) Write down the value of u_{20} . **(1)**

Q2

(Total 4 marks)



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7. On Alice’s 11th birthday she started to receive an annual allowance. The first annual allowance was £500 and on each following birthday the allowance was increased by £200.

(a) Show that, immediately after her 12th birthday, the total of the allowances that Alice had received was £1200. (1)

(b) Find the amount of Alice’s annual allowance on her 18th birthday. (2)

(c) Find the total of the allowances that Alice had received up to and including her 18th birthday. (3)

When the total of the allowances that Alice had received reached £32 000 the allowance stopped.

(d) Find how old Alice was when she received her last allowance. (7)



7. An athlete prepares for a race by completing a practice run on each of 11 consecutive days. On each day after the first day, he runs further than he ran on the previous day. The lengths of his 11 practice runs form an arithmetic sequence with first term a km and common difference d km.

He runs 9 km on the 11th day, and he runs a total of 77 km over the 11 day period.

Find the value of a and the value of d .

(7)



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9. Ann has some sticks that are all of the same length. She arranges them in squares and has made the following 3 rows of patterns:

Row 1 □

Row 2 □□

Row 3 □□□

She notices that 4 sticks are required to make the single square in the first row, 7 sticks to make 2 squares in the second row and in the third row she needs 10 sticks to make 3 squares.

(a) Find an expression, in terms of n , for the number of sticks required to make a similar arrangement of n squares in the n th row. (3)

Ann continues to make squares following the same pattern. She makes 4 squares in the 4th row and so on until she has completed 10 rows.

(b) Find the total number of sticks Ann uses in making these 10 rows. (3)

Ann started with 1750 sticks. Given that Ann continues the pattern to complete k rows but does not have sufficient sticks to complete the $(k + 1)$ th row,

(c) show that k satisfies $(3k - 100)(k + 35) < 0$. (4)

(d) Find the value of k . (2)



8. A sequence a_1, a_2, a_3, \dots is defined by

$$a_1 = k,$$

$$a_{n+1} = 3a_n + 5, \quad n \geq 1,$$

where k is a positive integer.

(a) Write down an expression for a_2 in terms of k .

(1)

(b) Show that $a_3 = 9k + 20$.

(2)

(c) (i) Find $\sum_{r=1}^4 a_r$ in terms of k .

(ii) Show that $\sum_{r=1}^4 a_r$ is divisible by 10.

(4)



7. A sequence is given by:

$$x_1 = 1,$$

$$x_{n+1} = x_n(p + x_n),$$

where p is a constant ($p \neq 0$).

(a) Find x_2 in terms of p . (1)

(b) Show that $x_3 = 1 + 3p + 2p^2$. (2)

Given that $x_3 = 1$,

(c) find the value of p , (3)

(d) write down the value of x_{2008} . (2)

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11. The first term of an arithmetic sequence is 30 and the common difference is -1.5

(a) Find the value of the 25th term. (2)

The r th term of the sequence is 0.

(b) Find the value of r . (2)

The sum of the first n terms of the sequence is S_n .

(c) Find the largest positive value of S_n . (3)

Lined area for student answers.



5. A sequence x_1, x_2, x_3, \dots is defined by

$$x_1 = 1,$$

$$x_{n+1} = ax_n - 3, \quad n > 1,$$

where a is a constant.

(a) Find an expression for x_2 in terms of a . (1)

(b) Show that $x_3 = a^2 - 3a - 3$. (2)

Given that $x_3 = 7$,

(c) find the possible values of a . (3)



7. Sue is training for a marathon. Her training includes a run every Saturday starting with a run of 5 km on the first Saturday. Each Saturday she increases the length of her run from the previous Saturday by 2 km.

(a) Show that on the 4th Saturday of training she runs 11 km. (1)

(b) Find an expression, in terms of n , for the length of her training run on the n th Saturday. (2)

(c) Show that the total distance she runs on Saturdays in n weeks of training is $n(n + 4)$ km. (3)

On the n th Saturday Sue runs 43 km.

(d) Find the value of n . (2)

(e) Find the total distance, in km, Sue runs on Saturdays in n weeks of training. (2)



5. A 40-year building programme for new houses began in Oldtown in the year 1951 (Year 1) and finished in 1990 (Year 40).

The numbers of houses built each year form an arithmetic sequence with first term a and common difference d .

Given that 2400 new houses were built in 1960 and 600 new houses were built in 1990, find

- (a) the value of d , (3)

- (b) the value of a , (2)

- (c) the total number of houses built in Oldtown over the 40-year period. (3)



7. Jill gave money to a charity over a 20-year period, from Year 1 to Year 20 inclusive. She gave £150 in Year 1, £160 in Year 2, £170 in Year 3, and so on, so that the amounts of money she gave each year formed an arithmetic sequence.

(a) Find the amount of money she gave in Year 10. (2)

(b) Calculate the total amount of money she gave over the 20-year period. (3)

Kevin also gave money to the charity over the same 20-year period.

He gave £A in Year 1 and the amounts of money he gave each year increased, forming an arithmetic sequence with common difference £30.

The total amount of money that Kevin gave over the 20-year period was **twice** the total amount of money that Jill gave.

(c) Calculate the value of A. (4)



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9. A farmer has a pay scheme to keep fruit pickers working throughout the 30 day season. He pays £ a for their first day, £ $(a + d)$ for their second day, £ $(a + 2d)$ for their third day, and so on, thus increasing the daily payment by £ d for each extra day they work.

A picker who works for all 30 days will earn £40.75 on the final day.

(a) Use this information to form an equation in a and d . (2)

A picker who works for all 30 days will earn a total of £1005

(b) Show that $15(a + 40.75) = 1005$ (2)

(c) Hence find the value of a and the value of d . (4)

Horizontal lines for writing answers.



5. A sequence a_1, a_2, a_3, \dots is defined by

$$\begin{aligned} a_1 &= k, \\ a_{n+1} &= 5a_n + 3, \quad n \geq 1, \end{aligned}$$

where k is a positive integer.

(a) Write down an expression for a_2 in terms of k . (1)

(b) Show that $a_3 = 25k + 18$. (2)

(c) (i) Find $\sum_{r=1}^4 a_r$ in terms of k , in its simplest form.

(ii) Show that $\sum_{r=1}^4 a_r$ is divisible by 6. (4)



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9. (a) Calculate the sum of all the even numbers from 2 to 100 inclusive,

2 + 4 + 6 + + 100 (3)

(b) In the arithmetic series

k + 2k + 3k + + 100

k is a positive integer and k is a factor of 100.

(i) Find, in terms of k, an expression for the number of terms in this series.

(ii) Show that the sum of this series is

50 + 5000/k (4)

(c) Find, in terms of k, the 50th term of the arithmetic sequence

(2k + 1), (4k + 4), (6k + 7), ,

giving your answer in its simplest form. (2)

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Question 9 continued

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4. A sequence x_1, x_2, x_3, \dots is defined by

$$x_1 = 1$$

$$x_{n+1} = ax_n + 5, \quad n \geq 1$$

where a is a constant.

(a) Write down an expression for x_2 in terms of a . (1)

(b) Show that $x_3 = a^2 + 5a + 5$ (2)

Given that $x_3 = 41$

(c) find the possible values of a . (3)



9. A company offers two salary schemes for a 10-year period, Year 1 to Year 10 inclusive.

Scheme 1: Salary in Year 1 is £ P .
Salary increases by £ $(2T)$ each year, forming an arithmetic sequence.

Scheme 2: Salary in Year 1 is £ $(P + 1800)$.
Salary increases by £ T each year, forming an arithmetic sequence.

(a) Show that the **total** earned under Salary Scheme 1 for the 10-year period is

$$\text{£}(10P + 90T) \quad (2)$$

For the 10-year period, the **total** earned is the same for both salary schemes.

(b) Find the value of T . (4)

For this value of T , the salary in Year 10 under Salary Scheme 2 is £29 850

(c) Find the value of P . (3)



5. A sequence of numbers $a_1, a_2, a_3 \dots$ is defined by

$$a_1 = 3$$

$$a_{n+1} = 2a_n - c \quad (n \geq 1)$$

where c is a constant.

(a) Write down an expression, in terms of c , for a_2 (1)

(b) Show that $a_3 = 12 - 3c$ (2)

Given that $\sum_{i=1}^4 a_i \geq 23$

(c) find the range of values of c . (4)



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6. A boy saves some money over a period of 60 weeks. He saves 10p in week 1, 15p in week 2, 20p in week 3 and so on until week 60. His weekly savings form an arithmetic sequence.

(a) Find how much he saves in week 15 (2)

(b) Calculate the total amount he saves over the 60 week period. (3)

The boy's sister also saves some money each week over a period of m weeks. She saves 10p in week 1, 20p in week 2, 30p in week 3 and so on so that her weekly savings form an arithmetic sequence. She saves a total of £63 in the m weeks.

(c) Show that

$$m(m + 1) = 35 \times 36$$
(4)

(d) Hence write down the value of m . (1)



Question 6 continued

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Question 7 continued

Lined area for writing the answer to Question 7.



7. Each year, Abbie pays into a savings scheme. In the first year she pays in £500. Her payments then increase by £200 each year so that she pays £700 in the second year, £900 in the third year and so on.

(a) Find out how much Abbie pays into the savings scheme in the tenth year. (2)

Abbie pays into the scheme for n years until she has paid in a total of £67200.

(b) Show that $n^2 + 4n - 24 \times 28 = 0$ (5)

(c) Hence find the number of years that Abbie pays into the savings scheme. (2)



4. A sequence a_1, a_2, a_3, \dots is defined by

$$a_1 = 4$$

$$a_{n+1} = k(a_n + 2), \quad \text{for } n \geq 1$$

where k is a constant.

(a) Find an expression for a_2 in terms of k . (1)

Given that $\sum_{i=1}^3 a_i = 2$,

(b) find the two possible values of k . (6)



Core Mathematics C1

Mensuration

$$\text{Surface area of sphere} = 4\pi r^2$$

$$\text{Area of curved surface of cone} = \pi r \times \text{slant height}$$

Arithmetic series

$$u_n = a + (n - 1)d$$

$$S_n = \frac{1}{2}n(a + l) = \frac{1}{2}n[2a + (n - 1)d]$$